

FOUNDATION OF DATA SCIENCE - UNIT I - INTRODUCTION

Data Science: Benefits and uses – facets of data - Data Science Process: Overview – Defining research goals – Retrieving data – Data preparation - Exploratory Data analysis – Build the model– presenting findings and building applications – Data Mining - Data Warehousing – Basic Statistical descriptions of Data

Data

In computing, data is information that has been translated into a form that is efficient for movement or processing

Data Science

Data science is an evolutionary extension of statistics capable of dealing with the massive amounts of data produced today. It adds methods from computer science to the repertoire of statistics.

Benefits and uses of data science

Data science and big data are used almost everywhere in both commercial and non commercial Settings

- Commercial companies in almost every industry use data science and big data to gain insights into their customers, processes, staff, completion, and products.
- Many companies use data science to offer customers a better user experience, as well as to cross-sell, up -sell, and personalize their offerings.
- Governmental organizations are also aware of data's value. Many governmental organizations not only rely on internal data scientists to discover valuable information, but also share their data with the public.
- Nongovernmental organizations (NGOs) use it to raise money and defend their causes.
- Universities use data science in their research but also to enhance the study experience of their students. The rise of massive open online courses (MOOC) produces a lot of data, which allow universities to study how this type of learning can complement traditional classes.

Facets of data

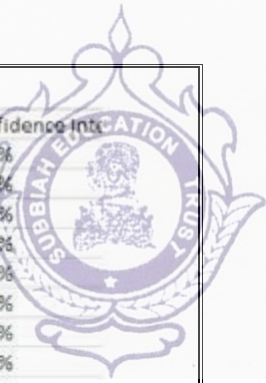
In data science and big data you'll come across many different types of data, and each of them tends to require different tools and techniques. The main categories of data are these:

- Structured
- Unstructured
- Natural language
- Machine-generated
- Graph-based
- Audio, video, and images
- Streaming

Let's explore all these interesting data types.

Structured data

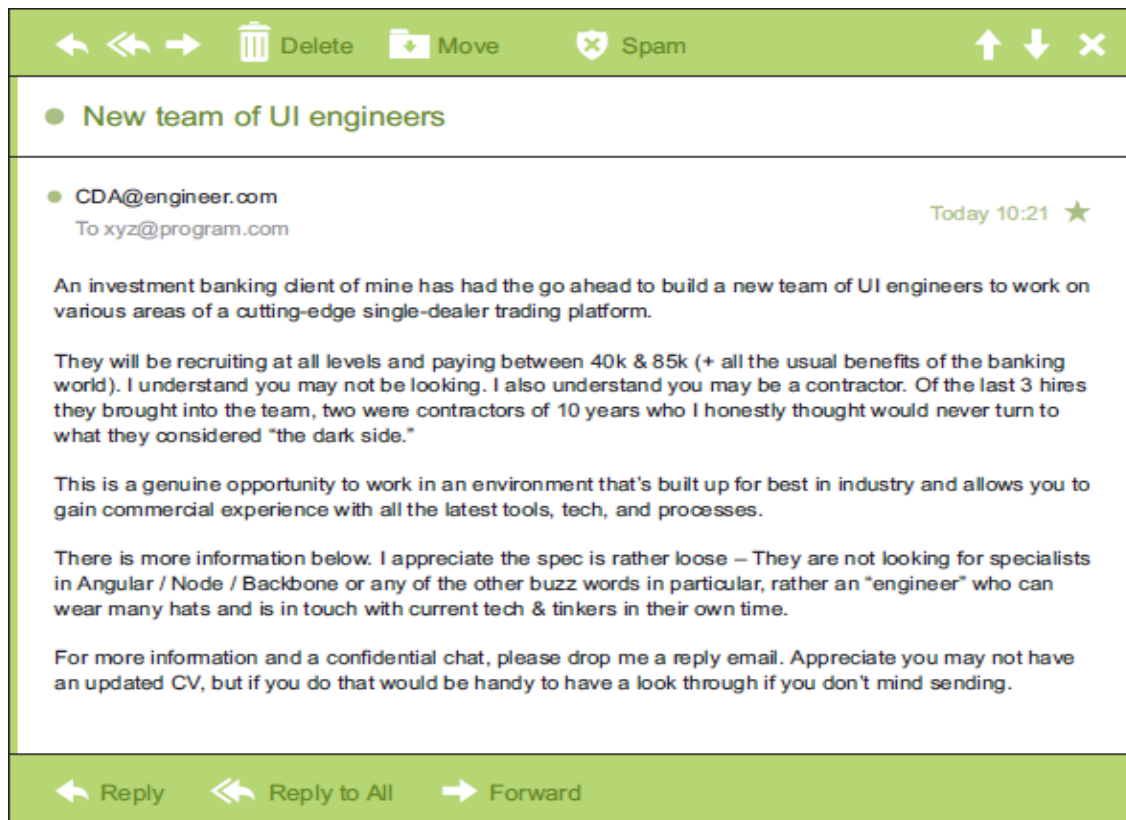
- Structured data is data that depends on a data model and resides in a fixed field within a record. As such, it's often easy to store structured data in tables within data bases or Excel files
- SQL, or Structured Query Language, is the preferred way to manage and query data that resides in data bases.



Indicator ID	Dimension List	Timeframe	Numeric Value	Missing Value Flag	Confidence Int
214390830	Total (Age-adjusted)	2008	74.6%		73.8%
214390833	Aged 18-44 years	2008	59.4%		58.0%
214390831	Aged 18-24 years	2008	37.4%		34.6%
214390832	Aged 25-44 years	2008	66.9%		65.5%
214390836	Aged 45-64 years	2008	88.6%		87.7%
214390834	Aged 45-54 years	2008	86.3%		85.1%
214390835	Aged 55-64 years	2008	91.5%		90.4%
214390840	Aged 65 years and over	2008	94.6%		93.8%
214390837	Aged 65-74 years	2008	93.6%		92.4%
214390838	Aged 75-84 years	2008	95.6%		94.4%
214390839	Aged 85 years and over	2008	96.0%		94.0%
214390841	Male (Age-adjusted)	2008	72.2%		71.1%
214390842	Female (Age-adjusted)	2008	76.8%		75.9%
214390843	White only (Age-adjusted)	2008	73.8%		72.9%
214390844	Black or African American only (Age-adjusted)	2008	77.0%		75.0%
214390845	American Indian or Alaska Native only (Age-adjusted)	2008	66.5%		57.1%
214390846	Asian only (Age-adjusted)	2008	80.5%		77.7%
214390847	Native Hawaiian or Other Pacific Islander only (Age-adjusted)	2008	DSU		
214390848	2 or more races (Age-adjusted)	2008	75.6%		69.6%

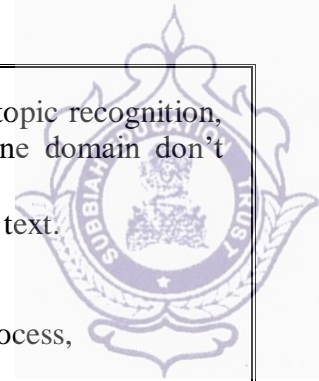
Unstructured data

Unstructured data is data that isn't easy to fit into a data model because the content is context-specific or varying. One example of unstructured data is your regular email.



Natural language

- Natural language is a special type of unstructured data; it's challenging to process because it requires knowledge of specific data science techniques and linguistics.



- The natural language processing community has had success in entity recognition, topic recognition, summarization, text completion, and sentiment analysis, but models trained in one domain don't generalize well to other domains.
- Even state-of-the-art techniques aren't able to decipher the meaning of every piece of text.

Machine-generated data

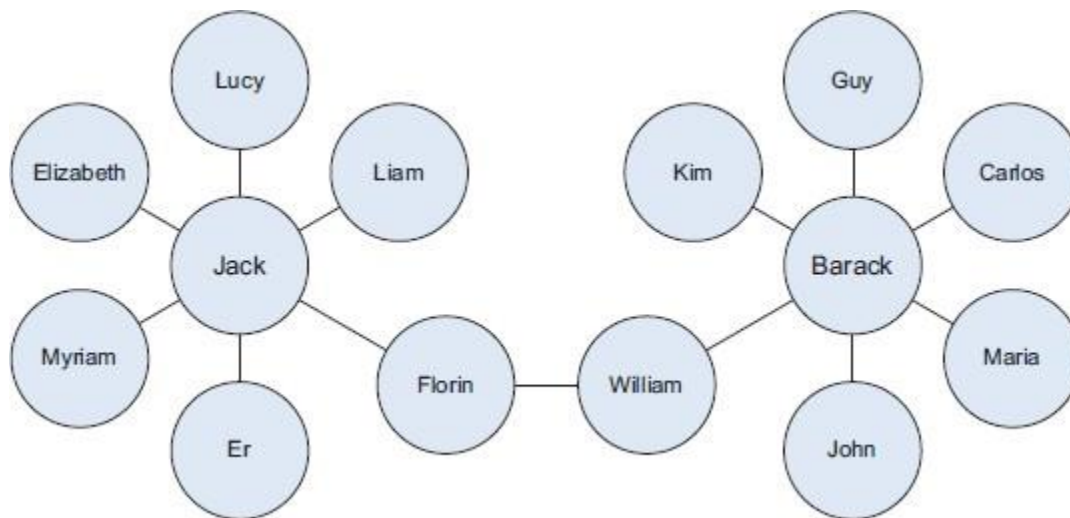
- Machine-generated data is information that's automatically created by a computer, process, application, or other machine without human intervention.
- Machine-generated data is becoming a major data resource and will continue to do so.
- The analysis of machine data relies on highly scalable tools, due to its high volume and speed. Examples of machine data are web server logs, called tail records, network event logs, and telemetry.

```

CSIPERF:TXCOMMIT:313236
2014-11-28 11:36:13, Info          CSI    00000153 Creating NT transaction (seq
69), objectname [6]"(null)"
2014-11-28 11:36:13, Info          CSI    00000154 Created NT transaction (seq 69)
result 0x00000000, handle @0x4e54
2014-11-28 11:36:13, Info          CSI    00000155@2014/11/28:10:36:13.471
Beginning NT transaction commit...
2014-11-28 11:36:13, Info          CSI    00000156@2014/11/28:10:36:13.705 CSI perf
    
```

Graph-based or network data

- "Graph data" can be a confusing term because any data can be show nina graph.
- Graphornetworkdatais,in short, datathat focuseson therelationshipor adjacencyof objects.
- Thegraphstructuresuse nodes,edges,andpropertytorepresentandstoregraphicaldata.
- Graph-baseddataisanaturalwaytorepresentsocialnetworks,anditsstructureallows you tocalulatespecificmetricssuchasthe influenceofapersonand the shortestpath betweentwo people.



Audio, image, and video

- Audio, image, and video are data types that pose specific challenges to a data scientist.
- Tasks that are trivial for humans, such as recognizing objects in pictures, turn out to be challenging for computers.
- MLBAM (Major League Baseball Advanced Media) announced in 2014 that they'll increase video capture to approximately 7 TB per game for the purpose of live, in-game analytics.
- Recently a company called DeepMind succeeded at creating an algorithm that's capable of learning how to play video games.
- This algorithm takes the video screen as input and learns to interpret everything via a complex of deep learning.



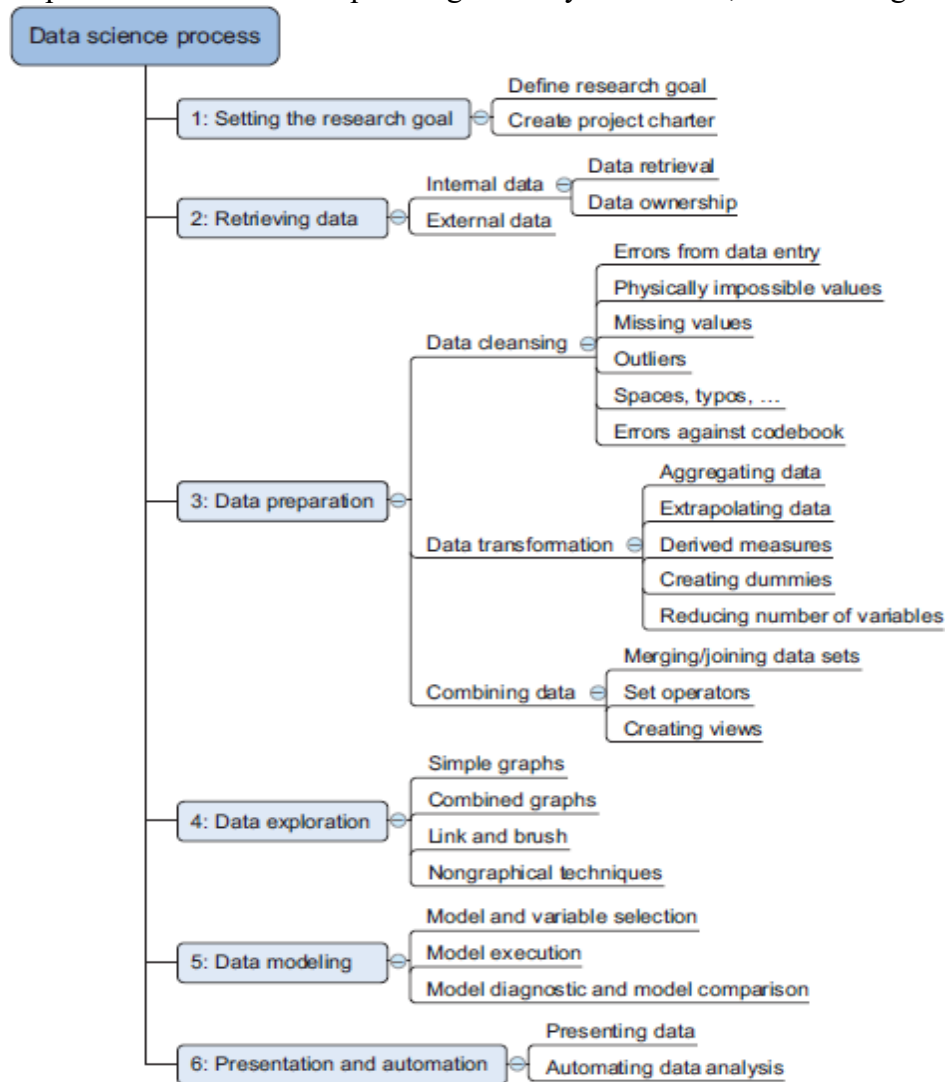
Streaming data

- The data flows into the system when an event happens instead of being loaded into a data store in a batch.
- Examples are the “What’s trending” on Twitter, live sporting or music events, and the stock market.

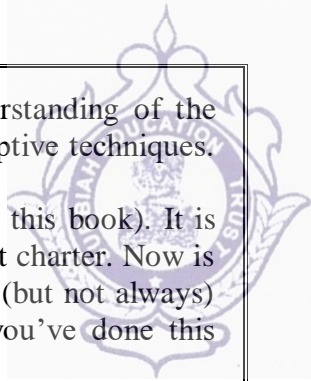
Data Science Process

Overview of the data science process

The typical data science process consists of six steps through which you’ll iterate, as shown in figure



1. The first step of this process is setting a research goal. The main purpose here is making sure all the stakeholders understand the what, how, and why of the project. In every serious project this will result in a project charter.
2. The second phase is data retrieval. You want to have data available for analysis, so this step includes finding suitable data and getting access to the data from the data owner. The result is data in its raw form, which probably needs polishing and transformation before it becomes usable.
3. Now that you have the raw data, it’s time to prepare it. This includes transforming the data from a raw form into data that’s directly usable in your models. To achieve this, you’ll detect and correct different kinds of errors in the data, combine data from different data sources, and transform it. If you have successfully completed this step, you can progress to data visualization and modeling.



4. The fourth step is data exploration. The goal of this step is to gain a deep understanding of the data. You'll look for patterns, correlations, and deviations based on visual and descriptive techniques. The insights you gain from this phase will enable you to start modeling.
5. Finally, we get to model building (often referred to as "data modeling" throughout this book). It is now that you attempt to gain the insights or make the predictions stated in your project charter. Now is the time to bring out the heavy guns, but remember research has taught us that often (but not always) a combination of simple models tends to outperform one complicated model. If you've done this phase right, you're almost done.
6. The last step of the data science model is presenting your results and automating the analysis, if needed. One goal of a project is to change a process and/or make better decisions. You may still need to convince the business that your findings will indeed change the business process as expected. This is where you can shine in your influencer role. The importance of this step is more apparent in projects on a strategic and tactical level. Certain projects require you to perform the business process over and over again, so automating the project will save time.

Defining research goals

A project starts by understanding the *what*, the *why*, and the *how* of your project. The outcome should be a clear research goal, a good understanding of the context, well-defined deliverables, and a plan of action with a timetable. This information is then best placed in a project charter.

Spend time understanding the goals and context of your research

- An essential outcome is the research goal that states the purpose of your assignment in a clear and focused manner.
- Understanding the business goals and context is critical for project success.
- Continue asking questions and devising examples until you grasp the exact business expectations, identify how your project fits in the bigger picture, appreciate how your research is going to change the business, and understand how they'll use your results

Create a project charter

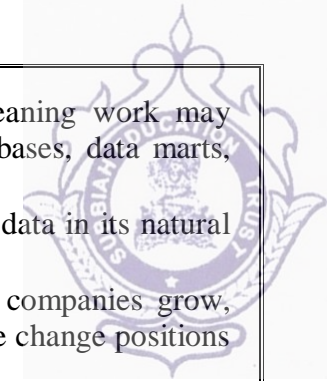
A project charter requires teamwork, and your input covers at least the following:

- A clear research goal
- The project mission and context
- How you're going to perform your analysis
- What resources you expect to use
- Proof that it's an achievable project, or proof of concepts
- Deliverables and a measure of success
- A timeline

Retrieving data

- The next step in data science is to retrieve the required data. Sometimes you need to go into the field and design a data collection process yourself, but most of the time you won't be involved in this step.
- Many companies will have already collected and stored the data for you, and what they don't have can often be bought from third parties.
- More and more organizations are making even high-quality data freely available for public and commercial use.
- Data can be stored in many forms, ranging from simple text files to tables in a database. The objective now is acquiring all the data you need.

Start with data stored within the company (Internal data)



- Most companies have a program for maintaining key data, so much of the cleaning work may already be done. This data can be stored in official data repositories such as databases, data marts, data warehouses, and data lakes maintained by a team of IT professionals.
- Data warehouses and data marts are home to preprocessed data, data lakes contain data in its natural or raw format.
- Finding data even within your own company can sometimes be a challenge. As companies grow, their data becomes scattered around many places. The data may be dispersed as people change positions and leave the company.
- Getting access to data is another difficult task. Organizations understand the value and sensitivity of data and often have policies in place so everyone has access to what they need and nothing more.
- These policies translate into physical and digital barriers called *Chinese walls*. These “walls” are mandatory and well-regulated for customer data in most countries.

External Data

- If data isn’t available inside your organization, look outside your organizations. Companies provide data so that you, in turn, can enrich their services and ecosystem. Such is the case with Twitter, LinkedIn, and Facebook.
- More and more governments and organizations share their data for free with the world.
- A list of open data providers that should get you started.

Open data site	Description
Data.gov	The home of the US Government’s open data
https://open-data.europa.eu/	The home of the European Commission’s open data
Freebase.org	An open database that retrieves its information from sites like Wikipedia, MusicBrains, and the SEC archive
Data.worldbank.org	Open data initiative from the World Bank
Aiddata.org	Open data for international development
Open.fda.gov	Open data from the US Food and Drug Administration

Data Preparation (Cleansing, Integrating, Transforming Data)

Your model needs the data in a specific format, so data transformation will always come into play. It’s a good habit to correct data errors as early on in the process as possible. However, this isn’t always possible in a realistic setting, so you’ll need to take corrective actions in your program.

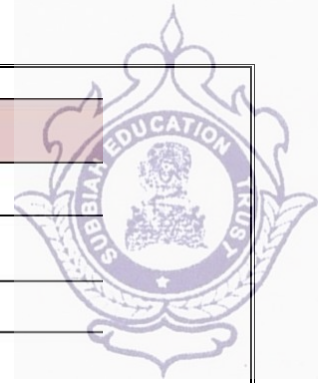
Cleansing data

Data cleansing is a subprocess of the data science process that focuses on removing errors in your data so your data becomes a true and consistent representation of the processes it originates from.

- The first type is the *interpretation error*, such as when you take the value in your data for granted, like saying that a person’s age is greater than 300 years.
- The second type of error points to *inconsistencies* between data sources or against your company’s standardized values.

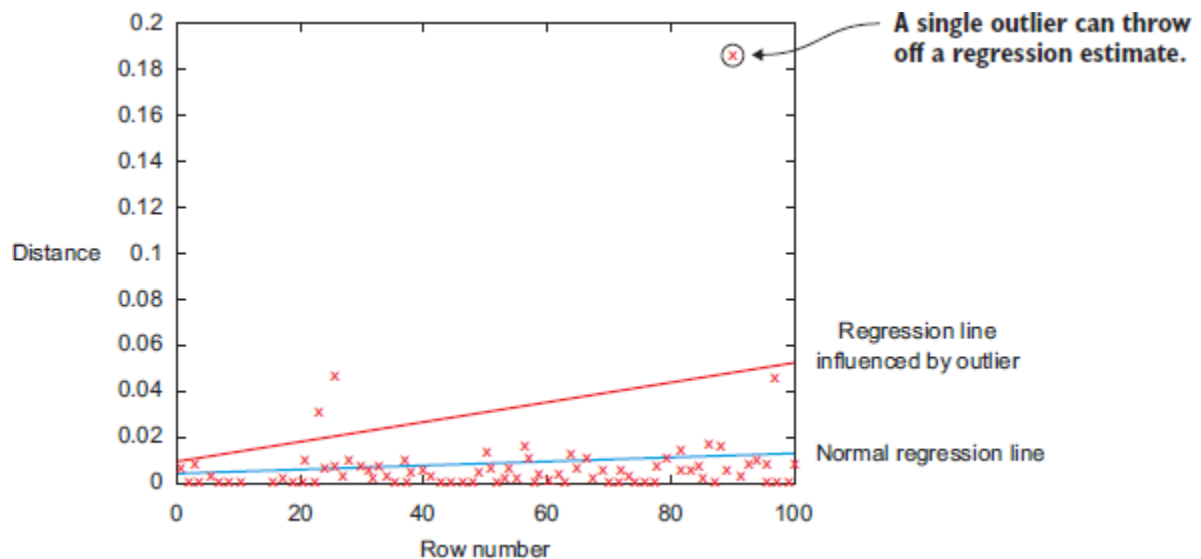
An example of this class of errors is putting “Female” in one table and “F” in another when they represent the same thing: that the person is female.

Overview of common errors



General solution	
Try to fix the problem early in the data acquisition chain or else fix it in the program.	
Error description	Possible solution
<i>Errors pointing to false values within one data set</i>	
Mistakes during data entry	Manual overrules
Redundant white space	Use string functions
Impossible values	Manual overrules
Missing values	Remove observation or value
Outliers	Validate and, if erroneous, treat as missing value (remove or insert)
<i>Errors pointing to inconsistencies between data sets</i>	
Deviations from a code book	Match on keys or else use manual overrules
Different units of measurement	Recalculate
Different levels of aggregation	Bring to same level of measurement by aggregation or extrapolation

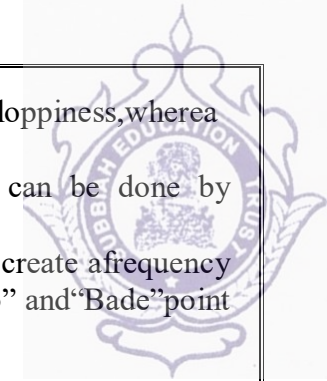
Sometimes you'll use more advanced methods, such as simple modeling, to find and identify data errors; diagnostic plots can be especially insightful. For example, in figure we use a measure to identify data points that seem out of place. We do a regression to get acquainted with the data and detect the influence of individual observations on the regression line.



The encircled point influences the model heavily and is worth investigating because it can point to a region where you don't have enough data or might indicate an error in the data, but it also can be a valid data point.

Data Entry Errors

- Data collection and data entry are error-prone processes. They often require human intervention, and introduce an error into the chain.



- Data collected by machines or computers isn't free from errors. Errors can arise from human sloppiness, whereas others are due to machine or hardware failure.
- Detecting data errors when the variables you study don't have many classes can be done by tabulating the data with counts.
- When you have a variable that can take only two values: "Good" and "Bad", you can create a frequency table and see if those are truly the only two values present. In the table the values "Godo" and "Bade" point out something went wrong in at least 16 cases.

Value	Count
Good	1598647
Bad	1354468
Godo	15
Bade	1

Most errors of this type are easy to fix with simple assignment statements and if-then-else rules:

```
if x == "Godo":
    x = "Good"
if x == "Bade":
    x = "Bad"
```

Redundant Whitespace

- Whitespace tends to be hard to detect but cause errors like other redundant characters would.
- The whitespace cause the miss match in the string such as "FR " – "FR", dropping the observation that couldn't be matched.
- If you know to watch out for them, fixing redundant whitespaces is luckily easy enough in most programming languages. They all provide string functions that will remove the leading and trailing whitespaces. For instance, in Python you can use the strip() function to remove leading and trailing spaces.

Fixing Capital Letter Mismatches

Capital letter mismatches are common. Most programming languages make a distinction between "Brazil" and "brazil"

In this case you can solve the problem by applying a function that returns both strings in lowercase, such as .lower() in Python. "Brazil".lower() == "brazil".lower() should result in true.

Impossible Values and Sanity Checks

Here you check the value against physically or theoretically impossible values such as people taller than 3 meters or someone with an age of 299 years. Sanity checks can be directly expressed with rules:

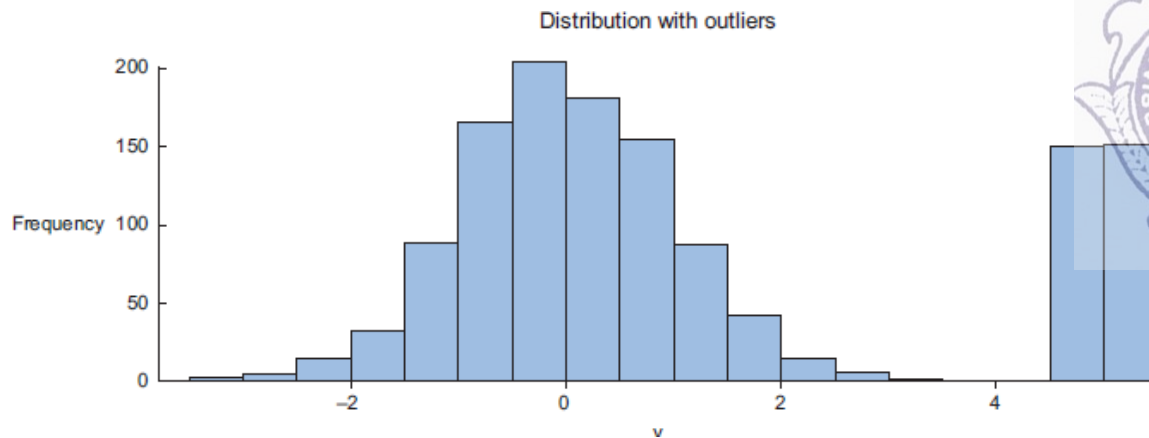
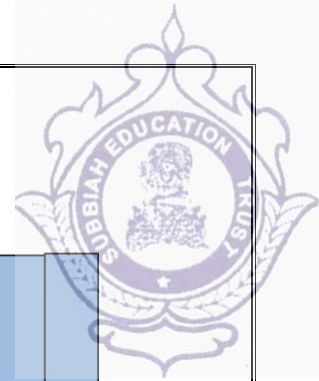
```
check = 0 <= age <= 120
```

Outliers

An outlier is an observation that seems to be distant from other observations or, more specifically, one observation that follows a different logic or generative process than the other observations. The easiest way to find outliers is to use a plot or a table with the minimum and maximum values.

The plot on the top shows no outliers, whereas the plot on the bottom shows possible outliers on the upper side when an normal distribution is expected.





Dealing with Missing Values

Missing values aren't necessarily wrong, but you still need to handle them separately; certain modeling techniques can't handle missing values. They might be an indicator that something went wrong in your data collection or that an error happened in the ETL process. Common techniques data scientists use are listed in table

Integrating data

Your data comes from several different places, and in this substep we focus on integrating these different sources. Data varies in size, type, and structure, ranging from databases and Excel files to text documents.

The Different Ways of Combining Data

You can perform two operations to combine information from different datasets.

- Joining
- Appending or stacking

Joining Tables

- Joining tables allows you to combine the information of one observation found in one table with the information that you find in another table. The focus is on enriching a single observation.
- Let's say that the first table contains information about the purchases of a customer and the other table contains information about the region where your customer lives.
- Joining the tables allows you to combine the information so that you can use it for your model, as shown in figure.

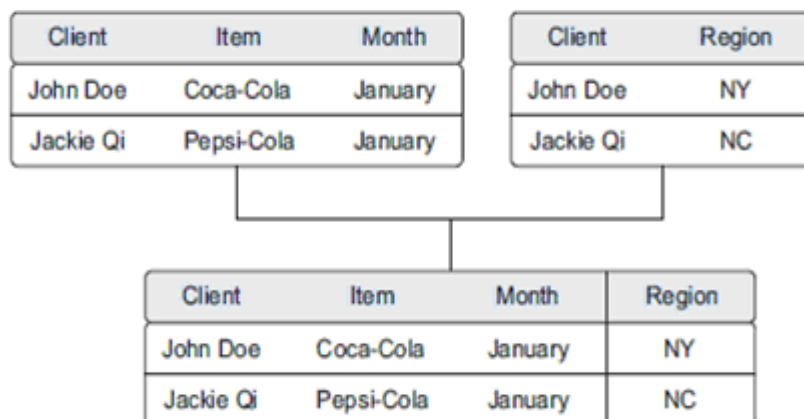
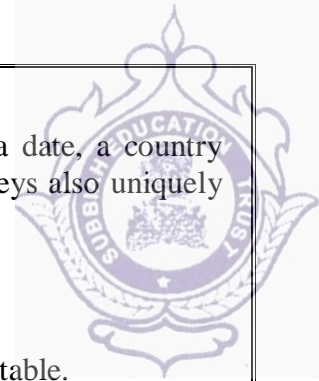


Figure. Joining two tables on the item and region key9



To join tables, you use variables that represent the same object in both tables, such as a date, a country name, or a Social Security number. These common fields are known as keys. When these keys also uniquely define the records in the table they are called *primary keys*.

The number of resulting rows in the output table depends on the exact joint type that you use

Appending Tables

- Appending or stacking tables is effectively adding observations from one table to another table.
- One table contains the observations from the month January and the second table contains observations from the month February. The result of appending these tables is a larger one with the observations from January as well as February.

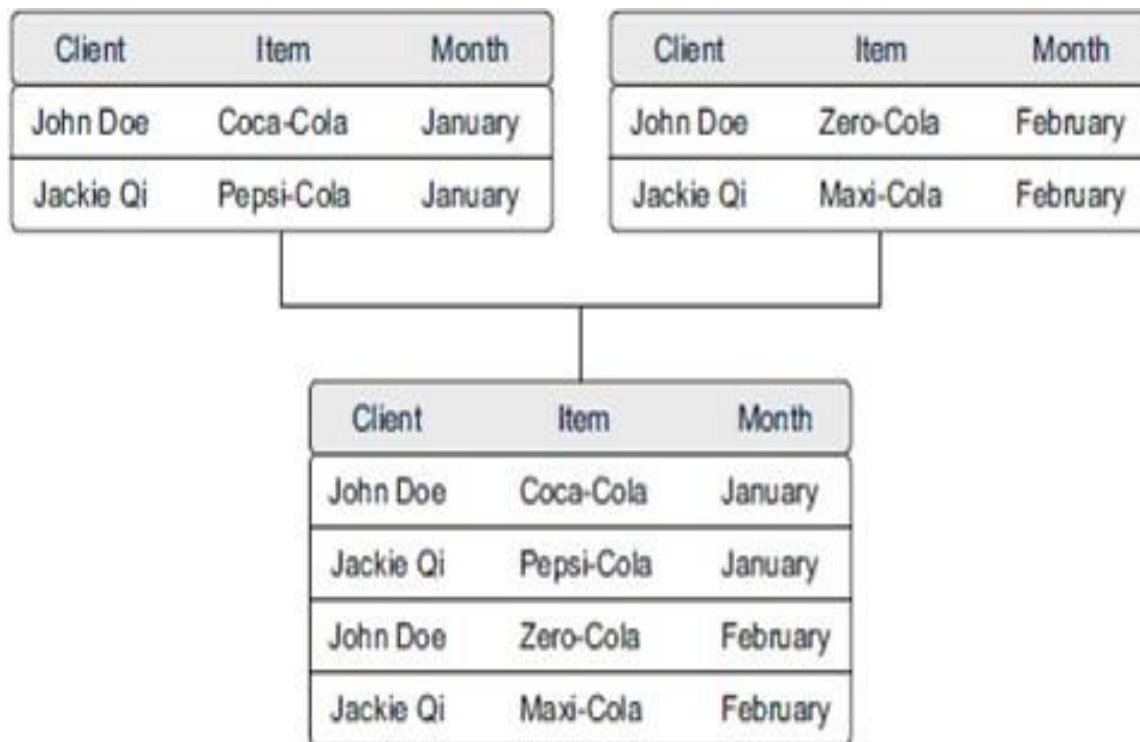
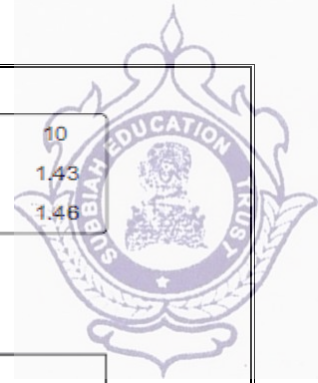


Figure. Appending data from tables is a common operation but requires an equal structure in the tables being appended,

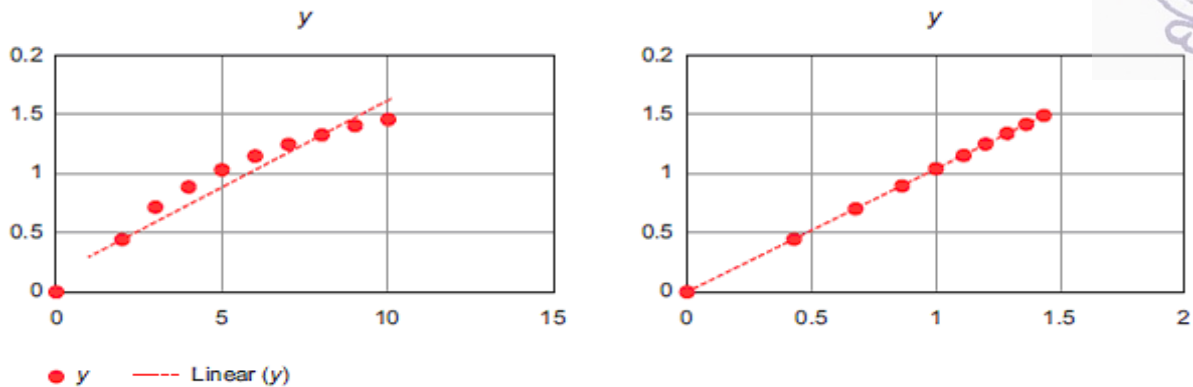
Transforming data

Certain models require their data to be in a certain shape. Transforming your data so it takes a suitable form for data modeling.

Relationships between an input variable and an output variable aren't always linear. Take, for instance, a relationship of the form $y = ae^{bx}$. Taking the log of the independent variables simplifies the estimation problem dramatically. Transforming the input variables greatly simplifies the estimation problem. Other times you might want to combine two variables into a new variable.



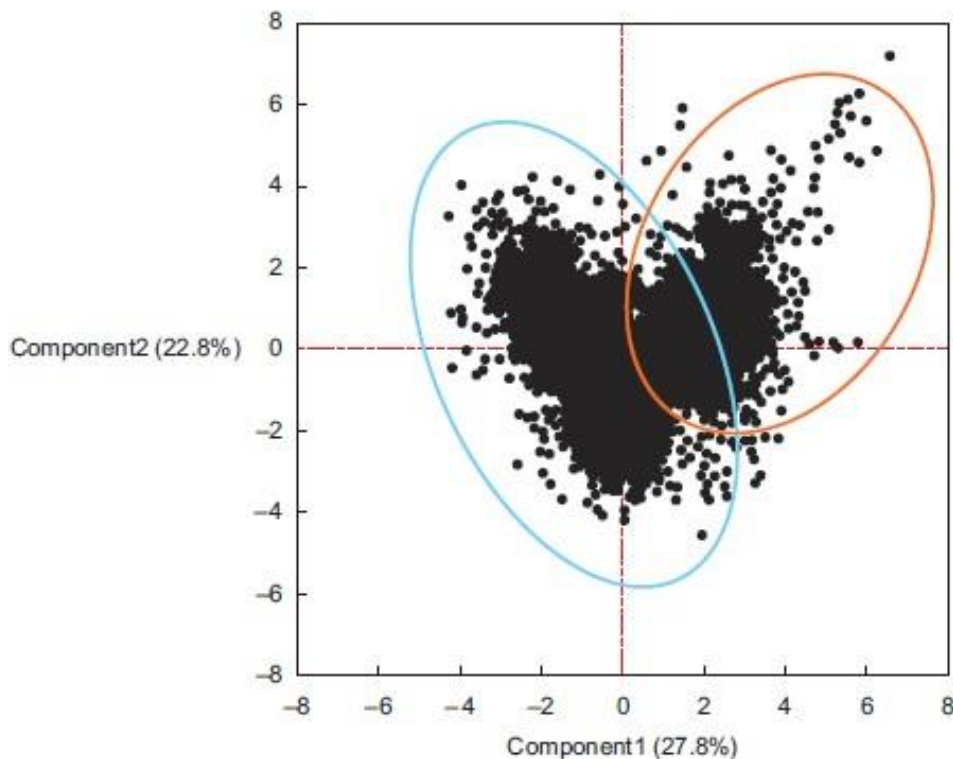
x	1	2	3	4	5	6	7	8	9	10
$\log(x)$	0.00	0.43	0.68	0.86	1.00	1.11	1.21	1.29	1.37	1.43
y	0.00	0.44	0.69	0.87	1.02	1.11	1.24	1.32	1.38	1.46



Transforming x to $\log x$ makes the relationship between x and y linear (right), compared with the non- $\log x$ (left).

Reducing the Number of Variables

- Having too many variables in your model makes the model difficult to handle, and certain techniques don't perform well when you overload them with too many input variables. For instance, all the techniques based on a Euclidean distance perform well only up to 10 variables.
- Data scientists use special methods to reduce the number of variables but retain the maximum amount of data.



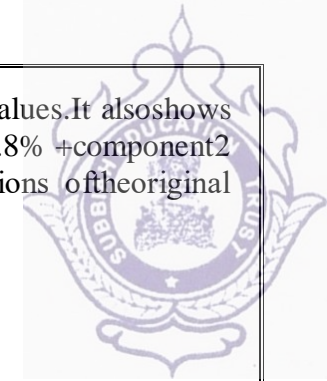


Figure shows how reducing the number of variables makes it easier to understand the key values. It also shows how two variables account for 50.6% of the variation within the data set (component1 = 27.8% + component2 = 22.8%). These variables, called “component1” and “component2,” are both combinations of the original variables. They’re the *principal components* of the underlying data structure

Turning Variables into Dummies

- *Dummy variables* can only take two values: true(1) or false(0). They’re used to indicate the absence of a categorical effect that may explain the observation.
- In this case you’ll make separate columns for the classes stored in one variable and indicate it with 1 if the class is present and 0 otherwise.
- An example is turning one column named *Weekdays* into the columns *Monday* through *Sunday*. You use an indicator to show if the observation was on a Monday; you put 1 on Monday and 0 elsewhere.
- Turning variables into dummies is a technique that’s used in modeling and is popular with, but not exclusive to, economists.

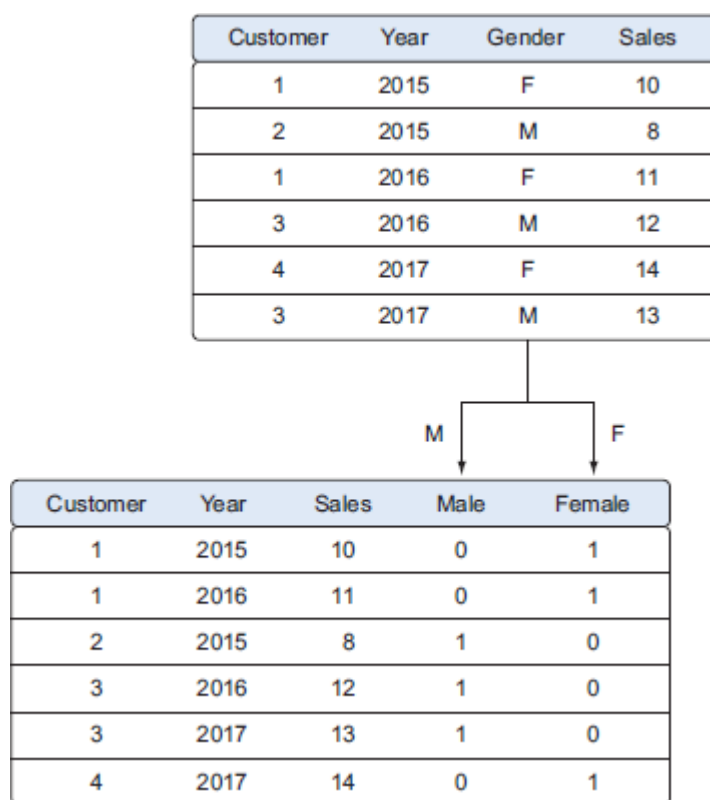
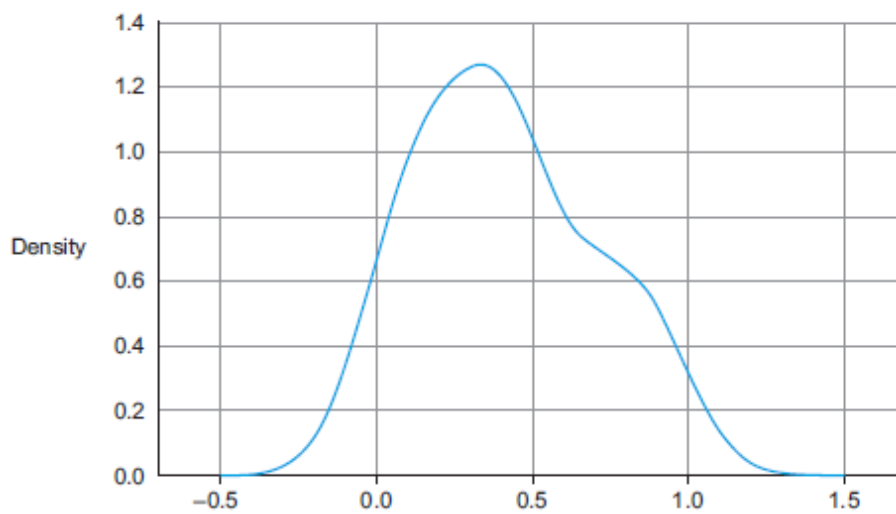
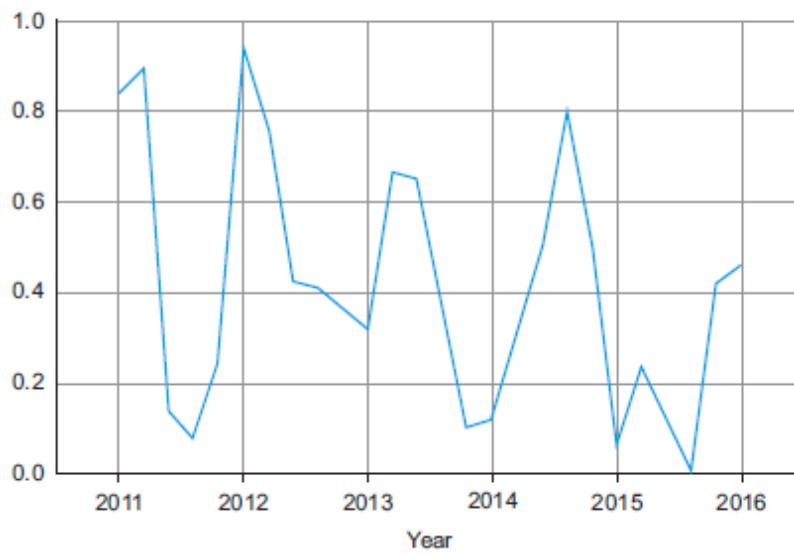
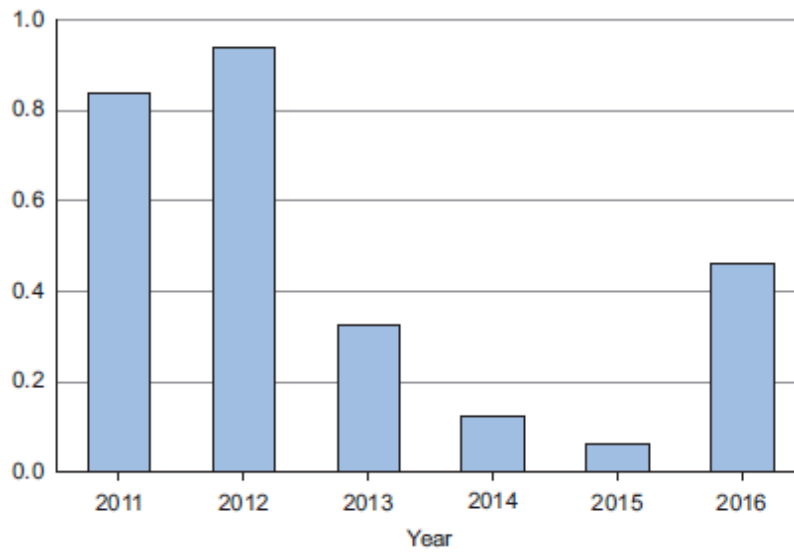


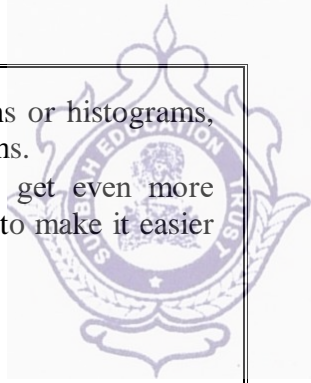
Figure. Turning variables into dummies is a data transformation that breaks a variable that has multiple classes into multiple variables, each having only two possible values: 0 or 1

Exploratory data analysis

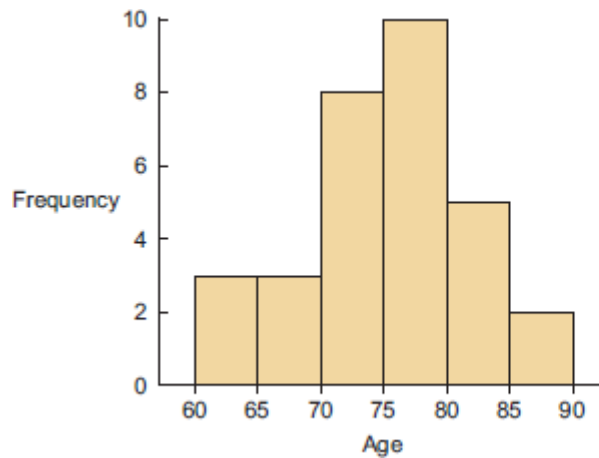
During exploratory data analysis you take a deep dive into the data (see figure below). Information becomes much easier to grasp when shown in a picture, therefore you mainly use graphical techniques to gain an understanding of your data and the interactions between variables. The goal isn’t to cleanse the data, but it’s common that you’ll still discover anomalies you missed before, forcing you to take a step back and fix them.



From top to bottom, a bar chart, a line plot, and a distribution are some of the graphs used in exploratory analysis.



- The visualization techniques you use in this phase range from simple line graphs or histograms, as shown in below figure, to more complex diagrams such as Sankey and network graphs.
- Sometimes it's useful to compose a composite graph from simple graphs to get even more insight into the data. Other times the graphs can be animated or made interactive to make it easier and, let's admit it, way more fun.



Example histogram:
the number of people in the age-groups of 5-year intervals

The techniques we described in this phase are mainly visual, but in practice they're certainly not limited to visualization techniques. Tabulation, clustering, and other modeling techniques can also be a part of exploratory analysis. Even building simple models can be a part of this step.

Build the models

- With clean data in place and a good understanding of the content, you're ready to build models with the goal of making better predictions, classifying objects, or gaining an understanding of the system that you're modeling.
- This phase is much more focused than the exploratory analysis step, because you know what you're looking for and what you want the outcome to be.

Building a model is an iterative process. The way you build your model depends on whether you go with classic statistics or the somewhat more recent machine learning school, and the type of technique you want to use. Either way, most models consist of the following main steps:

- Selection of a modeling technique and variables to enter in the model
- Execution of the model
- Diagnosis and model comparison

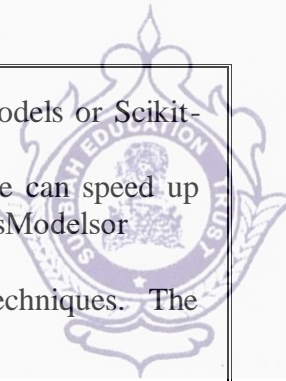
Model and variable selection

You'll need to select the variables you want to include in your model and a modeling technique. You'll need to consider model performance and whether your project meets all the requirements to use your model, as well as other factors:

- Must the model be moved to a production environment and, if so, would it be easy to implement?
- How difficult is the maintenance on the model: how long will it remain relevant if left untouched?
- Does the model need to be easy to explain?

Model execution

- Once you've chosen a model you'll need to implement it in code.



- Most programming languages, such as Python, already have libraries such as StatsModels or Scikit-learn. These packages use several of the most popular techniques.
- Coding a model is a nontrivial task in most cases, so having these libraries available can speed up the process. As you can see in the following code, it's fairly easy to use linear regression with StatsModels or Scikit-learn
- Doing this yourself would require much more effort even for the simple techniques. The following listing shows the execution of a linear prediction model.

```
import statsmodels.api as sm
import numpy as np
predictors = np.random.random(1000).reshape(500,2)
target = predictors.dot(np.array([0.4, 0.6])) + np.random.random(500)
lmRegModel = sm.OLS(target,predictors)
result = lmRegModel.fit()
result.summary()
```

Imports required Python modules.

Shows model fit statistics.

Fits linear regression on data.

Creates random data for predictors (x-values) and semi-random data for the target (y-values) of the model. We use predictors as input to create the target so we infer a correlation here.

Model diagnostics and model comparison

- You'll be building multiple models from which you then choose the best one based on multiple criteria. Working with a holdout sample helps you pick the best-performing model.
- A holdout sample is a part of the data you leave out of the model building so it can be used to evaluate the model afterward.
- The principle here is simple: the model should work on unseen data. You use only a fraction of your data to estimate the model and the other part, the holdout sample, is kept out of the equation.
- The model is then unleashed on the unseen data and error measures are recalculated to evaluate it.
- Multiple error measures are available, and in figure we show the general idea on comparing models. The error measure used in the example is the mean square error.

Formula for mean square error.

$$MSE = \frac{1}{n} \sum_{i=1}^n (\hat{Y}_i - Y_i)^2$$

Mean square error is a simple measure: check for every prediction how far it was from the truth, square this error, and add up the error of every prediction.



	<i>n</i>	Size	Price	Predicted model 1	Predicted model 2	Error model 1	Error model 2
80% train	1	10	3				
	2	15	5				
	3	18	6				
	4	14	5				
					
20% test	800	9	3				
	801	12	4	12	10	0	2
	802	13	4	12	10	1	3
	...						
	999	21	7	21	10	0	11
	1000	10	4	12	10	-2	0
Total						5861	110225

A holdout sample helps you compare models and ensures that you can generalize results to data that the model has not yet seen.

Above figure compares the performance of two models to predict the order size from the price. The first model is $size=3$ * $price$ and the second model is $size=10$.

- To estimate the models, we use 800 randomly chosen observations out of 1,000 (or 80%), without showing the other 20% of data to the model.
- Once the model is trained, we predict the values for the other 20% of the variables based on those for which we already know the true value, and calculate the model error with an error measure.
- Then we choose the model with the lowest error. In this example we chose model 1 because it has the lowest total error.

Many models make strong assumptions, such as independence of the inputs, and you have to verify that these assumptions are indeed met. This is called *model diagnostics*.

Presenting findings and building applications

- Sometimes people get so excited about your work that you'll need to repeat it over and over again because they value the predictions of your models or the insights that you produced.
- This doesn't always mean that you have to redo all of your analysis all the time. Sometimes it's sufficient that you implement only the model scoring; other times you might build an application that automatically updates reports, Excel spreadsheets, or PowerPoint presentations. The last stage of the data science process is where your *soft skills* will be most useful, and yes, they're extremely important.

Data mining

Data mining is the process of discovering actionable information from large sets of data. Data mining uses mathematical analysis to derive patterns and trends that exist in data. Typically, these patterns cannot be discovered by traditional data exploration because the relationships are too complex or because there is too much data.

These patterns and trends can be collected and defined as a *data mining model*. Mining models can be applied to specific scenarios, such as:

- **Forecasting:** Estimating sales, predicting server loads or server downtime



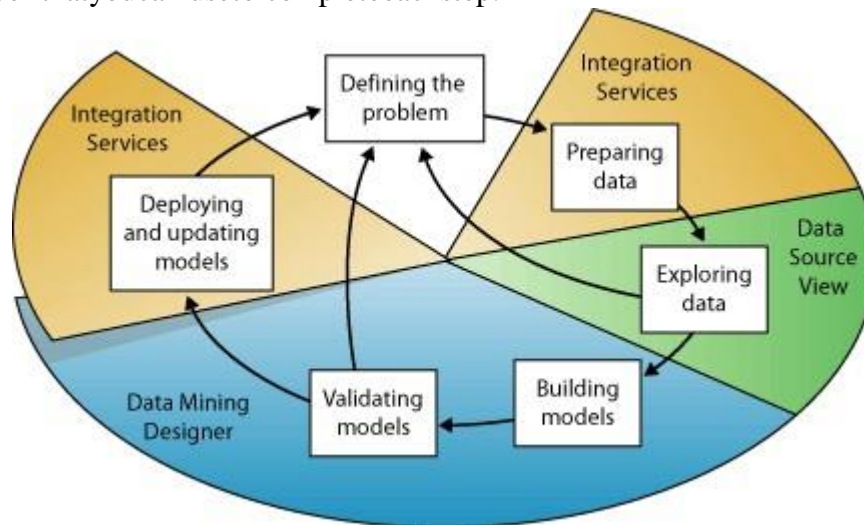
- **Risk and probability:** Choosing the best customers for targeted mailings, determining the probable break-even point for risk scenarios, assigning probabilities to diagnoses or other outcomes
- **Recommendations:** Determining which products are likely to be sold together, generating recommendations
- **Finding sequences:** Analyzing customer selections in a shopping cart, predicting next likely events
- **Grouping:** Separating customers or events into clusters of related items, analyzing and predicting affinities

Building a mining model is part of a larger process that includes everything from asking questions about the data and creating a model to answer those questions, to deploying the model into a working environment.

This process can be defined by using the following six basic steps:

1. Defining the Problem
2. Preparing Data
3. Exploring Data
4. Building Models
5. Exploring and Validating Models
6. Deploying and Updating Models

The following diagram describes the relationships between each step in the process, and the technologies in Microsoft SQL Server that you can use to complete each step.

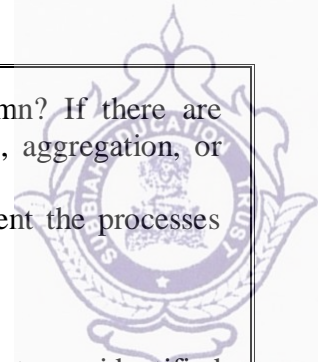


Defining the Problem

The first step in the data mining process is to clearly define the problem, and consider ways that data can be utilized to provide an answer to the problem.

This step includes analyzing business requirements, defining the scope of the problem, defining the metrics by which the model will be evaluated, and defining specific objectives for the data mining project. These tasks translate into questions such as the following:

- What are you looking for? What types of relationships are you trying to find?
- Does the problem you are trying to solve reflect the policies or processes of the business?
- Do you want to make predictions from the data mining model, or just look for interesting patterns and associations?
- Which outcome or attribute do you want to try to predict?



- What kind of data do you have and what kind of information is in each column? If there are multiple tables, how are the tables related? Do you need to perform any cleansing, aggregation, or processing to make the data usable?
- How is the data distributed? Is the data seasonal? Does the data accurately represent the processes of the business?

Preparing Data

- The second step in the data mining process is to consolidate and clean the data that was identified in the Defining the Problem step.
- Data can be scattered across a company and stored in different formats, or may contain inconsistencies such as incorrect or missing entries.
- Data cleaning is not just about removing bad data or interpolating missing values, but about finding hidden correlations in the data, identifying sources of data that are the most accurate, and determining which columns are the most appropriate for use in analysis.

Exploring Data

Exploration techniques include calculating the minimum and maximum values, calculating mean and standard deviations, and looking at the distribution of the data. For example, you might determine by reviewing the maximum, minimum, and mean values that the data is not representative of your customers or business processes, and that you therefore must obtain more balanced data or review the assumptions that are the basis for your expectations. Standard deviations and other distribution values can provide useful information about the stability and accuracy of the results.

Building Models

The mining structure is linked to the source of data, but does not actually contain any data until you process it. When you process the mining structure, SQL Server Analysis Services generates aggregates and other statistical information that can be used for analysis. This information can be used by any mining model that is based on the structure.

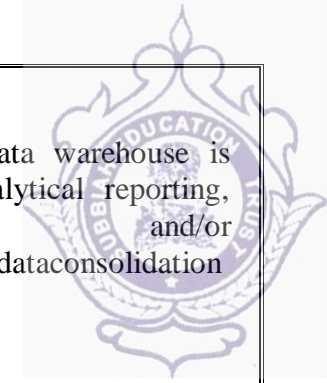
Exploring and Validating Models

Before you deploy a model into a production environment, you will want to test how well the model performs. Also, when you build a model, you typically create multiple models with different configurations and test all models to see which yields the best results for your problem and your data.

Deploying and Updating Models

After the mining models exist in a production environment, you can perform many tasks, depending on your needs. The following are some of the tasks you can perform:

- Use the model to create predictions, which you can then use to make business decisions.
- Create content queries to retrieve statistics, rules, or formulas from the model.
- Embed data mining functionality directly into an application. You can include Analysis Management Objects (AMO), which contains a set of objects that your application can use to create, alter, process, and delete mining structures and mining models.
- Use Integration Services to create a package in which a mining model is used to intelligently separate incoming data into multiple tables.
- Create a report that lets users directly query against an existing mining model.
- Update the models after review and analysis. Any update requires that you reprocess the models.
- Update the models dynamically, as more data comes into the organization, and making constant changes to improve the effectiveness of the solution should be part of the deployment strategy.



Data warehousing

Data warehousing is the process of constructing and using a data warehouse. A data warehouse is constructed by integrating data from multiple heterogeneous sources that support analytical reporting, structured and/or ad hoc queries, and decision making. Data warehousing involves data cleaning, data integration, and data consolidation.

Characteristics of data warehouse

The main characteristics of a data warehouse are as follows:

- **Subject-Oriented**
A data warehouse is subject-oriented since it provides topic-wise information rather than the overall processes of a business. Such subjects may be sales, promotion, inventory, etc.
- **Integrated**
A data warehouse is developed by integrating data from varied sources into a consistent format. The data must be stored in the warehouse in a consistent and universally acceptable manner in terms of naming, format, and coding. This facilitates effective data analysis.
- **Non-Volatile**
Data once entered into a data warehouse must remain unchanged. All data is read-only. Previous data is not erased when current data is entered. This helps you to analyze what has happened and when.
- **Time-Variant**
The data stored in a data warehouse is documented with an element of time, either explicitly or implicitly. An example of time variance in Data Warehouse is exhibited in the Primary Key, which must have an element of time like the day, week, or month.

Database vs. Data Warehouse

Although a data warehouse and a traditional database share some similarities, they need not be the same idea. The main difference is that in a database, data is collected for multiple transactional purposes. However, in a data warehouse, data is collected on an extensive scale to perform analytics. Databases provide real-time data, while warehouses store data to be accessed for big analytical queries.

Data Warehouse Architecture

Usually, data warehouse architecture comprises a three-tier structure.

Bottom Tier

The bottom tier or data warehouse server usually represents a relational database system. Back-end tools are used to cleanse, transform and feed data into this layer.

Middle Tier

The middle tier represents an OLAP server that can be implemented in two ways.

The ROLAP or Relational OLAP model is an extended relational database management system that maps multidimensional data to a standard relational process.

The MOLAP or multidimensional OLAP directly acts on multidimensional data and operations.

Top Tier

This is the front-end client interface that gets data out from the data warehouse. It holds various tools like query tools, analysis tools, reporting tools, and data mining tools.

How Data Warehouse Works

Data Warehousing integrates data and information collected from various sources into one comprehensive database. For example, a data warehouse might combine customer information from an organization's point-of-sale systems, its mailing lists, website, and comment cards. It might also incorporate confidential





information about employees, salary information, etc. Businesses use such components of data warehouse to analyze customers.

Data mining is one of the features of a data warehouse that involves looking for meaningful data patterns in vast volumes of data and devising innovative strategies for increased sales and profits.

Types of Data Warehouse

There are three main types of data warehouse.

Enterprise Data Warehouse (EDW)

This type of warehouse serves as a key or central database that facilitates decision-support services throughout the enterprise. The advantage to this type of warehouse is that it provides access to cross-organizational information, offers a unified approach to data representation, and allows running complex queries.

Operational Data Store (ODS)

This type of data warehouse refreshes in real-time. It is often preferred for routine activities like storing employee records. It is required when data warehouse systems do not support reporting needs of the business.

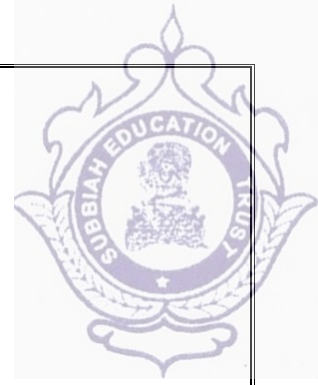
Data Mart

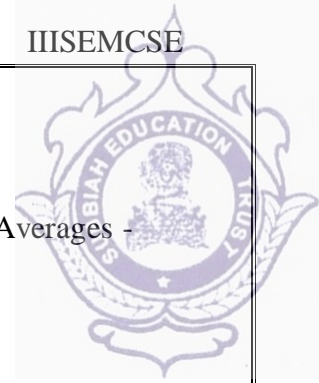
A data mart is a subset of a data warehouse built to maintain a particular department, region, or business unit. Every department of a business has a central repository or data mart to store data. The data from the data mart is stored in the ODS periodically. The ODS then sends the data to the EDW, where it is stored and used.

Summary

In this chapter you learned the data science process consists of six steps:

- *Setting the research goal*—Defining the what, the why, and the how of your project in a project charter.
- *Retrieving data*—Finding and getting access to data needed in your project. This data is either found within the company or retrieved from a third party.
- *Data preparation*—Checking and remediating data errors, enriching the data with data from other data sources, and transforming it into a suitable format for your models.
- *Data exploration*—Diving deeper into your data using descriptive statistics and visual techniques.
- *Data modeling*—Using machine learning and statistical techniques to achieve your project goal.
- *Presentation and automation*—Presenting your results to the stakeholders and industrializing your analysis process for repetitive reuse and integration with other tools.





Unit- II DESCRIBING DATA

Types of Data - Types of Variables - Describing Data with Tables and Graphs - Describing Data with Averages - Describing Variability - Normal Distributions and Standard (z) Scores

THREE TYPES OF DATA

- **Qualitative data** consist of words (Yes or No), letters (Y or N), or numerical codes (0 or 1) that represent a class or category.
- **Ranked data** consist of numbers (1st, 2nd, ... 40th place) that represent relative standing within a group.
- **Quantitative data** consist of numbers (weights of 238, 170, ... 185 lbs) that represent an amount or amount. To determine the type of data, focus on a single observation in any collection of observations

TYPES OF VARIABLES

Variable is a characteristic or property that can take on different values.

- The weights can be described not only as quantitative data but also as observations for a quantitative variable, since the various weights take on different numerical values.
- By the same token, the replies can be described as observations for a qualitative variable, since the replies to the Facebook profile question take on different values of either Yes or No.
- Given this perspective, any single observation can be described as a constant, since it takes on only one value.

Discrete and Continuous Variables

Quantitative variables can be further distinguished as **discrete** or **continuous**.

A **discrete variable** consists of isolated numbers separated by gaps.

Discrete variables can only assume specific values that you cannot subdivide. Typically, you count discrete values, and the results are integers.

Examples

- Counts - such as the number of children in a family. (1, 2, 3, etc., but never 1.5)
- These variables cannot have fractional or decimal values. You can have 20 or 21 cats, but not 20.5
- The number of heads in a sequence of coin tosses.
- The result of rolling a die.
- The number of patients in a hospital.
- The population of a country.

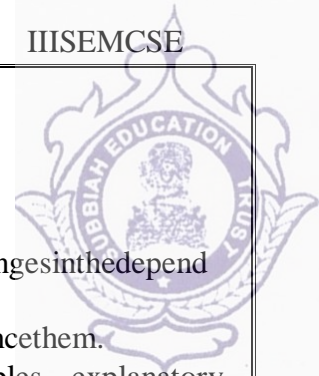
While discrete variables have no decimal places, the average of these values can be fractional. For example, families can have only a discrete number of children: 1, 2, 3, etc. However, the average number of children per family can be 2.2.

A **continuous variable** consists of numbers whose values, at least in theory, have no restrictions.

Continuous variables can assume any numeric value and can be meaningfully split into smaller parts. Consequently, they have valid fractional and decimal values. In fact, continuous variables have an infinite number of potential values between any two points. Generally, you measure them using a scale.

Examples of continuous variables include weight, height, length, time, and temperature.

Durations, such as the reaction times of grade school children to a fire alarm; and standardized test scores, such as those on the Scholastic Aptitude Test (SAT).



Independent and Dependent Variables

Independent Variable

In an experiment, an **independent variable** is the treatment manipulated by the investigator.

- Independent variables (IVs) are the ones that you include in the model to explain or predict changes in the dependent variable.
- Independent indicates that they stand alone and other variables in the model do not influence them.
- Independent variables are also known as predictors, factors, treatment variables, explanatory variables, input variables, x-variables, and right-hand variables—because they appear on the right side of the equation in a regression equation.
- It is a variable that stands alone and isn't changed by the other variables you are trying to measure.

For example, someone's age might be an independent variable. Other factors (such as what they eat, how much they go to school, how much television they watch)

The impartial creation of distinct groups, which differ only in terms of the independent variable, has a most desirable consequence. Once the data have been collected, any difference between the groups can be interpreted as being *caused* by the independent variable.

Dependent Variable

When a variable is believed to have been influenced by the independent variable, it is called a **dependent variable**. In an experimental setting, the dependent variable is measured, counted, or recorded by the investigator.

- The dependent variable (DV) is what you want to use the model to explain or predict. The values of this variable depend on other variables.
- It's also known as the response variable, outcome variable, and left-hand variable. Graphs place dependent variables on the vertical, or Y, axis.
- A dependent variable is exactly what it sounds like. It is something that depends on other factors.

For example, the blood sugar test depends on what food you ate, at what time you ate etc.

Unlike the independent variable, the dependent variable isn't manipulated by the investigator. Instead, it represents an outcome: the data produced by the experiment.

Confounding Variable

An *uncontrolled variable that compromises the interpretation of a study* is known as a **confounding variable**. Sometimes a confounding variable occurs because it's impossible to assign subjects randomly to different conditions.

Describing Data with Tables and Graphs

Frequency Distributions for Quantitative Data

- A frequency distribution is a collection of observations produced by sorting observations into classes and showing their frequency (f) of occurrence in each class.
- When observations are sorted into classes of single values, as in Table 2.1, the result is referred to as a frequency distribution for ungrouped data.
- The frequency distribution shown in Table 2.1 is only partially displayed because there are more than 100 possible values between the largest and smallest observations.

Frequency distribution table is much more informative if possible

observed values is less than 20. If more entries are observed then grouped data is used.

Grouped Data

According to their frequency of occurrence. When observations are sorted into classes of more than one value result is referred to as a frequency for grouped data. (Shown in table 2.2)

- The general structure of this frequency distribution is the data is grouped into class intervals with 10 possible values each.
- The frequency (f) column shows the frequency of observations in each class and, at the bottom, the total number of observations in all classes.

**Table 2.2 EDUCATION
FREQUENCY
DISTRIBUTION
(GROUPED DATA)**

WEIGHT	f
240-249	1
230-239	0
220-229	3
210-219	0
200-209	2
190-199	4
180-189	3
170-179	7
160-169	12
150-159	17
140-149	1
130-139	3
Total	53

GUIDELINES

**Table 2.3
FREQUENCY
DISTRIBUTION WITH
TOO MANY
INTERVALS**

WEIGHT	f
245-249	1
240-244	0
235-239	0
230-234	0
225-229	2
220-224	1
215-219	0
210-214	0
205-209	2
200-204	0
195-199	0
190-194	4
185-189	1
180-184	2
175-179	2
170-174	5
165-169	7
160-164	5
155-159	9
150-154	8
145-149	1
140-144	0
135-139	2
130-134	1
Total	53

**Table 2.4
FREQUENCY
DISTRIBUTION WITH
TOO FEW
INTERVALS**

WEIGHT	f
200-249	6
150-199	43
100-149	4
Total	53

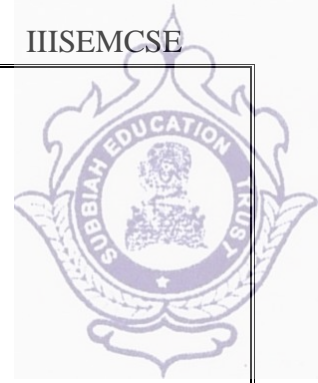
GUIDELINES FOR FREQUENCY DISTRIBUTIONS

Essential

- 1. Each observation should be included in one, and only one, class.**
Example: 130-139, 140-149, 150-159, etc. It would be incorrect to use 130-140, 140-150, 150-160, etc., in which, because the boundaries of classes overlap, an observation of 140 (or 150) could be assigned to either of two classes.
- 2. List all classes, even those with zero frequencies.**
Example: Listed in Table 2.2 is the class 210-219 and its frequency of zero. It would be incorrect to skip this class because of its zero frequency.
- 3. All classes should have equal intervals.**
Example: 130-139, 140-149, 150-159, etc. It would be incorrect to use 130-139, 140-159, etc., in which the second class interval (140-159) is twice as wide as the first class interval (130-139).

Optional

- 4. All classes should have both an upper boundary and a lower boundary.**
Example: 240-249. Less preferred would be 240-above, in which no maximum value can be assigned to observations in this class. (Nevertheless, this type of open-ended class is employed as a space-saving device when many different tables must be listed, as in the *Statistical Abstract of the United States*. An open-ended class appears in the table "Two Age Distributions" in Review Question 2.17 at the end of this chapter.)
- 5. Select the class interval from convenient numbers, such as 1, 2, 3, . . . 10, particularly 5 and 10 or multiples of 5 and 10.**
Example: 130-139, 140-149, in which the class interval of 10 is a convenient number. Less preferred would be 130-142, 143-155, etc., in which the class interval of 13 is not a convenient number.
- 6. The lower boundary of each class interval should be a multiple of the class interval.**
Example: 130-139, 140-149, in which the lower boundaries of 130, 140, are multiples of 10, the class interval. Less preferred would be 135-144, 145-154, etc., in which the lower boundaries of 135 and 145 are not multiples of 10, the class interval.
- 7. Aim for a total of approximately 10 classes.**
Example: The distribution in Table 2.2 uses 12 classes. Less preferred would be the distributions in Tables 2.3 and 2.4. The distribution in Table 2.3 has too many classes (24), whereas the distribution in Table 2.4 has too few classes (3).



CONSTRUCTING FREQUENCY DISTRIBUTIONS

1. **Find the range, that is**, the difference between the largest and smallest observations. The range of weights in Table 1.1 is $245 - 133 = 112$.
2. **Find the class interval required to span the range** by dividing the range by the desired number of classes (ordinarily 10). In the present example,

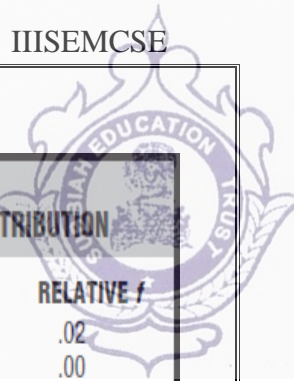
$$\text{Class interval} = \frac{\text{range}}{\text{desired number of classes}} = \frac{112}{10} = 11.2$$

3. **Round off to the nearest convenient interval** (such as 1, 2, 3, . . . 10, particularly 5 or 10 or multiples of 5 or 10). In the present example, the nearest convenient interval is 10.
4. **Determine where the lowest class should begin.** (Ordinarily, this number should be a multiple of the class interval.) In the present example, the smallest score is 133, and therefore the lowest class should begin at 130, since 130 is a multiple of 10 (the class interval).
5. **Determine where the lowest class should end** by adding the class interval to the lower boundary and then subtracting one unit of measurement. In the present example, add 10 to 130 and then subtract 1, the unit of measurement, to obtain 139—the number at which the lowest class should end.
6. **Working upward, list as many equivalent classes as are required to include the largest observation.** In the present example, list 130–139, 140–149, . . . , 240–249, so that the last class includes 245, the largest score.
7. **Indicate with a tally the class in which each observation falls.** For example, the first score in Table 1.1, 160, produces a tally next to 160–169; the next score, 193, produces a tally next to 190–199; and so on.
8. **Replace the tally count for each class with a number—the frequency (f)—and show the total of all frequencies.** (Tally marks are not usually shown in the final frequency distribution.)
9. **Supply headings for both columns and a title for the table.**

OUTLIERS

An outlier is an extremely high or extremely low data point relative to the nearest data point and the rest of the neighboring co-existing values in a data graph or data set you're working with.

Outliers are extreme values that stand out greatly from the overall pattern of values in a data set or graph.



RELATIVE FREQUENCY DISTRIBUTIONS

Relative frequency distributions show the frequency of each class as a part or fraction of the total frequency for the entire distribution.

This type of distribution is especially helpful when you must compare two or more distributions based on different total numbers of observations.

The conversion to relative frequencies allows a direct comparison of the shapes of two distributions without adjusting other observations.

Constructing Relative Frequency Distributions

To convert a frequency distribution into a relative frequency distribution, divide the frequency for each class by the total frequency for the entire distribution.

Table 2.5 illustrates a relative frequency distribution based on the eight distribution of Table 2.2.

Table 2.5
RELATIVE FREQUENCY DISTRIBUTION

WEIGHT	<i>f</i>	RELATIVE <i>f</i>
240-249	1	.02
230-239	0	.00
220-229	3	.06
210-219	0	.00
200-209	2	.04
190-199	4	.08
180-189	3	.06
170-179	7	.13
160-169	12	.23
150-159	17	.32
140-149	1	.02
130-139	<u>3</u>	<u>.06</u>
Total	53	1.02*

* The sum does not equal 1.00 because of rounding-off errors.

Percentages or Proportions

Some people prefer to deal with percentages rather than proportions because percentages usually lack decimal points. A proportion always varies between 0 and 1, whereas a percentage always varies between 0 percent and 100 percent.

To convert the relative frequencies, multiply each proportion by 100; that is, move the decimal point two places to the right.

CUMULATIVE FREQUENCY DISTRIBUTIONS

Cumulative frequency distributions show the total number of observations in each class and in all lower-ranked classes.

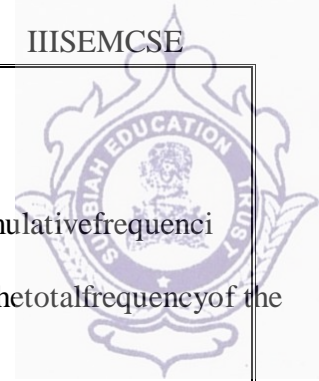
Cumulative frequencies are usually converted, in turn, to cumulative percentages. Cumulative percentages are often referred to as percentiles ranks.

Constructing Cumulative Frequency Distributions

To convert a frequency distribution into a cumulative frequency distribution, add to the frequency of each class the sum of the frequencies of all classes ranked below it.

Table 2.6
CUMULATIVE FREQUENCY DISTRIBUTION

WEIGHT	<i>f</i>	CUMULATIVE <i>f</i>	CUMULATIVE PERCENT
240-249	1	53	100
230-239	0	52	98
220-229	3	52	98
210-219	0	49	92
200-209	2	49	92
190-199	4	47	89
180-189	3	43	81
170-179	7	40	75
160-169	12	33	62
150-159	17	21	40
140-149	1	4	8
130-139	<u>3</u>	<u>3</u>	<u>6</u>
Total	53		



Cumulative Percentages

As has been suggested, if relative standing within a distribution is particularly important, then cumulative frequencies are converted to cumulative percentages. To obtain this cumulative percentage, the cumulative frequency of the class should be divided by the total frequency of the entire distribution.

Percentile Ranks

When used to describe the relative position of any score within its parent distribution, cumulative percentages are referred to as percentile ranks. The percentile rank of a score indicates the percentage of scores in the entire distribution with similar or smaller values than that score. Thus a weight has a percentile rank of 80 if equal or lighter weights constitute 80 percent of the entire distribution.

FREQUENCY DISTRIBUTIONS FOR QUALITATIVE (NOMINAL) DATA

Frequency distributions for qualitative data are easy to construct. Simply determine the frequency with which observations occupy each class, and report these frequencies as shown in Table 2.7 for the Facebook profile survey

Response	f
Yes	56
No	<u>27</u>
Total	83

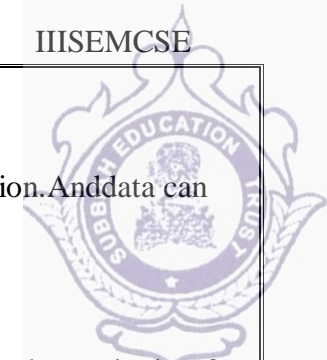
Qualitative data have an ordinal level of measurement because observations can be ordered from least to most, that order should be preserved in the frequency table

Relative and Cumulative Distributions for Qualitative Data

Frequency distributions for qualitative variables can always be converted into relative frequency distributions. If measurement is ordinal because observations can be ordered from least to most, cumulative frequencies (and cumulative percentages) can be used.

RANK	f	PROPORTION	CUMULATIVE PERCENT
General	311	.004*	100.0
Colonel	13,156	.167	99.6
Major	16,108	.204	82.9
Captain	29,169	.370	62.5
Lieutenant	<u>20,083</u>	.255	25.5
Total	78,827		

**To avoid a value of .00 for General, proportions are carried three places to the right of the decimal point.*



GRAPHS

Data can be described clearly and concisely with the aid of a well-constructed frequency distribution. And data can often be described even more vividly by converting frequency distributions into graphs.

GRAPHS FOR QUANTITATIVE DATA

Histograms

A bar-type graph for quantitative data. The common boundaries between adjacent bars emphasize the continuity of the data, as with continuous variables.

A histogram is a display of statistical information that uses rectangles to show the frequency of data items in successive numerical intervals of equal size.

Important features of histograms

- Equal units along the horizontal axis (the X axis, or abscissa) reflect the various class intervals of the frequency distribution.
- Equal units along the vertical axis (the Y axis, or ordinate) reflect increases in frequency. (The units along the vertical axis do not have to be the same width as those along the horizontal axis.)
- The intersection of the two axes defines the origin at which both numerical scales equal 0.
- Numerical scales always increase from left to right along the horizontal axis and from bottom to top along the vertical axis.
- The body of the histogram consists of a series of bars whose heights reflect the frequencies for the various classes.
- The adjacent bars in histogram have common boundaries that emphasize the continuity of quantitative data for continuous variables.
- The introduction of gaps between adjacent bars would suggest an artificial disruption in the data more appropriate for discrete quantitative variables or for qualitative variables.

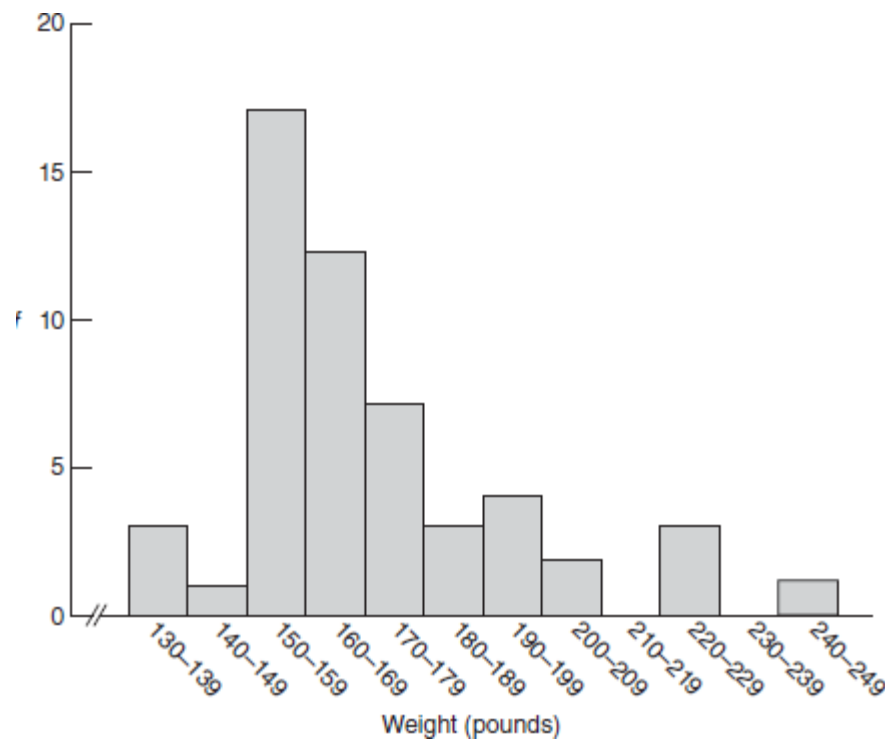


Figure: Histogram



Frequency Polygon

An important variation on a histogram is the frequency polygon, or line graph. Frequency polygons may be constructed directly from frequency distributions.

Step-by-step transformation of a histogram into a frequency polygon

- A. This panel shows the histogram for the weight distribution.
- B. Placedots at the midpointsof eachbartop or, intheabsenceof bartops, atmidpointsfor classesonthehorizontal axis, and connect them with straight lines.
- C. Anchor the frequency polygon to the horizontal axis. First, extend the upper tail to the midpoint ofthe first unoccupied class on the upper flank of the histogram. Then extend the lower tail to themidpoint of the first unoccupied class on the lower flank of the histogram. Now all of the area underthe frequency polygon is enclosed completely.
- D. Finally, eraseallof the histogrambars, leavingonlythe frequency polygon.

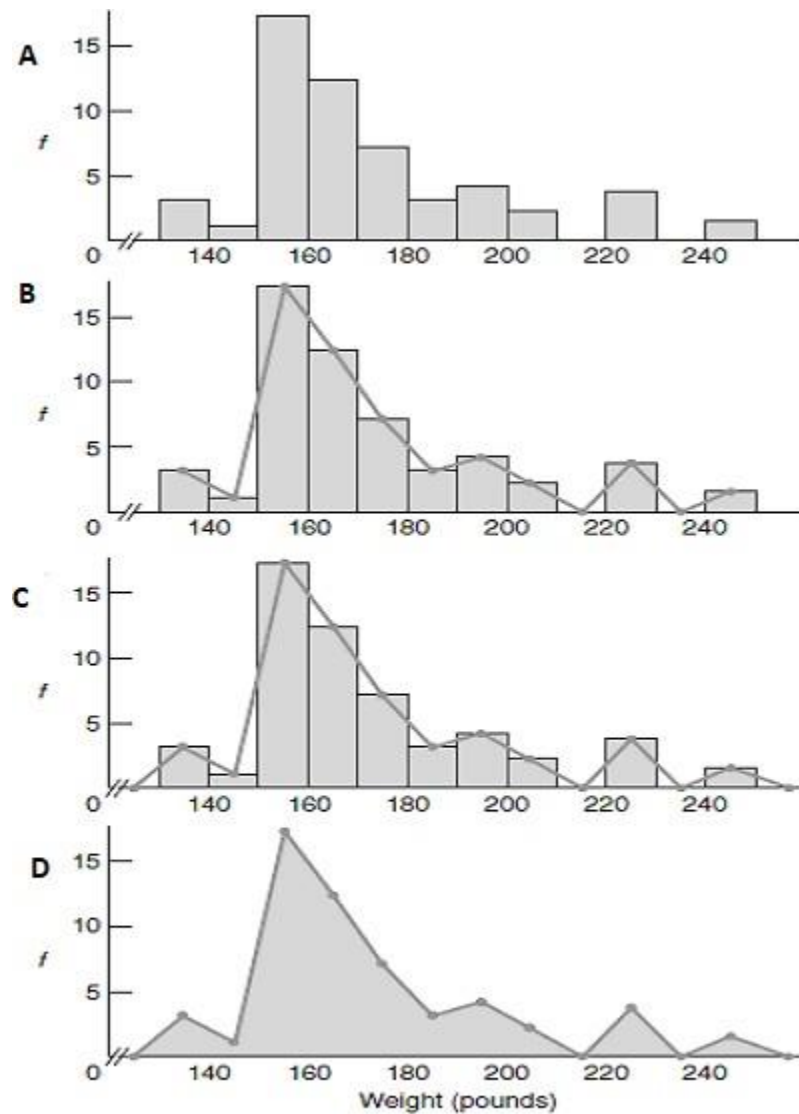
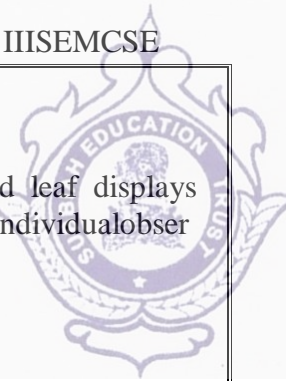


FIGURE Transition from histogram to frequency polygon.



Stem and Leaf Displays

Another technique for summarizing quantitative data is a stem and leaf display. Stem and leaf displays are ideal for summarizing distributions, such as that for weight data, without destroying the identities of individual observations.

Constructing Stem and Leaf Display

The leftmost panel of a table here creates the weights.

To construct the stem and leaf display for the table given below, first note that, when counting by tens, the weights range from the 130s to the 240s.

Arrange a column of numbers, the stems, beginning with 13 (representing the 130s) and ending with 24 (representing the 240s). Draw a vertical line to separate the stems, which represent multiples of 10, from the space to be occupied by the leaves, which represent multiples of 1.

For example

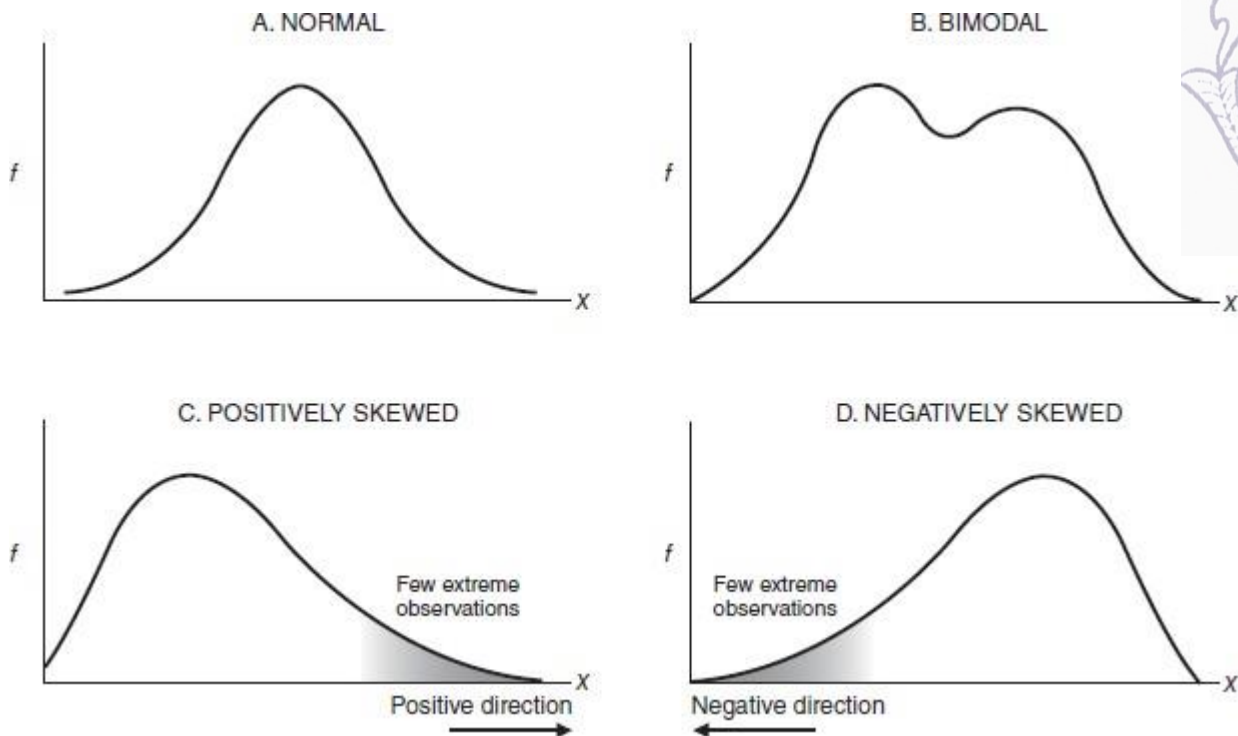
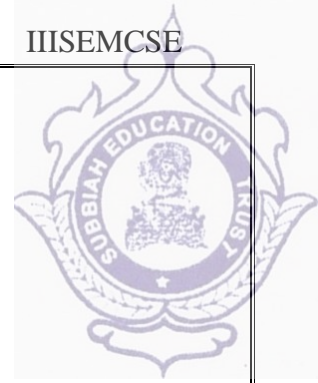
Enter each raw score into the stem and leaf display. As suggested by the shaded coding in Table 2.9, the first raw score of 160 reappears as a leaf of 0 on a stem of 16. The next raw score of 193 reappears as a leaf of 3 on a stem of 19, and the third raw score of 226 reappears as a leaf of 6 on a stem of 22, and so on, until each raw score reappears as a leaf on its appropriate stem.

Table 2.9
CONSTRUCTING STEM AND LEAF DISPLAY FROM WEIGHTS OF MALE STATISTICS STUDENTS

RAW SCORES				STEMS	STEM AND LEAF DISPLAY
160	165	135	175		
193	168	245	165	13	3 5 5
226	169	170	185	14	5
152	160	156	154	15	2 7 1 7 8 0 2 0 2 6 9 8 2 6 4 7 6
180	170	160	179	16	0 3 5 8 9 0 0 0 6 5 5 5
205	150	225	165	17	2 0 0 0 2 5 9
163	152	190	206	18	0 0 5
157	160	159	165	19	3 0 0 0
151	190	172	157	20	5 6
157	150	190	156	21	
220	133	166	135	22	6 0 5
145	180	158		23	
158	152	152		24	5
172	170	156			

TYPICAL SHAPES

Whether expressed as a histogram, a frequency polygon, or a stem and leaf display, an important characteristic of a frequency distribution is its shape. Below figure shows some of the more typical shapes for smoothed frequency polygons (which ignore the inevitable irregularities of real data).

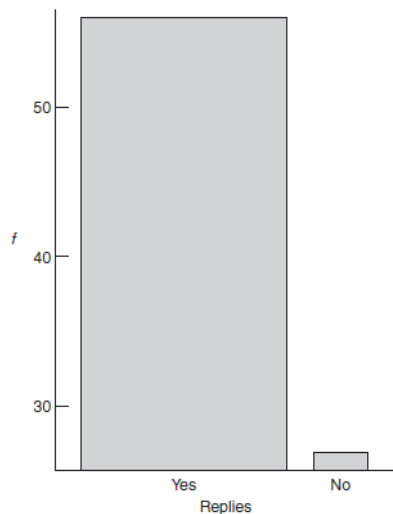


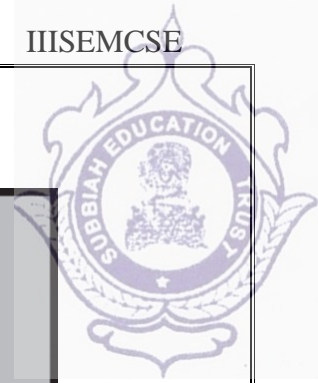
AGRAPH FORQUALITATIVE(NOMINAL)DATA

- As with histograms, equal segments along the horizontal axis are allocated to the different words or classes that appear in the frequency distribution for qualitative data. Likewise, equal segments along the vertical axis reflect increases in frequency. The body of the bar graph consists of a series of bars whose heights reflect the frequencies for the various words or classes.
- A person’s answer to the question “Do you have a Facebook profile?” is either Yes or No, not some impossible intermediate value, such as 40 percent Yes and 60 percent No.
- Gaps are placed between adjacent bars of a bar graph to emphasize the discontinuous nature of qualitative data.

MISLEADINGGRAPHS

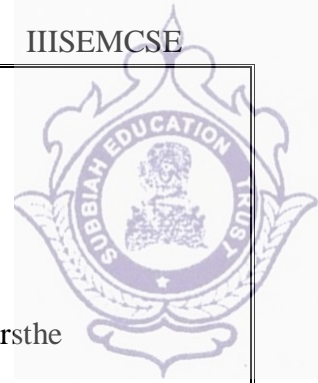
Graphs can be constructed in an unscrupulous manner to support a particular point of view. Popular sayings, including “Numbers don’t lie, but statisticians do” and “There are three kinds of lies—lies, damned lies, and statistics.”





CONSTRUCTING GRAPHS

1. **Decide on the appropriate type of graph**, recalling that histograms and frequency polygons are appropriate for quantitative data, while bar graphs are appropriate for qualitative data and also are sometimes used with discrete quantitative data.
2. **Draw the horizontal axis, then the vertical axis**, remembering that the vertical axis should be about as tall as the horizontal axis is wide.
3. **Identify the string of class intervals that eventually will be superimposed on the horizontal axis**. For qualitative data or ungrouped quantitative data, this is easy—just use the classes suggested by the data. For grouped quantitative data, proceed as if you were creating a set of class intervals for a frequency distribution. (See the box “Constructing Frequency Distributions” on page 27.)
4. **Superimpose the string of class intervals (with gaps for bar graphs) along the entire length of the horizontal axis**. For histograms and frequency polygons, be prepared for some trial and error—use a pencil! Do not use a string of empty class intervals to bridge a sizable gap between the origin of 0 and the smallest class interval. Instead, use wiggly lines to signal a break in scale, then begin with the smallest class interval. Also, do not clutter the horizontal scale with excessive numbers—use just a few convenient numbers.
5. **Along the entire length of the vertical axis, superimpose a progression of convenient numbers**, beginning at the bottom with 0 and ending at the top with a number as large as or slightly larger than the maximum observed frequency. If there is a considerable gap between the origin of 0 and the smallest observed frequency, use wiggly lines to signal a break in scale.
6. Using the scaled axes, **construct bars (or dots and lines) to reflect the frequency of observations within each class interval**. For frequency polygons, dots should be located above the midpoints of class intervals, and both tails of the graph should be anchored to the horizontal axis, as described under “Frequency Polygons” in Section 2.8.
7. **Supply labels for both axes and a title (or even an explanatory sentence) for the graph**.



Describing Data with Averages

MODE

The mode reflects the value of the most frequently occurring score. In other words

A mode is defined as the value that has a higher frequency in a given set of values. It is the value that appears the most number of times.

Example:

In the given set of data: 2, 4, 5, 5, 6, 7, the mode of the dataset is 5 since it has appeared in the set twice.

Types of Modes

Bimodal, Trimodal & Multimodal (More than one mode)

- When there are two modes in a dataset, then the set is called **bimodal**

For example, The mode of Set A = {2, 2, 2, 3, 4, 4, 5, 5, 5} is 2 and 5, because both 2 and 5 is repeated three times in the given set.

- When there are three modes in a dataset, then the set is called **trimodal**

For example, the mode of set A = {2, 2, 2, 3, 4, 4, 5, 5, 5, 7, 8, 8, 8} is 2, 5 and 8

- When there are four or more modes in a dataset, then the set is called **multimodal**

Example: The following table represents the number of wicket taken by a bowler in 10 matches. Find the mode of the given set of data.

Match No.	1	2	3	4	5	6	7	8	9	10
No. of Wickets	2	1	1	3	2	3	2	2	4	1

It can be seen that 2 wickets were taken by the bowler frequently in different matches. Hence, the mode of the given data is 2.

MEDIAN

The median reflects the middle value when observations are ordered from least to most.

The median splits a set of ordered observations into two equal parts, the upper and lower halves.

Finding the Median

- Orders scores from least to most.
- If the total number of observations given is odd, then the formula to calculate the median

$$\text{is: Median} = \{(n+1)/2\}^{\text{th}} \text{ term / observation}$$

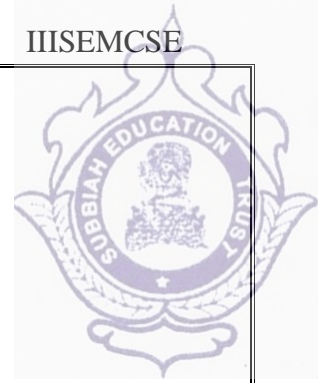
- If the total number of observations is even, then the

$$\text{median formula is: Median} = 1/2[(n/2)^{\text{th}} \text{ term} + \{(n/2)+1\}^{\text{th}} \text{ term}]$$

Example 1:

Find the median of the following:

4, 17, 77, 25, 22, 23, 92, 82, 40, 24, 14, 12, 67, 23, 29



Solution:

$n=15$

When we put those numbers in the order we have:

4, 12, 14, 17, 22, 23, 23, 24, 25, 29, 40, 67, 77, 82, 92,

$$\begin{aligned} \text{Median} &= \left\{ \frac{(n+1)}{2} \right\}^{\text{th}} \text{term} \\ &= \frac{(15+1)}{2} \\ &= 8 \end{aligned}$$

The 8th term in the list is 24

The median value of this set of numbers is 24.

Example 2:

Find the median of the following:

9, 7, 2, 11, 18, 12, 6, 4

Solution

$n=8$

When we put those numbers in the order we have:

2, 4, 6, 7, 9, 11, 12, 18

$$\text{Median} = \frac{1}{2} \left[\left(\frac{n}{2} \right)^{\text{th}} \text{term} + \left\{ \left(\frac{n}{2} \right) + 1 \right\}^{\text{th}} \text{term} \right]$$

$$= \frac{1}{2} \left[\left(\frac{8}{2} \right)^{\text{th}} \text{term} + \left\{ \left(\frac{8}{2} \right) + 1 \right\}^{\text{th}} \text{term} \right]$$

$$= \frac{1}{2} \left[4^{\text{th}} \text{term} + 5^{\text{th}} \text{term} \right]$$

(in our list 4th term is 7 and 5th term is 9)

$$= \frac{1}{2} [7 + 9]$$

$$= \frac{1}{2} (16)$$

$$= 8$$

The median value of this set of numbers is 8.

MEAN

The mean is found by adding all scores and then dividing by the number of scores.

Mean is the average of the given numbers and is calculated by dividing the sum of given numbers by the total number of numbers.

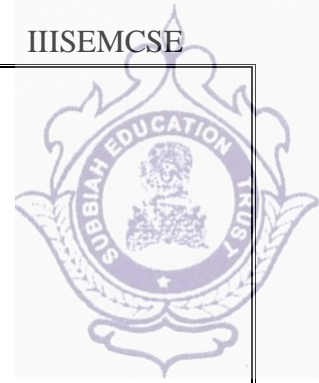
$$\text{Mean} = \frac{\text{sum of all scores}}{\text{number of scores}}$$

Types of means

- Sample mean
- Population mean

Sample Mean

The sample mean is a central tendency measure. The arithmetic average is computed using samples or random values taken from the population. It is evaluated as the sum of all the sample variables divided by the total number of variables.



SAMPLE MEAN

$$\bar{X} = \frac{\sum X}{n}$$

Population Mean

The population mean can be calculated by the sum of all values in the given data/population divided by a total number of values in the given data/population.

POPULATION MEAN

$$\mu = \frac{\sum X}{N}$$

AVERAGES FOR QUALITATIVE AND RANKED DATA

Mode

The mode always can be used with qualitative data.

Median

The median can be used whenever it is possible to order qualitative data from least to most because the level of measurement is ordinal.

Describing Variability

RANGE

The range is the difference between the largest and smallest scores.

The range in statistics for a given data set is the difference between the highest and lowest values. For example, if the given data set is {2,5,8,10,3}, then the range will be 10 - 2 = 8.

Example 1: Find the range of

given observations: 32, 41, 28, 54, 35, 26, 23, 33, 38, 40. Solution: Let us

first arrange the given values in ascending order.

23, 26, 28, 32, 33, 35, 38, 40, 41, 54

Since 23 is the lowest value and 54 is the highest value, therefore, the range of the observations will be; Range

$$(X) = \text{Max}(X) - \text{Min}(X)$$

$$= 54 - 23$$

$$= 31$$

VARIANCE

Variance is a measure of how data points differ from the mean. A variance is a measure of how far a set of data (numbers) are spread out from their mean (average) value.

Formula

$$\sigma = \frac{\sum (x - \mu)^2}{n}$$

$$\text{Variance} = (\text{Standard deviation})^2 = \sigma^2 \Rightarrow \sigma^2 = \frac{\sum (x - \mu)^2}{n}$$

the values of all scores must be added and then divided by the total

number of scores. Example

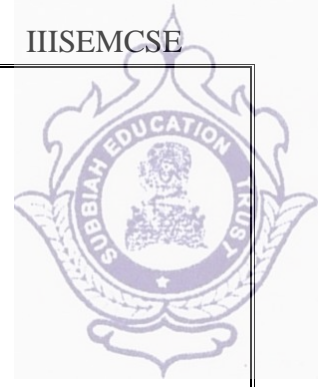
X = 5, 8, 6, 10, 12, 9, 11, 10, 12, 7

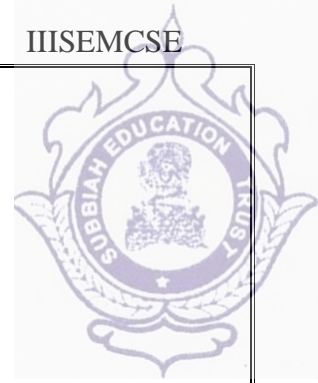
Solution

$$\text{Mean} = \frac{\sum(x)}{n}$$

$$= 10$$

$$\sum(x) = 5 + 8 + 6 + 10 + 12 + 9 + 11 + 10 + 12 + 7$$





$$=90$$

$$\text{Mean} \Rightarrow \mu = 90/10 = 9$$

Deviation from mean

$$x - \mu = -4, -1, -3, 1, 3, 0, 2, 1, 3, -2$$

$$(x - \mu)^2 = 16, 1, 9, 1, 9, 0, 4, 1, 9, 4$$

$$\Sigma(x - \mu)^2 = 16 + 1 + 9 + 1 + 9 + 0 + 4 + 1 + 9 + 4 = 54$$

$$\sigma^2 = \Sigma(x - \mu)^2 / n$$

$$= 54 / 10$$

$$= 5.4$$

STANDARD DEVIATION

The standard deviation, the square root of the mean of all squared deviations from the mean, that is,
Standard deviation = $\sqrt{\text{variance}}$

Standard Deviation: A rough measure of the average (or standard) amount by which scores deviate

Standard Deviation: A Measure of Distance

The mean is a measure of position, but the standard deviation is a measure of distance (on either side of the mean of the distribution).

Sum of Squares (SS)

Calculating the standard deviation requires that we obtain first a value for the variance. However, calculating the variance requires, in turn, that we obtain the sum of the squared deviation scores.

The sum of squared deviation scores or more simply the sum of squares, symbolized by SS

SUM OF SQUARES (SS) FOR POPULATION (DEFINITION FORMULA)

$$SS = \Sigma(X - \mu)^2 \quad (4.1)$$

“The sum of squares equal the sum of all squared deviation scores.” You can reconstruct this formula by remembering the following three steps:

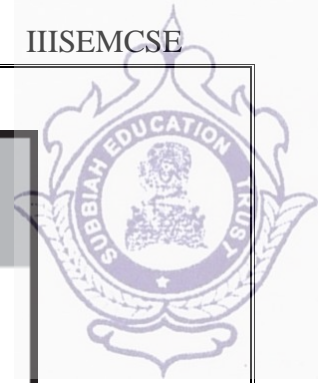
1. Subtract the population mean, μ , from each original score, X , to obtain a deviation score, $X - \mu$.
2. Square each deviation score, $(X - \mu)^2$, to eliminate negative signs.
3. Sum all squared deviation scores, $\Sigma(X - \mu)^2$.

VARIANCE FOR POPULATION

$$\sigma^2 = \frac{SS}{N} \quad (4.5)$$

STANDARD DEVIATION FOR POPULATION

$$\sigma = \sqrt{\sigma^2} = \sqrt{\frac{SS}{N}} \quad (4.6)$$



**Table 4.1
CALCULATION OF POPULATION STANDARD DEVIATION σ
(DEFINITION FORMULA)**

A. COMPUTATION SEQUENCE

- Assign a value to N **1** representing the number of X scores
- Sum all X scores **2**
- Obtain the mean of these scores **3**
- Subtract the mean from each X score to obtain a deviation score **4**
- Square each deviation score **5**
- Sum all squared deviation scores to obtain the sum of squares **6**
- Substitute numbers into the formula to obtain population variance, σ^2 **7**
- Take the square root of σ^2 to obtain the population standard deviation, σ **8**

B. DATA AND COMPUTATIONS

X	4 $X - \mu$	5 $(X - \mu)^2$
13	3	9
10	0	0
11	1	1
7	-3	9
9	-1	1
11	1	1
9	-1	1

1 $N = 7$ **2** $\Sigma X = 70$ **6** $SS = \Sigma (X - \mu)^2 = 22$

3 $\mu = \frac{70}{7} = 10$

7 $\sigma^2 = \frac{SS}{N} = \frac{22}{7} = 3.14$ **8** $\sigma = \sqrt{\frac{SS}{N}} = \sqrt{\frac{22}{7}} = \sqrt{3.14} = 1.77$

Sum of Squares Formulas for Sample

Sample notation can be substituted for population notation in the above two formulas without causing any essential changes:

SUM OF SQUARES (SS) FOR SAMPLE (DEFINITION FORMULA)

$$SS = \Sigma (X - \bar{X})^2 \tag{4.3}$$

VARIANCE FOR SAMPLE

$$s^2 = \frac{SS}{n-1} \tag{4.7}$$

STANDARD DEVIATION FOR SAMPLE

$$s = \sqrt{s^2} = \sqrt{\frac{SS}{n-1}} \tag{4.8}$$

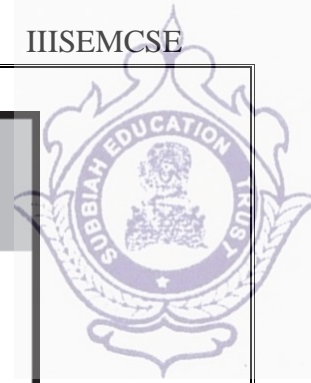


Table 4.3
CALCULATION OF SAMPLE STANDARD DEVIATION (S)
(DEFINITION FORMULA)

A. COMPUTATION SEQUENCE

- Assign a value to n **1** representing the number of X scores
- Sum all X scores **2**
- Obtain the mean of these scores **3**
- Subtract the mean from each X score to obtain a deviation score **4**
- Square each deviation score **5**
- Sum all squared deviation scores to obtain the sum of squares **6**
- Substitute numbers into the formula to obtain the sample variance, s^2 **7**
- Take the square root of s^2 to obtain the sample standard deviation, s **8**

B. DATA AND COMPUTATIONS

X	4 $X - \bar{X}$	5 $(X - \bar{X})^2$
7	4	16
3	0	0
1	-2	4
0	-3	9
4	1	1

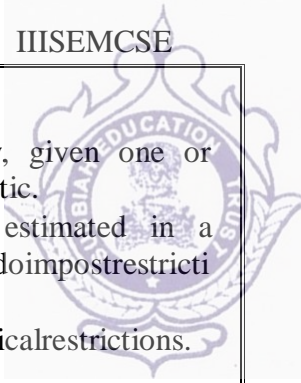
1 $n = 5$ **2** $\Sigma X = 15$ **6** $SS = \Sigma(X - \bar{X})^2 = 30$

3 $\bar{X} = \frac{15}{5} = 3$

7 $s^2 = \frac{SS}{n-1} = \frac{30}{4} = 7.50$ **8** $s = \sqrt{\frac{SS}{n-1}} = \sqrt{\frac{30}{4}} = \sqrt{7.50} = 2.74$

Table 4.5
TWO ESTIMATES OF POPULATION VARIABILITY

WHEN μ IS UNKNOWN ($\bar{X} = 3$)			WHEN μ IS KNOWN ($\mu = 2$)		
X	$X - \bar{X}$	$(X - \bar{X})^2$	X	$X - \mu$	$(X - \mu)^2$
7	$7 - 3 = 4$	16	7	$7 - 2 = 5$	25
3	$3 - 3 = 0$	0	3	$3 - 2 = 1$	1
1	$1 - 3 = -2$	4	1	$1 - 2 = -1$	1
0	$0 - 3 = -3$	9	0	$0 - 2 = -2$	4
4	$4 - 3 = 1$	1	4	$4 - 2 = 2$	4
$\Sigma(X - \bar{X}) = 0$ $\Sigma(X - \bar{X})^2 = 30$			$\Sigma(X - \mu) = 5$ $\Sigma(X - \mu)^2 = 35$		
$df = n - 1 = 5 - 1 = 4$			$df = n = 5$		
$s^2(df = n - 1) = \frac{\Sigma(X - \bar{X})^2}{n - 1} = \frac{30}{4} = 7.50$			$s^2(df = n) = \frac{\Sigma(X - \mu)^2}{n} = \frac{35}{5} = 7.00$		



DEGREES OF FREEDOM (df)

- Degrees of freedom (df) refers to the number of values that are free to vary, given one or more mathematical restrictions, in a sample being used to estimate a population characteristic.
- Degrees of freedom are the number of independent variables that can be estimated in a statistical analysis. These values of these variables are without constraint, although the values do impose restrictions on other variables if the data set is to comply with estimate parameters.
- Degrees of Freedom (df) The number of values free to vary, given one or more mathematical restrictions.

Formula

Degree of freedom **df = n - 1**

Example

Consider a data set consists of five positive integers. The sum of the five integers must be the multiple of 6. The values are randomly selected as 3, 8, 5, and 4.

The sum of this for values is 20. So we have to choose the fifth integer to make the sum divisible by 6. Therefore the fifth element is 10.

The number of degrees of Degrees of Freedom (df) The number of values free to vary, given one or more mathematical restrictions. Freedom—in the numerator, as in the formulas for s^2 and s . In fact, we can use degrees of freedom to rewrite the formulas for the sample variance and standard deviation:

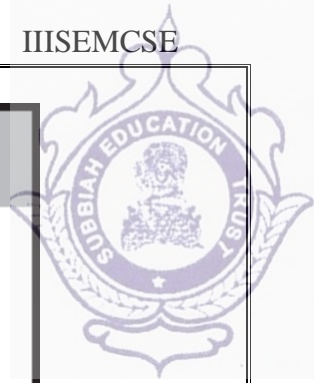
VARIANCE FOR SAMPLE	
$s^2 = \frac{SS}{n-1} = \frac{SS}{df}$	(4.9)

STANDARD DEVIATION FOR SAMPLE	
$s = \sqrt{\frac{SS}{n-1}} = \sqrt{\frac{SS}{df}}$	(4.10)

INTERQUARTILE RANGE (IQR)

The interquartile range (IQR), is simply the range for the middle 50 percent of the scores. More specifically, the IQR equals the distance between the third quartile (or 75th percentile) and the first quartile (or 25th percentile), that is, after the highest quarter (or top 25 percent) and the lowest quarter (or bottom 25 percent) have been trimmed from the original set of scores. Since most distributions are spread more widely in their extremities than their middle, the IQR tends to be less than half the size of the range.

Simply, The IQR describes the middle 50% of values when ordered from lowest to highest. To find the interquartile range (IQR), first find the median (middle value) of the lower and upper half of the data. These values are quartile 1 (Q1) and quartile 3 (Q3). The IQR is the difference between Q3 and Q1.



**Table 4.6
CALCULATION OF THE IQR**

A. INSTRUCTIONS

- 1 Order scores from least to most.
- 2 To determine how far to penetrate the set of ordered scores, begin at either end, then add 1 to the total number of scores and divide by 4. If necessary, round the result to the nearest whole number.
- 3 Beginning with the largest score, count the requisite number of steps (calculated in step 2) into the ordered scores to find the location of the third quartile.
- 4 The third quartile equals the value of the score at this location.
- 5 Beginning with the smallest score, again count the requisite number of steps into the ordered scores to find the location of the first quartile.
- 6 The first quartile equals the value of the score at this location.
- 7 The IQR equals the third quartile minus the first quartile.

B. EXAMPLE

- 1 7, 9, 9, 10, 11, 11, 13
 - 2 $(7 + 1)/4 = 2$
 - 3 7, 9, 9, 10, 11, 11, 13
- \uparrow
 2 1
 \curvearrowright
- 4 third quartile = 11
 - 5 7, 9, 9, 10, 11, 11, 13
- \uparrow
 1 2
 \curvearrowleft
- 6 first quartile = 9
 - 7 IQR = 11 - 9 = 2

Normal Distributions and Standard (z) Scores

THE NORMAL CURVE

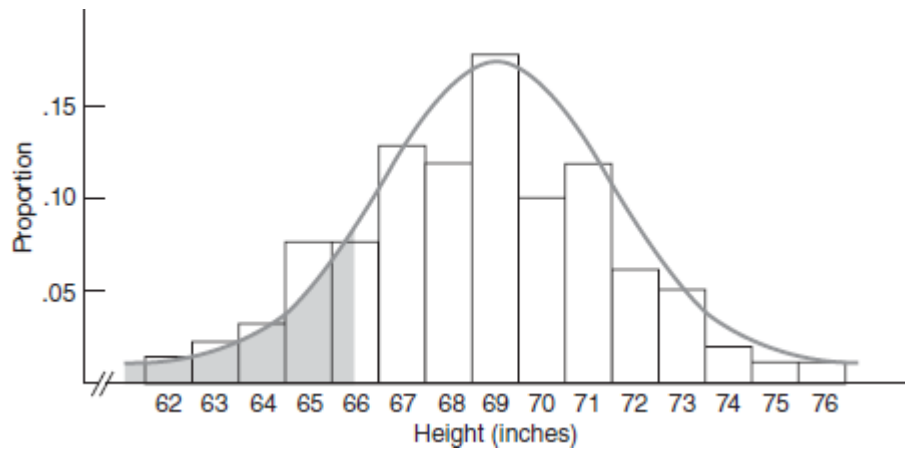
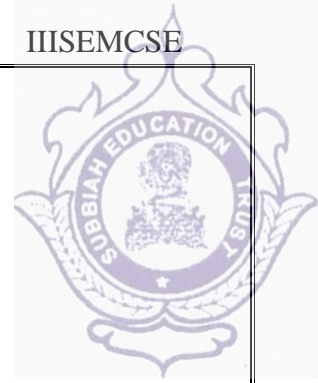
The normal distribution is a continuous probability distribution that is symmetrical on both sides of the mean, so the right side of the center is a mirror image of the left side.

Properties of the Normal Curve

- The normal curve is a theoretical curve defined for a continuous variable, as described in Section 1.6, and noted for its symmetrical bell-shaped form, as revealed in below figure
- Because the normal curve is symmetrical, its lower half is the mirror image of its upper half.
- The normal curve peaks above a point midway along the horizontal spread and then tapers off gradually in either direction from the peak (without actually touching the horizontal axis, since, in theory, the tails of a normal curve extend infinitely far).
- The values of the mean, median (or 50th percentile), and mode, located at a point midway along the horizontal spread, are the same for the normal curve.

Properties of a normal distribution

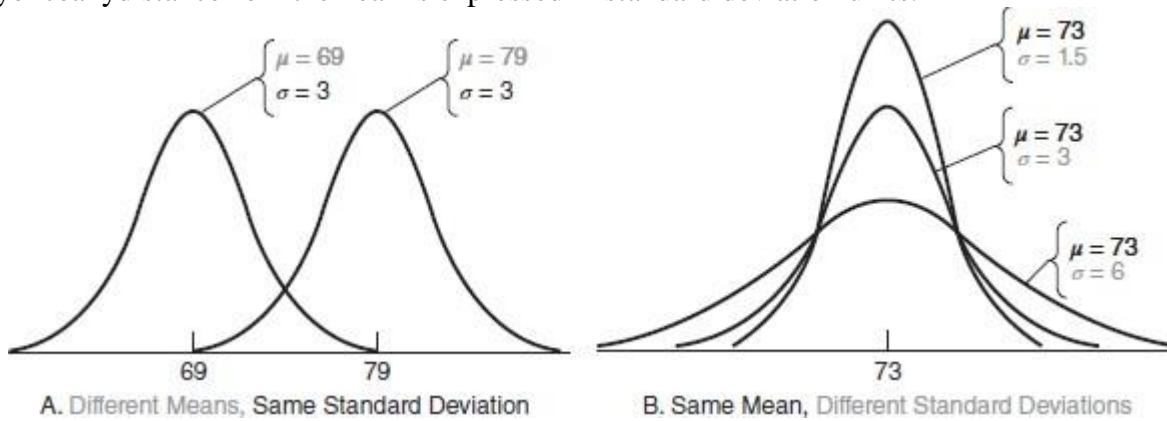
- The mean, mode and median are all equal.
- The curve is symmetric at the center (i.e. around the mean, μ).
- Exactly half of the values are to the left of center and exactly half the values are to the right.
- The total area under the curve is 1.



Different Normal Curves

As a theoretical exercise, it is instructive to note the various types of normal curves that are produced by an arbitrary change in the value of either the mean (μ) or the standard deviation (σ).

Obvious differences in appearance among normal curves are less important than you might suspect. Because of their common mathematical origin, every normal curve can be interpreted in exactly the same way once any distance from the mean is expressed in standard deviation units.



z SCORES

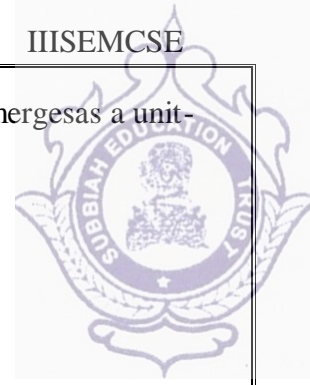
A z score is a unit-free, standardized score that, regardless of the original units of measurement, indicates how many standard deviations a score is above or below the mean of its distribution.

A z score can be defined as a measure of the number of standard deviations by which a score is below or above the mean of a distribution. In other words, it is used to determine the distance of a score from the mean. If the z score is positive it indicates that the score is above the mean. If it is negative then the score will be below the mean. However, if the z score is 0 it denotes that the data point is the same as the mean.

To obtain a z score, express any original score, whether measured in inches, milliseconds, dollars, IQ points, etc., as a deviation from its mean (by subtracting its mean) and then split this deviation into standard deviation units (by dividing by its standard deviation),

$$z = \frac{X - \mu}{\sigma}$$

Where X is the original score and μ and σ are the mean and the standard deviation, respectively, for the normal distribution of the original scores. Since identical units of measurement appear in both the numerator



and denominator of the ratio for z , the original units of measurement cancel each other and the z score emerges as a unit-free or standardized number, often referred to as a standard score.

A z score consists of two parts:

1. A positive or negative sign indicating whether it's above or below the mean; and
2. A number indicating the size of its deviation from the mean in standard deviation units.

Converting to z

Scores Example

Suppose on a GRE test a score of 1100 is obtained. The mean score for the GRE test is 1026 and the population standard deviation is 209. In order to find how well a person scored with respect to the score of an average test taker, the z score will have to be determined.

The steps to calculate the z score are as follows:

- Step 1: Write the value of the raw score in the z score equation. $z = (1100 - \mu) / \sigma$
- Step 2: Write the mean and standard deviation of the population in the z score formula. $z = (1100 - 1026) / 209$
- Step 3: Perform the calculation to get the required z score. $z = 0.345$
- Step 4: A z score table can be used to find the percentage of test-takers that are below the score of the person. Using the first two digits of the z score, determine the row containing these digits of the z table. Now using the 2nd digit after the decimal, find the corresponding column. The intersection of this row and column will give a value. As shown below, this value will be 0.6368 for the given example.
- Step 5: Use the value from step 4 and multiply it by 100 to get the required percentage. $0.6368 * 100 = 63.68\%$. This shows that 63.68% of test-takers scores are lesser than the given raw score.

STANDARD NORMAL CURVE

If the original distribution approximates a normal curve, then the shift to standard or z scores will always produce a new distribution that approximates the standard normal curve. This is the one normal curve for which a table is actually available.

Although there is an infinite number of different normal curves, each with its own mean and standard deviation, there is only one standard normal curve, with a mean of 0 and a standard deviation of 1.

For a standard normal curve

Mean = 0

$$\text{Mean of } z = \frac{X - \mu}{\sigma} = \frac{\mu - \mu}{\sigma} = \frac{0}{\sigma} = 0$$

Standard deviation = 1

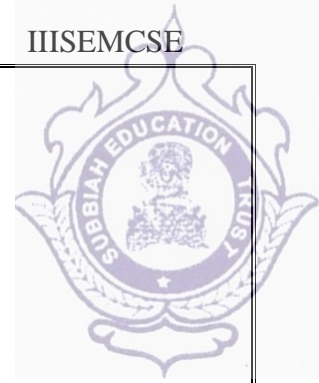
$$\text{Standard deviation of } z = \frac{X - \mu}{\sigma} = \frac{\mu + 1\sigma - \mu}{\sigma} = \frac{1\sigma}{\sigma} = 1$$

Standard Normal Table

The standard normal table consists of columns of z scores coordinated with columns of proportions

Using the Top Legend of the Table

Notice that columns are arranged in sets of three, designated as A, B, and C in the legend at the top of the table. When using the top legend, all entries refer to the upper half of the standard normal curve. The entries in column A are z scores, beginning with 0.00 and ending with 4.00



FINDING PROPORTIONS

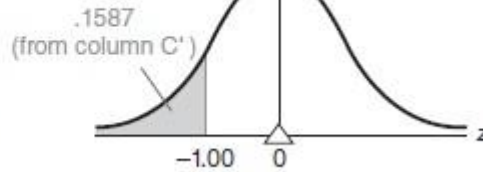
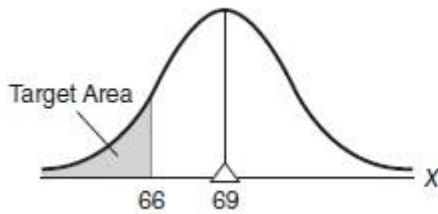
Finding Proportions for One Score

- Sketch a normal curve and shade in the target area,
- Plan your solution according to the normal table.
- Convert X to z .

$$z = \frac{X - \mu}{\sigma}$$

Find: Proportion Below 66

Solution:



Answer: .1587

- Find the target area.

Finding Proportions between Two Scores

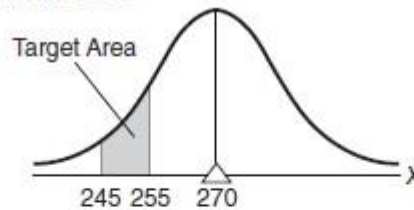
- Sketch a normal curve and shade in the target area, (example, find proportion between 245 to 255)
- Plan your solution according to the normal table.
- Convert X to z by expressing 255 as

$$z = \frac{255 - 270}{15} = \frac{-15}{15} = -1.00$$

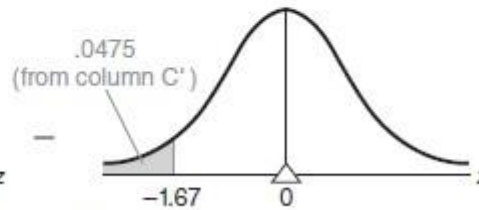
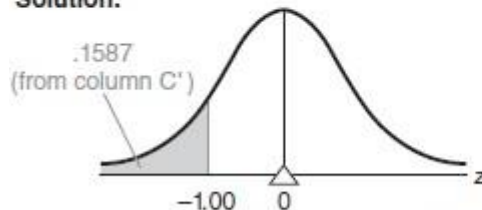
and by expressing 245 as

$$z = \frac{245 - 270}{15} = \frac{-25}{15} = -1.67$$

Find: Proportion Between 245 and 255



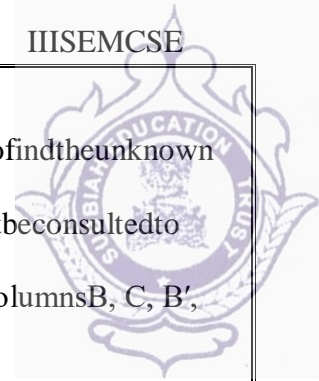
Solution:



Answer: .1587
- .0475

.1112

- Find the target area.



FINDINGScores

Sofar,wehaveconcentratedonnormalcurveproblemsforwhichTableAmustbeconsultedtofindtheunknown proportion(ofarea)associated with some known scoreorpair ofknown scores

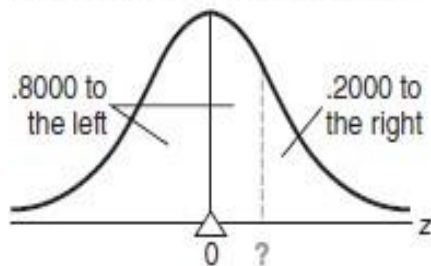
NowwewillconcentrateontheoppositetypeofnormalcurveproblemforwhichTableAmustbeconsultedto find theunknown scoreor scores associatedwith some known proportion.

Forthistypeofproblemrequires thatwereverseouruseofTableAbyenteringproportionsincolumnsB, C, B', or C'and findingzscoreslistedincolumns Aor A'.

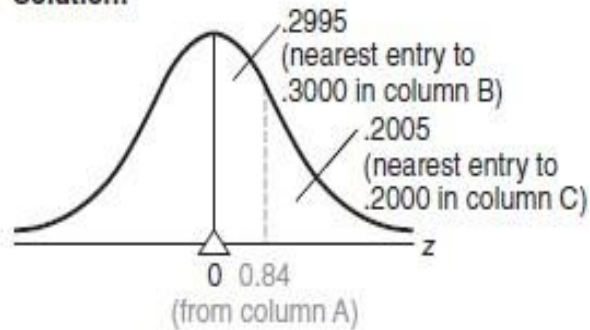
FindingOneScore

- Sketchanormalcurveand,onthecorrectsideofthemean,drawalinerrepresentingthetargetscore,as in figure

Find: Lowest Score in Upper 20%



Solution:



$$\begin{aligned} \text{Answer: } X &= \mu + (z)(\sigma) \\ &= 230 + (0.84)(50) \\ &= 230 + 42 \\ &= 272 \end{aligned}$$

It's often helpful to visualize the target score as splitting the total area into two sectors—one to the left of(below)the target scoreand oneto theright of (above) thetarget score

- Plan yoursolution accordingtothenormaltable.

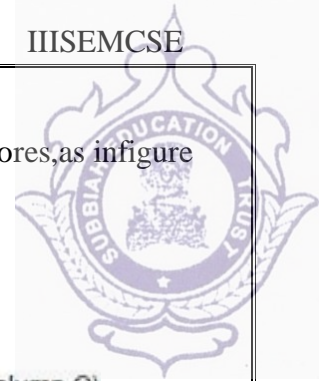
In problems of this type, you must plan how to find the z score for the target score. Because the target score ison the right side of the mean, concentrate on the area in the upper half of the normal curve, as described incolumnsBand C.

- Findz.
- Convertztothetargetscore.

When converting z scores to original scores, you will probably find it more efficient to use the followingequation

CONVERTING z SCORE TO ORIGINAL SCORE

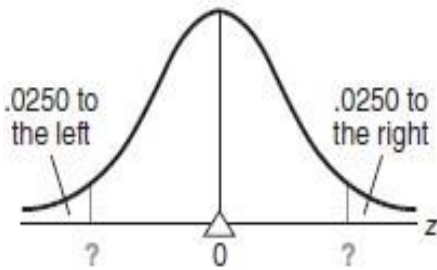
$$X = \mu + (z)(\sigma)$$



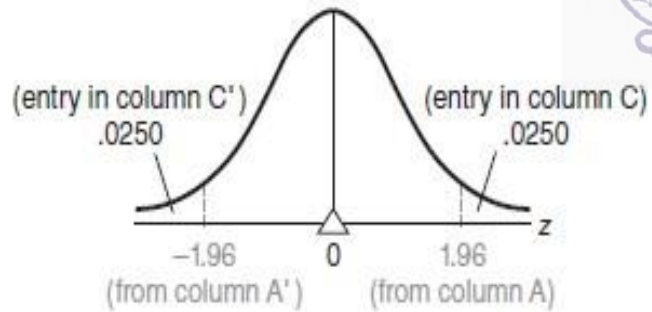
Finding Two Scores

- Sketch a normal curve. On either side of the mean, draw two lines representing the two target scores, as in figure

Find: Pairs of Scores for the Extreme 2.5%



Solution:



$$\begin{aligned} \text{Answer: } X_{\min} &= \mu + (z)(\sigma) \\ &= 22 + (-1.96)(4) \\ &= 22 - 7.84 \\ &= 14.16 \end{aligned}$$

$$\begin{aligned} \text{Answer: } X_{\max} &= \mu + (z)(\sigma) \\ &= 22 + (1.96)(4) \\ &= 22 + 7.84 \\ &= 29.84 \end{aligned}$$

- Plan your solution according to the normal table.
- Find z .
- Convert z to the target score.

Points to Remember

- range = largest value – smallest value in a list
- class interval = range / desired no of classes
- relative frequency = frequency (f) / ϵ (f)
- Cumulative frequency - add to the frequency of each class the sum of the frequencies of all classes ranked below it.
- Cumulative percentage = (f/cumulative f) * 100
- Histograms
- Construction of frequency polygon
- Stem and leaf display
- Mode - The value of the most frequent score.
- For odd no of terms **Median** = $\{(n+1)/2\}^{\text{th}}$ term/observation. For even no of terms **Median** = $1/2[(n/2)^{\text{th}}$ term + $\{(n/2)+1\}^{\text{th}}$ term]
- Mean = sum of all scores / number of scores

SAMPLE MEAN

$$\bar{X} = \frac{\sum X}{n}$$

Variance

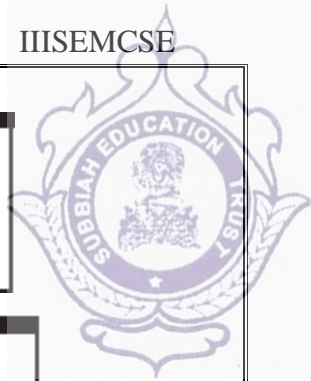
$$\text{Variance} = (\text{Standard deviation})^2 = \sigma^2 \Rightarrow \sigma^2 = \frac{\sum (x - \mu)^2}{n}$$

POPULATION MEAN

$$\mu = \frac{\sum X}{N}$$

$\sigma = \sqrt{\sum (x - \mu)^2}$ or

- Range (X) = Max (X) – Min (X)



STANDARD DEVIATION FOR POPULATION

$$\sigma = \sqrt{\sigma^2} = \sqrt{\frac{SS}{N}} \tag{4.6}$$

SUM OF SQUARES (SS) FOR POPULATION (DEFINITION FORMULA)

$$SS = \sum(X - \mu)^2 \tag{4.1}$$

VARIANCE FOR SAMPLE

$$s^2 = \frac{SS}{n-1} \tag{4.7}$$

STANDARD DEVIATION FOR SAMPLE

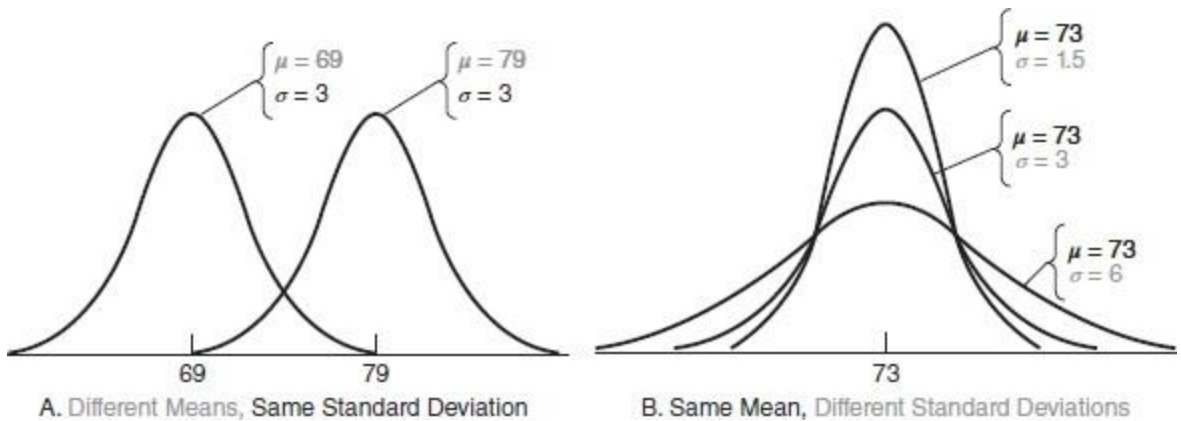
$$s = \sqrt{s^2} = \sqrt{\frac{SS}{n-1}} \tag{4.8}$$

SUM OF SQUARES (SS) FOR SAMPLE (DEFINITION FORMULA)

$$SS = \sum(X - \bar{X})^2 \tag{4.3}$$

13. Degree of freedom **df= n-1**

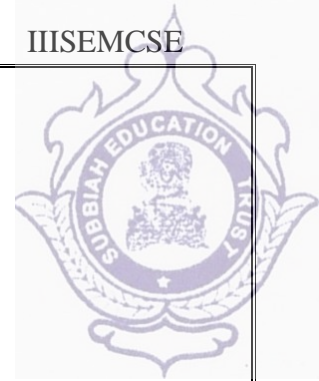
14. Types of normal curve



15. z -score

z SCORE

$$z = \frac{X - \mu}{\sigma} \tag{5.1}$$



16. Standard normal curve; mean=0, standard deviation=1

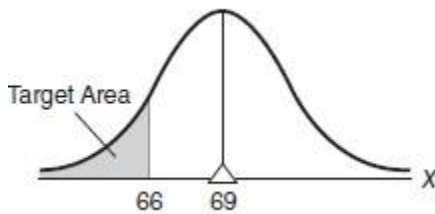
17. Finding proportion

$$z = \frac{X - \mu}{\sigma}$$

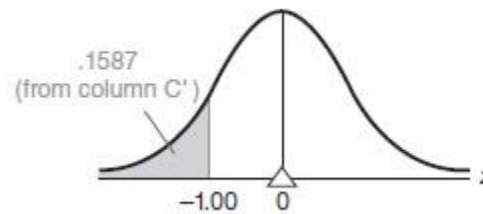
18. Finding proportion

1. For one score

Find: Proportion Below 66



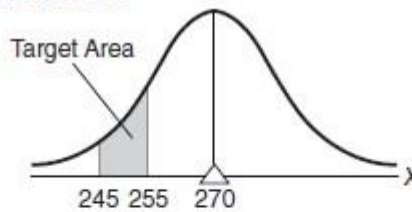
Solution:



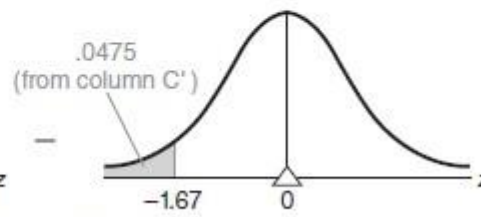
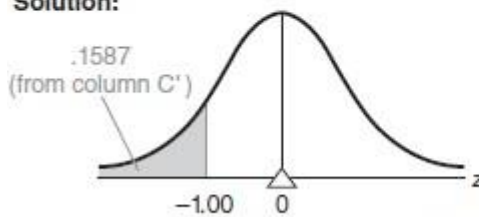
Answer: .1587

2. For between two scores

Find: Proportion Between 245 and 255



Solution:



Answer: $.1587 - .0475 = .1112$

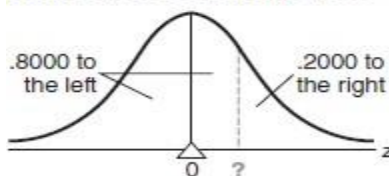
19. Finding scores

CONVERTING z SCORE TO ORIGINAL SCORE

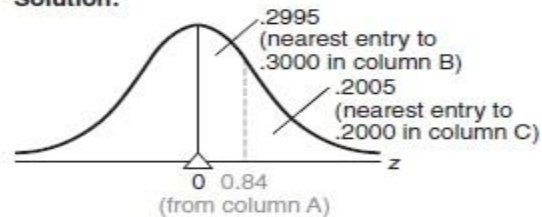
$$X = \mu + (z)(\sigma)$$

20. Finding scores – one score

Find: Lowest Score in Upper 20%

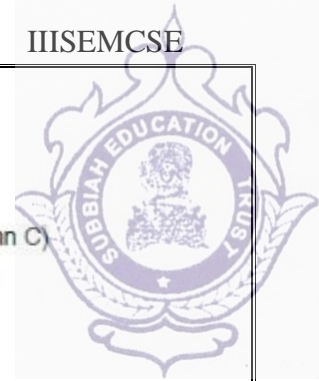


Solution:

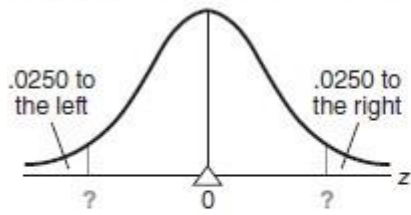


Answer: $X = \mu + (z)(\sigma)$
 $= 230 + (0.84)(50)$
 $= 230 + 42$
 $= 272$

Two scores

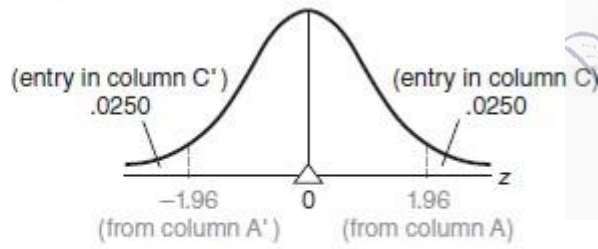


Find: Pairs of Scores for the Extreme 2.5%

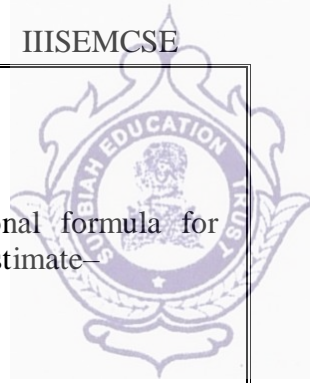


$$\begin{aligned} \text{Answer: } X_{\min} &= \mu + (z)(\sigma) \\ &= 22 + (-1.96)(4) \\ &= 22 - 7.84 \\ &= 14.16 \end{aligned}$$

Solution:



$$\begin{aligned} \text{Answer: } X_{\max} &= \mu + (z)(\sigma) \\ &= 22 + (1.96)(4) \\ &= 22 + 7.84 \\ &= 29.84 \end{aligned}$$



**Unit –
II DESCRIBING RELATIONSHIPS**

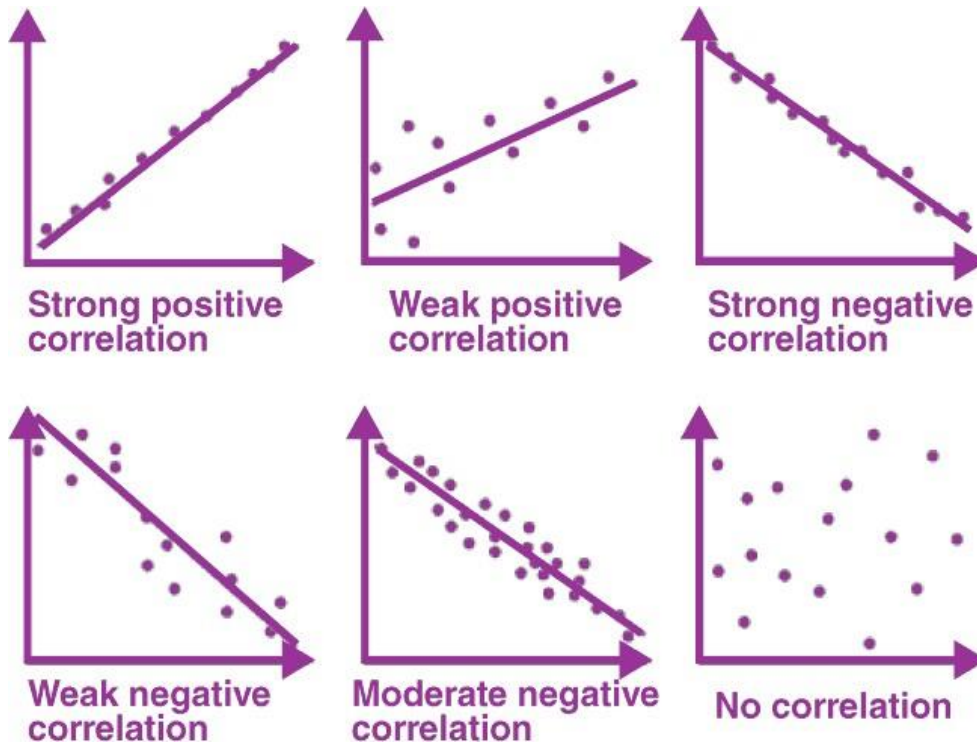
Correlation – Scatter plots – correlation coefficient for quantitative data – computational formula for correlation coefficient – Regression – regression line – least squares regression line – Standard error of estimate – interpretation of r^2 – multiple regression equations – regression toward the mean

Correlation

Correlation refers to a process for establishing the relationships between two variables. You learned a way to get a general idea about whether or not two variables are related, is to plot them on a “scatter plot”. While there are many measures of association for variables which are measured at the ordinal or higher level of measurement, correlation is the most commonly used approach.

Types of Correlation

- **Positive Correlation** – when the values of the two variables move in the same direction so that an increase/decrease in the value of one variable is followed by an increase/decrease in the value of the other variable.
- **Negative Correlation** – when the values of the two variables move in the opposite direction so that an increase/decrease in the value of one variable is followed by decrease/increase in the value of the other variable.
- **No Correlation** – when there is no linear dependence or relation between the two variables.



**Table 6.2
THREE TYPES OF RELATIONSHIPS**

A. POSITIVE RELATIONSHIP		
FRIEND	SENT	RECEIVED
Doris	13	14
Steve	9	18
Mike	7	12
Andrea	5	10
John	1	6

B. NEGATIVE RELATIONSHIP		
FRIEND	SENT	RECEIVED
Doris	13	6
Steve	9	10
Mike	7	14
Andrea	5	12
John	1	18

C. LITTLE OR NO RELATIONSHIP		
FRIEND	SENT	RECEIVED
Doris	13	10
Steve	9	18
Mike	7	12
Andrea	5	6
John	1	14

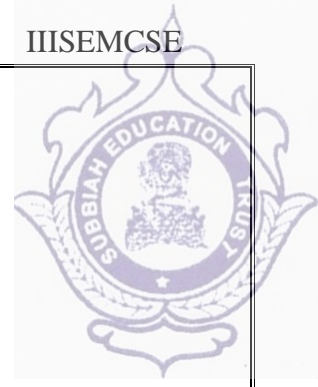
SCATTERPLOTS

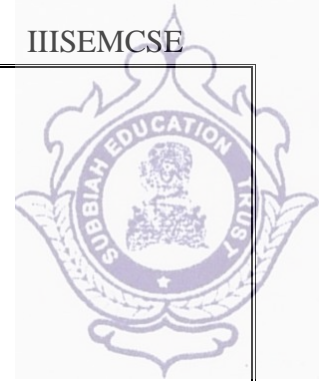
A scatter plot is a graph containing a cluster of dots that represents all pairs of scores. In other words, scatter plots are the graphs that present the relationship between two variables in a data set. It represents data points on a two-dimensional plane or on a Cartesian system.

Construction of scatter plots

- The independent variable or attribute is plotted on the X-axis.
- The dependent variable is plotted on the Y-axis.

Fig 6.1





- Use each pair of scores to locate a dot within the scatterplot

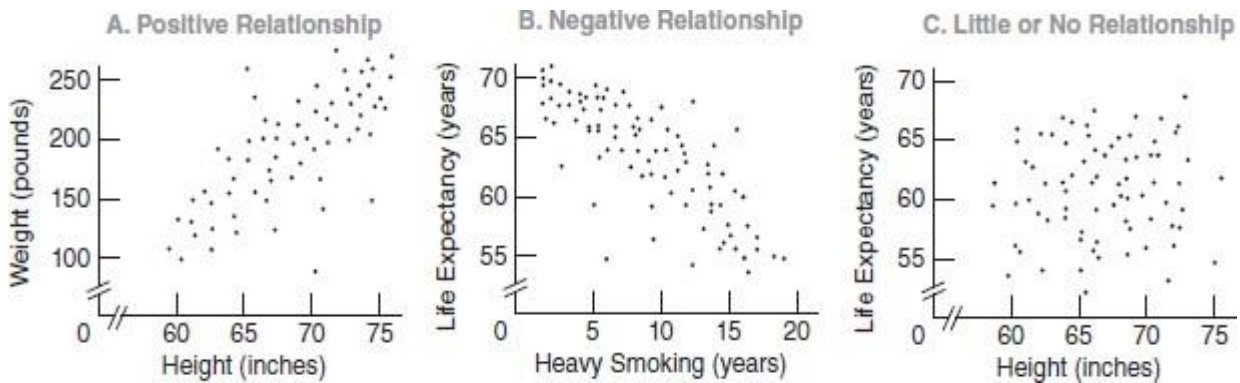
Positive, Negative, or Little or No Relationship?

The first step is to note the tilt or slope, if any, of a dot cluster.

A dot cluster that has a slope from the lower left to the upper right, as in panel A of below figure, reflects a **positive relationship**.

A dot cluster that has a slope from the upper left to the lower right, as in panel B of below figure, reflects a **negative relationship**.

A dot cluster that lacks any apparent slope, as in panel C of below figure, reflects a **little or no relationship**.

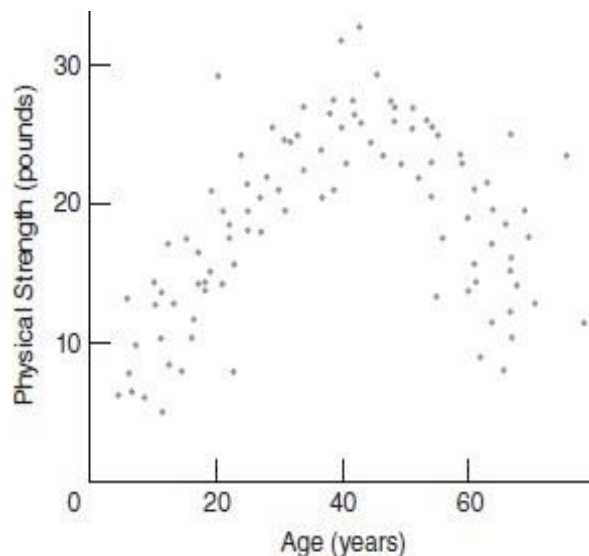


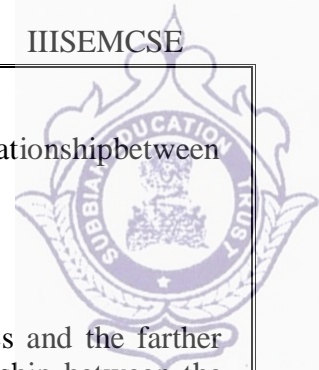
Perfect Relationship

A dot cluster that equals (rather than merely approximates) a straight line reflects a perfect relationship between two variables.

Curvilinear Relationship

The previous discussion assumes that a dot cluster approximates a straight line and, therefore, reflects a **linear relationship**. But this is not always the case. Sometimes a dot cluster approximates a bent or curved line, as in below figure, and therefore reflects a **curvilinear relationship**.





ACORRELATIONCOEFFICIENTFORQUANTITATIVEDATA: r

Thecorrelationcoefficient,r,isasummarymeasurethatdescribestheextentofthestatisticalrelationshipbetween twointerval or ratio level variables.

Propertiesofr

- Thecorrelationcoefficientisscaledsothat itisalwaysbetween -1and+1.
- When r is close to 0 this means that there is little relationship between the variables and the farther awayfrom 0 r is, in either the positive or negative direction, the greater the relationship between the twovariables.
- Thesignof rindicates thetypeoflinearrelationship, whetherpositiveornegative.
- Thenumericalvalueof r, without regardto sign,indicatesthrengthofthelinearrelationship.
- A number with a plus sign (or no sign) indicates a positive relationship, and a number with a minus signindicatesanegativerelationship

COMPUTATIONFORMULAFORr

Calculate avalueforrbyusingthe followingcomputation formula:

CORRELATION COEFFICIENT (COMPUTATION FORMULA)

$$r = \frac{SP_{xy}}{\sqrt{SS_x SS_y}}$$

Wherethetwo sumofsquares termsin thedenominatoraredefinedas

$$SS_x = \sum(X - \bar{X})^2 = \sum X^2 - \frac{(\sum X)^2}{n}$$

$$SS_y = \sum(Y - \bar{Y})^2 = \sum Y^2 - \frac{(\sum Y)^2}{n}$$

Thesumof theproductsterminthe numerator,SP_{xy}, isdefinedin belowformula

$$SP_{xy} = \sum(X - \bar{X})(Y - \bar{Y}) = \sum XY - \frac{(\sum X)(\sum Y)}{n}$$

Orthe formulais writtenas

$$r = \frac{n(\sum xy) - (\sum x)(\sum y)}{\sqrt{[n \sum x^2 - (\sum x)^2][n \sum y^2 - (\sum y)^2]}}$$

Wheren =Number of Information

Σx= Totalofthe

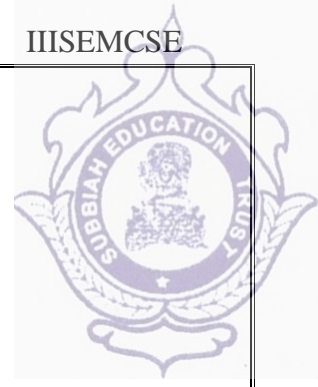
FirstVariableValueΣy=TotaloftheSecon

d VariableValue

Σxy=SumoftheProductoffirst&Second ValueΣx²

=Sum of the Squaresof theFirst Value

Σy² =Sumof theSquares of theSecond Value



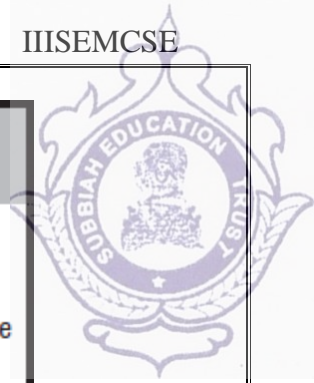


Table 6.3
CALCULATION OF r : COMPUTATION FORMULA

A. COMPUTATIONAL SEQUENCE

- Assign a value to n (1), representing the number of pairs of scores.
- Sum all scores for X (2) and for Y (3).
- Find the product of each pair of X and Y scores (4), one at a time, then add all of these products (5).
- Square each X score (6), one at a time, then add all squared X scores (7).
- Square each Y score (8), one at a time, then add all squared Y scores (9).
- Substitute numbers into formulas (10) and solve for SP_{xy} , SS_x , and SS_y .
- Substitute into formula (11) and solve for r .

B. DATA AND COMPUTATIONS

	CARDS		4	6	8
FRIEND	SENT, X	RECEIVED, Y	XY	X^2	Y^2
Doris	13	14	182	169	196
Steve	9	18	162	81	324
Mike	7	12	84	49	144
Andrea	5	10	50	25	100
John	1	6	6	1	36

1 $n = 5$ 2 $\Sigma X = 35$ 3 $\Sigma Y = 60$ 4 $\Sigma XY = 484$ 5 $\Sigma X^2 = 325$ 6 $\Sigma Y^2 = 800$

10 $SP_{xy} = \Sigma XY - \frac{(\Sigma X)(\Sigma Y)}{n} = 484 - \frac{(35)(60)}{5} = 484 - 420 = 64$

$$SS_x = \Sigma X^2 - \frac{(\Sigma X)^2}{n} = 325 - \frac{(35)^2}{5} = 325 - 245 = 80$$

$$SS_y = \Sigma Y^2 - \frac{(\Sigma Y)^2}{n} = 800 - \frac{(60)^2}{5} = 800 - 720 = 80$$

11 $r = \frac{SP_{xy}}{\sqrt{SS_x SS_y}} = \frac{64}{\sqrt{(80)(80)}} = \frac{64}{80} = .80$

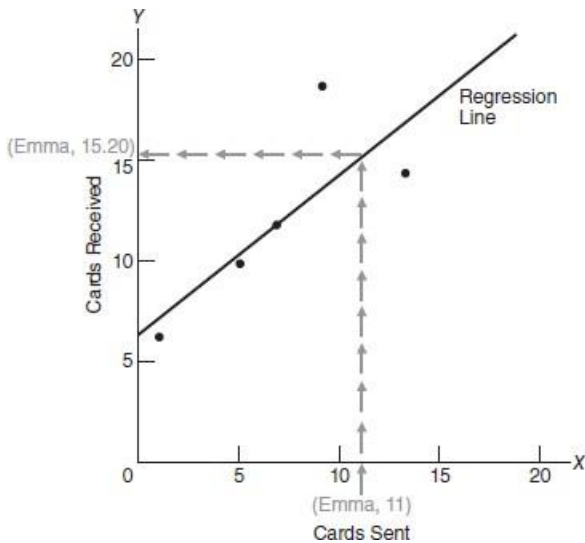
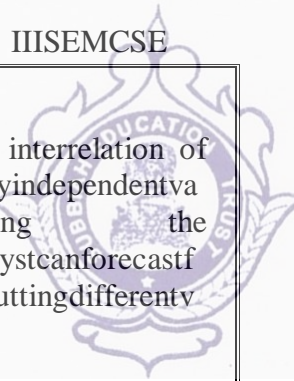
REGRESSION

A regression is a statistical technique that relates a dependent variable to one or more independent(explanatory) variables. A regression model is able to show whether changes observed in the dependent variable are associated with changes in one or more of the explanatory variables.

Regression captures the correlation between variables observed in a data set, and quantifies whether those correlations are statistically significant or not.

A Regression Line

A regression line is a line that best describes the behaviour of a set of data. In other words, it's a line that best fits the trend of a given data.



The purpose of the line is to describe the interrelation of dependent variable (Y variable) with one or many independent variables (X variable). By using the equation obtained from the regression line, an analyst can forecast future behaviour of the dependent variable by inputting different values for the independent ones.

Types of regression

The two basic types of regression are

- Simple linear regression

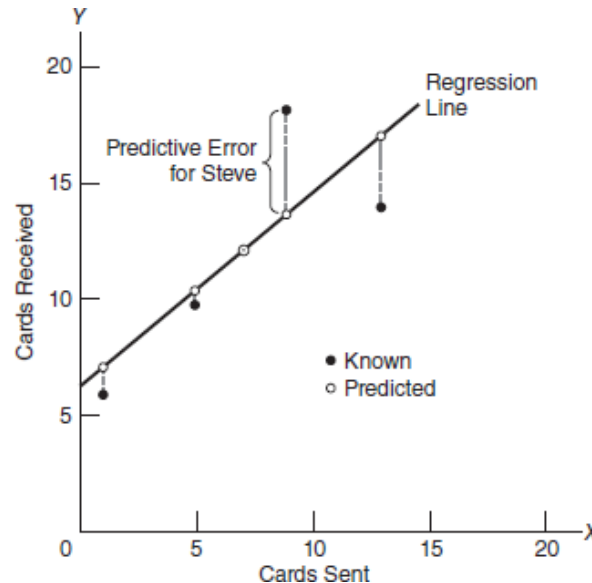
Simple linear regression uses one independent variable to explain or predict the outcome of the dependent variable Y

- Multiple linear regression

Multiple linear regression uses two or more independent variables to predict the outcome

Predictive Errors

Prediction error refers to the difference between the predicted values made by some model and the actual values.



LEAST SQUARES REGRESSION LINE

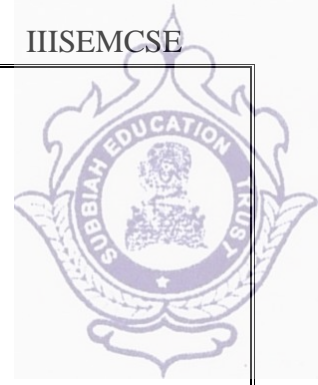
The placement of the regression line minimizes not the total predictive error but the total squared predictive error, that is, the total for all squared predictive errors. When located in this fashion, the regression line is often referred to as the least squares regression line.

The Least Squares Regression Line is the line that minimizes the sum of the residuals squared. The residual is the vertical distance between the observed point and the predicted point, and it is calculated by subtracting \hat{y} from y .

Formula

$y' = bx + a$ b - slope, a - y-intercept

$$b = \frac{N \sum(xy) - \sum x \sum y}{N \sum(x^2) - (\sum x)^2}$$



$$b = \frac{\sum y - m \sum x}{N}$$

Example

"x"	"y"
2	4
3	5
5	7
7	10
9	15

Step1: For each (x,y) calculate x^2 and xy :

x	y	x^2	xy
2	4	4	8
3	5	9	15
5	7	25	35
7	10	49	70
9	15	81	135

Step2: Sum x , y , x^2 and xy (gives us $\sum x$, $\sum y$, $\sum x^2$ and $\sum xy$):

$\sum x: 26 \quad \sum y: 41 \quad \sum x^2: 168 \quad \sum xy: 263$

Step3: Calculate Slope b

$$b = \frac{N \sum(xy) - \sum x \sum y}{\sum y N \sum(x^2) - (\sum x)^2}$$

$$= \frac{5 \times 263 - 26 \times 41}{5 \times 168 - 26^2}$$

$$= \frac{1315 - 1066}{840 - 676}$$

$$= \frac{249}{164}$$

$$b = 1.5183$$

Step 4: Calculate Intercept

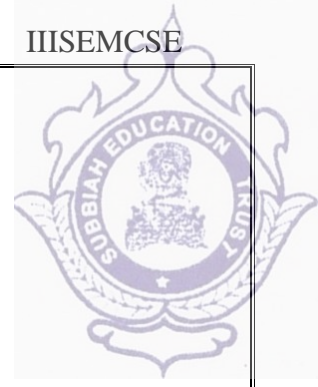
$$a = \frac{\sum y - b \sum x}{N}$$

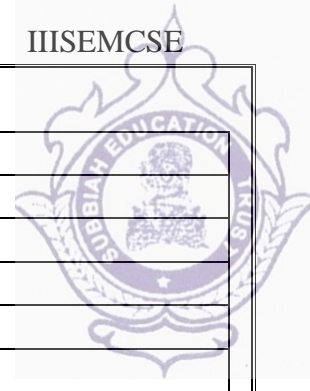
$$= \frac{41 - 1.5183 \times 26}{5}$$

$$a = 0.3049$$

Step5: $y' = bx + a$

$$y' = 1.518x + 0.305$$





x	y	y=1.518x+0.305	error
2	4	3.34	-0.66
3	5	4.86	-0.14
5	7	7.89	0.89
7	10	10.93	0.93
9	15	13.97	-1.03

To predict the value we can assume any value for x. Assume x=8.
Then y = 1.518 x 8 + 0.305
= 12.45

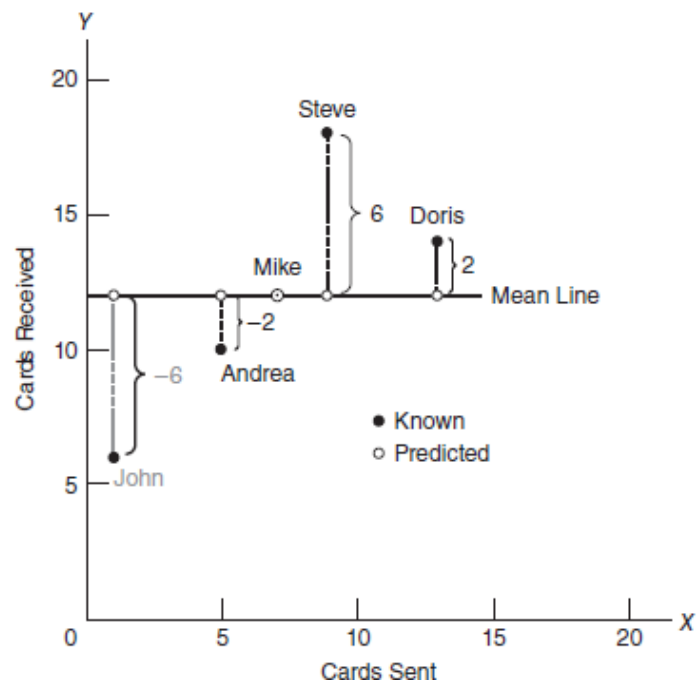
STANDARD ERROR OF ESTIMATE, $s_{y|x}$

The standard error of the estimate is a measure of the accuracy of predictions. The regression line is the line that minimizes the sum of squared deviations of prediction (also called the sum of squares error), and the standard error of the estimate is the square root of the average squared deviation.

The standard error of estimate and symbolized as $s_{y|x}$, this estimate of predictive error complies with the general format for any sample standard deviation, that is, the square root of a sum of squares term divided by its degrees of freedom.

$$SS_{y|x} = \sum(Y - Y')^2$$

A. Errors Using Mean



B. Errors Using Least Squares Equation

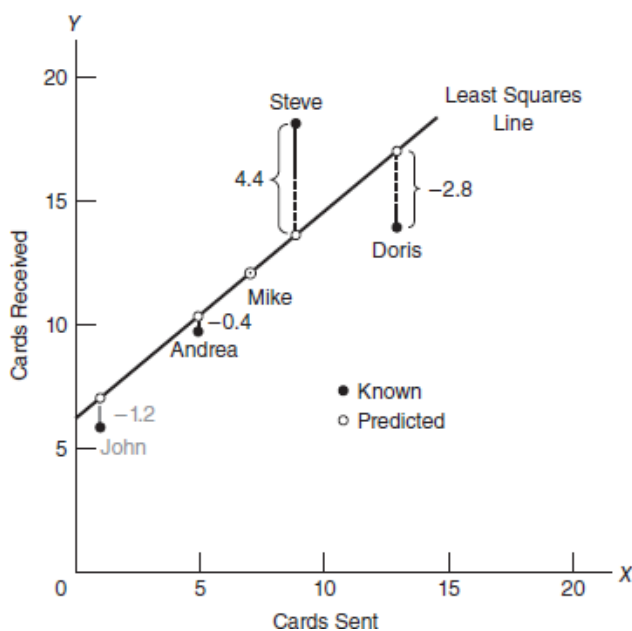
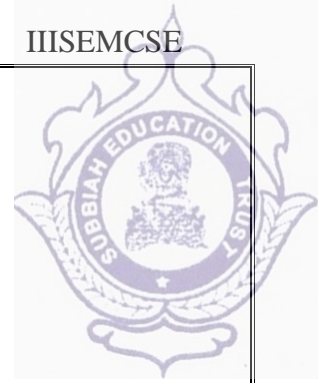


Fig. Predictive errors for five friends

Example

Calculate the standard error of estimate for the given X and Y values. X=1,2,3,4,5 Y=2,4,5,4,5



Solution

Create five columns labeled $x, y, y', y-y', (y-y')^2$ and $N=5$

x	y	x^2	xy	$Y' = bx+a$	$y-y'$	$(y-y')^2$
1	2	1	2	2.8	-0.8	0.64
2	4	4	8	3.4	0.6	0.36
3	5	9	15	4.0	1	1
4	4	16	16	4.6	-0.6	0.36
5	5	25	25	5.2	-0.2	0.04
$\Sigma x: 15$	$\Sigma y: 20$	$\Sigma x^2: 55$	$\Sigma xy: 66$			$\Sigma (y-y')^2 = 2.4$

Note: for finding b value we have to find xy and x^2 , so add xy and x^2 column in table

$$b = \frac{N \Sigma(xy) - \Sigma x \Sigma y}{\Sigma x^2 - \frac{(\Sigma x)^2}{N}}$$

$$b = \frac{5(66) - 15 \times 20}{5(55) - (15)^2}$$

$$= \frac{330 - 300}{275 - 225}$$

$$b = 30/50 = 0.6$$

$$a = \frac{\Sigma y - b \Sigma x}{N}$$

$$= \frac{20 - (0.6 \times 15)}{5}$$

$$= \frac{20 - 9}{5}$$

$$a = 9/5 = 2.2$$

$$SS_{y/x} = \frac{\Sigma (y-y')^2}{n-2}$$

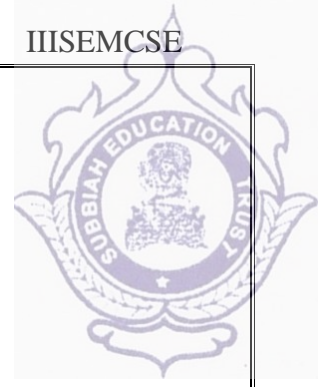
$$= \frac{2.4}{3}$$

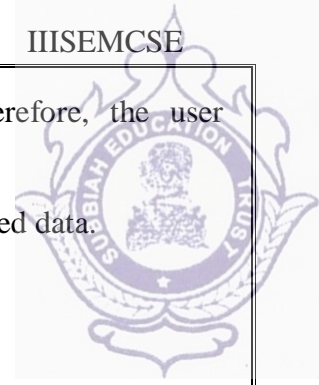
$$SS_{y/x} = 0.894$$

INTERPRETATION OF R^2

R^2 (or the coefficient of determination) is a statistical measure in a regression model that determines the proportion of variance in the dependent variable that can be explained by the independent variable. In other words, R^2 shows how well the data fit the regression model (the goodness of fit).

R^2 can take any values between 0 to 1. Although the statistical measure provides some useful insights regarding the regression model, the user should not rely only on the measure in the assessment of a statistical model.





In addition, it does not indicate the correctness of the regression model. Therefore, the user should always draw conclusions about the model by analyzing r^2 together with the other variables in a statistical model.

The most common interpretation of r^2 is how well the regression model explains observed data.

$$r^2 = \frac{SS_{Y'}}{SS_Y} = \frac{SS_Y - SS_{YIX}}{SS_Y}$$

$$SS_{Y'} = \sum(Y' - \bar{Y})^2$$

MULTIPLE REGRESSION EQUATIONS

Multiple regression is a statistical technique applied on datasets dedicated to draw out a relationship between one response or dependent variable and multiple independent variables.

Multiple regression works by considering the values of the available multiple independent variables and predicting the value of one dependent variable.

Example:

A researcher decides to study students' performance from a school over a period of time. He observed that as the lectures proceed to operate online, the performance of students started to decline as well. The parameters for the dependent variable "decrease in performance" are various independent variables like "lack of attention, more internet addiction, neglecting studies" and much more.

Formula to find multiple regression

$$y = b_1x_1 + b_2x_2 + \dots + b_nx_n + a$$

REGRESSION TOWARD THE MEAN

Regression toward the mean refers to a tendency for scores, particularly extreme scores, to shrink toward the mean.

In statistics, regression toward the mean (also called reversion to the mean, and reversion to mediocrity) is a concept that refers to the fact that if one sample of a random variable is extreme, the next sampling of the same random variable is likely to be closer to its mean.

Example

A military commander has two units return, one with 20% casualties and another with 50% casualties. He praises the first and berates the second. The next time, the two units return with the opposite results. From this experience, he "learns" that praise weakens performance and berating increases performance.

The Regression Fallacy

The regression fallacy is committed whenever regression toward the mean is interpreted as a real, rather than a chance, effect.

The regression fallacy can be avoided by splitting the subset of extreme observations into two groups

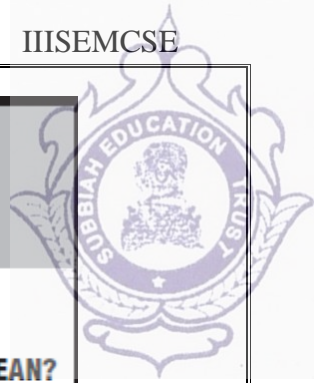
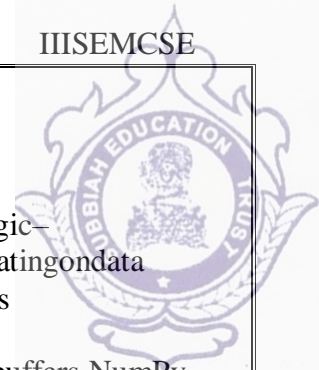


Table 7.4
REGRESSION TOWARD THE MEAN: BATTING AVERAGES OF TOP
10 HITTERS IN MAJOR LEAGUE BASEBALL
DURING 2014 AND HOW THEY FARED DURING 2015

TOP 10 HITTERS (2014)	BATTING AVERAGES*		REGRESS TOWARD MEAN?
	2014	2015	
1. J. Altuve	.341	.313	Yes
2. V. Martinez	.335	.282	Yes
3. M. Brantley	.327	.310	Yes
4. A. Beltre	.324	.287	Yes
5. J. Abreu	.317	.290	Yes
6. R. Cano	.314	.287	Yes
7. A. McCutchen	.314	.292	Yes
8. M. Cabrera	.313	.338	No
9. B. Posey	.311	.318	No
10. B. Revere	.306	.306	No



UNIT IV PYTHON LIBRARIES FOR DATA WRANGLING

Basics of NumPy arrays—aggregations—computations on arrays—comparisons, masks, boolean logic—fancy indexing—structured arrays—Data manipulation with Pandas—data indexing and selection—operating on data—missing data— Hierarchical indexing —combining datasets —aggregation and grouping—pivot tables

NumPy (short for Numerical Python) provides an efficient interface to store and operate on dense data buffers. NumPy arrays are like Python's built-in list type, but NumPy arrays provide much more efficient storage and data operations as the arrays grow larger in size.

We'll cover a few categories of basic array manipulations here:

Attributes of arrays

Determining the size, shape, memory consumption, and data types of arrays

Indexing of arrays

Getting and setting the value of individual array elements

Slicing of arrays

Getting and setting smaller subarrays within a larger array

Reshaping of arrays

Changing the shape of a given array

Joining and splitting of arrays

Combining multiple arrays into one, and splitting one array into many

NumPy Array Attributes

- `ndim` (the number of dimensions),
- `shape` (the size of each dimension)
- `size` (the total size of the array)

Example

```
np.random.seed(0) # seed for reproducibility
x1=np.random.randint(10,size=6) # One-dimensional array
x2=np.random.randint(10,size=(3,4)) # Two-dimensional array
x3=np.random.randint(10,size=(3,4,5)) # Three-dimensional array
print("x3 ndim: ",
x3.ndim) print("x3 shape:",
x3.shape) print("x3 size:
",x3.size)

print("dtype:",x3.dtype)

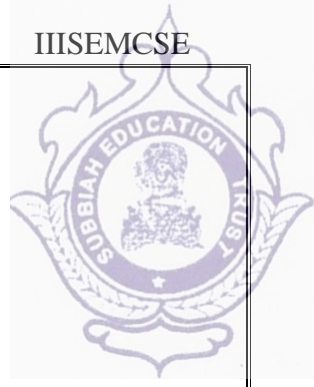
print("itemsize:",x3.itemsize,"bytes")
print("nbytes:",x3.nbytes,"bytes")
```

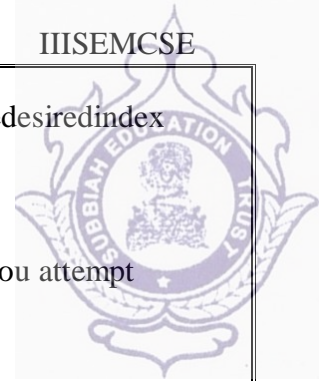
Array Indexing:

- Accessing Single Elements

Accessing Single Elements

- Indexing in NumPy will feel quite familiar like list indexing,





- In a one-dimensional array, you can access the value (counting from zero) by specifying the desired index in square brackets, just as with Python lists
- To index from the end of the array, you can use negative indices
- In a multidimensional array, you access items using a comma-separated tuple of indices
- Unlike Python lists, NumPy arrays have a fixed type. This means, for example, that if you attempt to insert a floating-point value to an integer array, the value will be silently truncated.

Array Slicing: Accessing Subarrays

Just as we can use square brackets to access individual array elements, we can also use them to access subarrays with the slice notation, marked by the colon (:) character.

The NumPy slicing syntax follows that of the standard Python list; to access a slice of an array `x`, use this:

```
x[start:stop:step]
start – starting array index
stop – array index to stop (last value will not be considered)
step – terms has to be printed from start to stop
Default to the values start=0, stop=size of dimension, step=1.
```

Example

```
x =
np.arange(10)
x
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

```
x[:5] # prints first five elements
array([0, 1, 2, 3, 4])
```

```
x[5:] # elements after index 5
array([5, 6, 7, 8, 9])
```

```
x[4:7] # middle subarray (from 4th index to 6th index)
array([4, 5, 6])
```

While using negative indices the defaults for start and stop are swapped. This becomes a convenient way to reverse an array

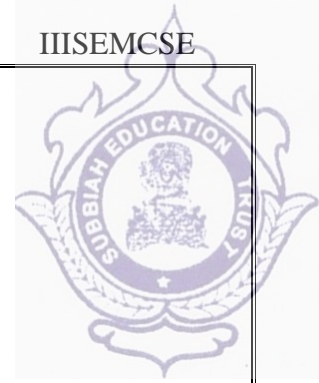
```
x[::-1] # all elements, reversed
array([9, 8, 7, 6, 5, 4, 3, 2, 1, 0])
```

```
x[5::-2] # reverse every other from index 5
array([5, 3, 1])
```

Multidimensional subarrays

Multidimensional slices work in the same way, with multiple slices separated by commas. For example:

```
x2
array([[12, 5, 2, 4],
       [7, 6, 8, 8],
       [1, 6, 7, 7]])
```



```
x2[:2, :3] # two rows, three
columnsarray([[12,5,2],
              [ 7,6,8]])
```

```
x2[:3, ::2] # all rows, every other column(every second
column)array([[12,2],
              [ 7,8],
              [ 1,7]])
```

Finally, subarray dimensions can even be reversed together

```
x2[::-1, ::-1]
array([[ 7,7,6,1],
       [8,8, 6,7],
       [ 4,2,5,12]])
```

Reshaping of Arrays

The most flexible way of doing this is with the **reshape()** method. For example, if you want to put the numbers 1 through 9 in a 3x3 grid, you can do the following

```
grid = np.arange(1, 10).reshape((3,
3))print(grid)
[[12 3]
 [456]
 [7 89]]
```

Array Concatenation and Splitting

Concatenation of arrays

Concatenation, or joining of two arrays in NumPy, is primarily accomplished through the routines **np.concatenate**, **np.vstack**, and **np.hstack**. **np.concatenate** takes a tuple or list of arrays as its first argument.

```
x=np.array([1,2,3])
y = np.array([3, 2,
1])np.concatenate([x,
y])
```

```
array([1,2,3,3,2, 1])
```

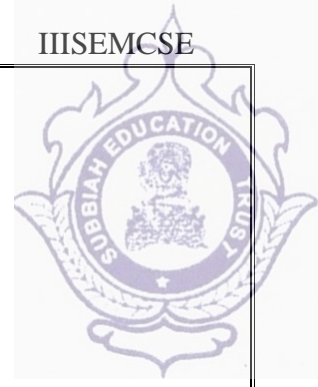
You can also concatenate more than two arrays at once

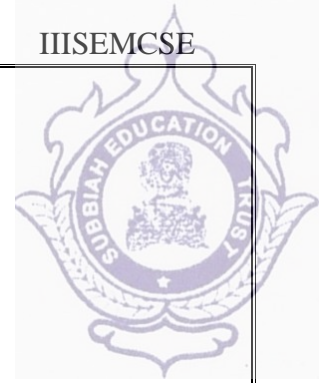
```
z =[99,99, 99]
print(np.concatenate([x, y,
z]))[ 123321999999]
```

np.concatenate can also be used for two-dimensional arrays

```
grid =np.array([[1,2,3],
                [4,5, 6]])
np.concatenate([grid,grid])
```

```
array([[1,2, 3],
       [4,5,6],
       [1,2,3],
```





```
[4,5,6]])
```

Concatenate along the second axis (zero-indexed)

```
np.concatenate([grid,grid],axis=1)
```

```
array([[1,2,3,1,2,3],  
       [4,5,6,4,5,6]])
```

np.vstack(vertical stack) functions

```
x=np.array([1,2,3])  
grid =np.array([[9,8,7],  
               [6,5,4]])
```

```
np.vstack([x,grid])
```

```
array([[1,2, 3],  
       [9,8, 7],  
       [6,5,4]])
```

np.hstack(horizontal stack) functions

```
y=np.array([[99],  
           [99]])
```

```
np.hstack([grid,y])
```

```
array([[ 9,8,7, 99],  
       [ 6,5,4,99]])
```

Splitting of arrays

The opposite of concatenation is splitting, which is implemented by the functions **np.split**, **np.hsplit**, and **np.vsplit**. For each of these, we can pass a list of indices giving the split points

```
x=[1,2,3,99,99,3,2,1]  
x1, x2, x3 = np.split(x, [3,  
5])  
print(x1, x2,x3)
```

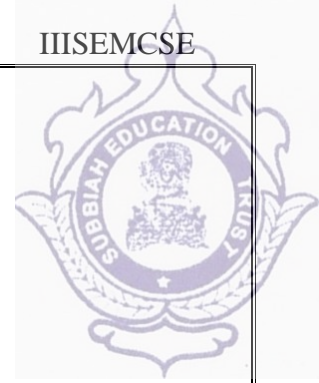
```
[1 23][9999][321]
```

Notice that N split points lead to $N + 1$ subarrays. There are related functions **np.hsplit** and **np.vsplit** are similar

```
grid = np.arange(16).reshape((4,  
4))  
grid
```

```
array([[ 0,1,2,3],  
       [ 4,5,6,7],  
       [ 8,9,10,11],  
       [12,13,14,15]])
```

```
upper, lower=np.vsplit(grid,[2])  
print(upper)  
print(lower)
```



```
[[012 3]
 [456 7]]
[[891011]
 [12131415]]
```

```
left,right=np.hsplit(grid,[2])
print(left)
print(right)
```

```
[[01]
 [45]
 [89]
 [1213]]
[[23]
 [67]
 [1011]
 [1415]]
```

Computation on NumPy Arrays: Universal Functions

Introducing UFuncs

NumPy provides a convenient interface into just this kind of statically typed, compiled routine. This is known as a vectorized operation.

Vectorized operations in NumPy are implemented via ufuncs, whose main purpose is to quickly execute repeated operations on values in NumPy arrays. Ufuncs are extremely flexible—before we saw an operation between a scalar and an array, but we can also operate between two arrays

Exploring NumPy's UFuncs

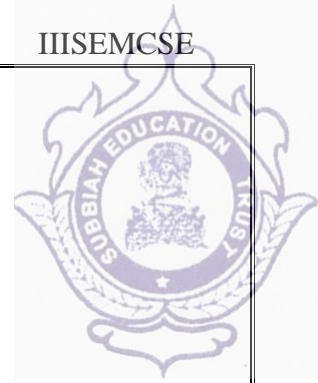
Ufuncs exist in two flavors: unary ufuncs, which operate on a single input, and binary ufuncs, which operate on two inputs. We'll see examples of both these types of functions here.

Array arithmetic

NumPy's ufuncs make use of Python's native arithmetic operators. The standard addition, subtraction, multiplication, and division can all be used.

```
x=np.arange(4)
print("x =", x)
print("x + 5 =", x + 5)
print("x - 5 =", x - 5)
print("x * 2 =", x * 2)
```

Operator	Equivalent ufunc	Description
+	np.add	Addition (e.g., 1+1=2)
-	np.subtract	Subtraction (e.g., 3-2=1)
-	np.negative	Unary negation (e.g., -2)
*	np.multiply	Multiplication (e.g., 2*3=6)
/	np.divide	Division (e.g., 3 / 2 = 1.5)



//	np.floor_divide	Floordivision (e.g.,3 //2 =1)
**	np.power	Exponentiation(e.g.,2 **3 =8)
%	np.mod	Modulus/remainder(e.g.,9%4 =1)

Absolutevalue

JustasNumPyunderstandsPython'sbuiltinarithmeticooperators,italsounderstandsPython'sbuiltinabsolutevaluefunction.

- np.abs()
- np.absolute()

```
x = np.array([-2, -1, 0, 1,
2])abs(x)
```

```
array([2, 1,0,1,2])
```

ThecorrespondingNumPyfuncis np.absolute,which is also available under thealias np.abs

```
np.absolute(x)arra
y([2,1,0,1,2])
```

```
np.abs(x)
array([2, 1,0,1,2])
```

Trigonometricfunctions

NumPyprovidesalargenumberofusefulufuncs,andsoeofthemoftusefulforthedatacientistarethetrigonometric functions.

- np.sin()
- np.cos()
- np.tan()

inversetrigonometricfunctions

- np.arcsin()
- np.arccos()
- np.arctan()

Defininganarrayofangles:theta=np.linspace(0,np.pi, 3)

Computesometrigonometricfunctions like

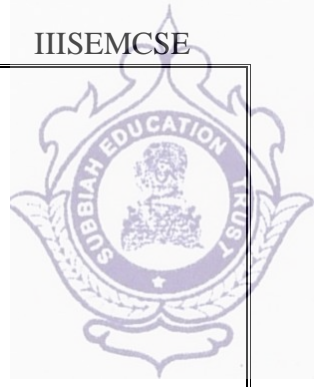
```
print("theta = ",
theta)print("sin(theta) = ",
np.sin(theta))print("cos(theta) = ",
np.cos(theta))print("tan(theta)=",n
p.tan(theta))
```

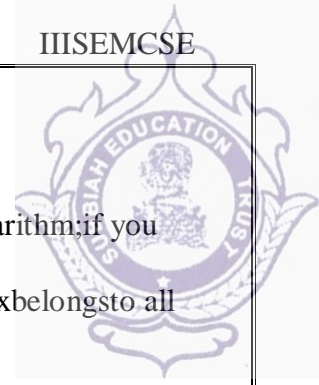
Exponentsandlogarithms

Anothercommon typeofoperation availablein aNumPyufuncaretheexponentials.

- np.exp(x) – calculateexponent ofall elementsin theinput arrayie e^x ($e=2.7182$)
- np.exp2(x)–calculate 2^{**x} forallxbeingthe arrayelements
- np.power(x,y) – calculates thepower as x^y

```
x=[1,2, 3]
print("x =",x)
print("e^x=",np.exp(x))
```





```
print("2^x=", np.exp2(x))
print("3^x =", np.power(3,x))
```

The inverse of the exponentials, the logarithms, are also available. The basic `np.log` gives the natural logarithm, if you prefer to compute the base-2 logarithm or the base-10 logarithm as.

- `np.log(x)` - is a mathematical function that helps us to calculate Natural logarithm of `x` where `x` belongs to all the input array elements
- `np.log2(x)` - to calculate Base-2 logarithm of `x`
- `np.log10(x)` - to calculate Base-10 logarithm of `x`

```
x=[1, 2,4, 10]
print("x =",x)
print("ln(x)=", np.log(x))
print("log2(x)=", np.log2(x))
print("log10(x)=", np.log10(x))
```

Specialized ufuncs

NumPy has many more ufuncs available like

- Hyperbolic trig functions,
- Bitwise arithmetic,
- Comparison operators,
- Conversions from radians to degrees,
- Rounding and remainders, and much more

More specialized and obscure ufuncs is the submodule `scipy.special`. If you want to compute some obscure mathematical function on your data, chances are it is implemented in `scipy.special`.

- Gamma function

Advanced Ufunc Features

Specifying output

Rather than creating a temporary array, you can use this to write computation results directly to the memory location where you'd like them to be. For all ufuncs, you can do this using the `out` argument of the function.

```
x =
np.arange(5)
y = np.empty(5)
np.multiply(x, 10, out=y)
print(y)
```

```
[0. 10. 20. 30. 40.]
```

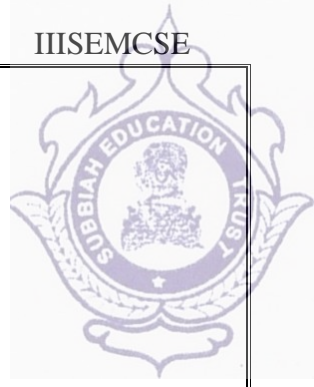
Aggregates

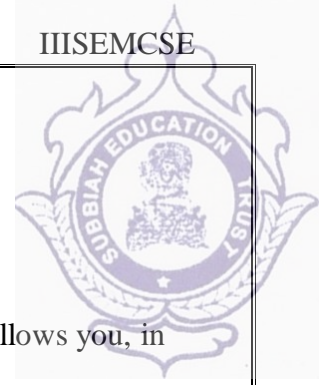
To reduce an array with a particular operation, we can use the `reduce` method of any ufunc. `reduce` repeatedly applies a given operation to the elements of an array until only a single result remains.

```
x = np.arange(1,
6)
np.add.reduce(x)
```

Similarly, calling `reduce` on the `multiply` ufunc results in the product of all array elements

```
np.multiply.reduce(x)
120
```





If we'd like to store all the intermediate results of the computation, we can instead use `Accumulate`
`np.add.accumulate(x)`
`rray([1,3,6,10,15])`

Outer products

`ufunc` can compute the output of all pairs of two different inputs using the outer method. This allows you, in one line, to do things like create a multiplication table.

```
x = np.arange(1,
6)np.multiply.outer(x,
x)

array([[ 1, 2, 3, 4, 5],
       [ 2, 4, 6, 8, 10],
       [ 3, 6, 9, 12, 15],
       [ 4, 8, 12, 16, 20],
       [ 5, 10, 15, 20, 25]])
```

Aggregations: Min, Max, and Everything in Between Minimum and Maximum

Python has built-in `min` and `max` functions, used to find the minimum value and maximum value of any given array.

For `min`, `max`, `sum`, and several other NumPy aggregates, a shorter syntax is to use methods of the array object itself.

- `np.min()` – finds the minimum (smallest) value in the array
- `np.max()` – finds

the maximum (largest) value in the array Example

```
x=[1,2,3,4]
np.min(x)
1
np.max(x)
4
```

Multidimensional aggregates

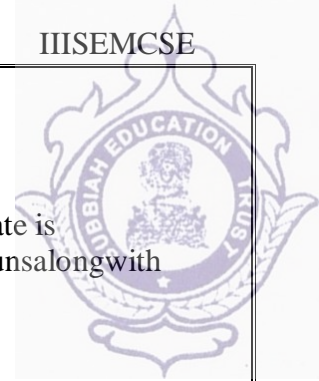
One common type of aggregation operation is an aggregate along a row or column.

By default, each NumPy aggregation function will return the aggregate over the entire array. ie. If we use `np.sum()` it will calculate the sum of all elements of the array.

Example

```
m=np.random.random((3,4))
print(M)
```

```
[[0.89675760 0.03783739  0.75952519  0.06682827]
 [0.8354065  0.99196818  0.19544769  0.43447084]
 [ 0.66859307 0.15038721  0.37911423  0.6687194 ]]
```



`M.sum()`6.085055566
7307118

Aggregation functions take an additional argument specifying the axis along which the aggregate is computed. The axis normally takes either 0 or 1. If the axis=0 then it runs along with columns, if axis=1 it runs along with rows.

Example

We can find the minimum value within each column by specifying axis=0

`M.min(axis=0)`
`array([0.66859307, 0.03783739, 0.19544769, 0.06682827])`

Similarly, we can find the maximum value within each

row `M.max(axis=1)`
`array([0.8967576 , 0.99196818, 0.6687194])`

Other aggregation functions

NumPy provides many other aggregation functions most aggregates have a NaN-safe counterpart that computes the result while ignoring missing values, which are marked by the special IEEE floating-point NaN value.

Function Name	NaN-safe Version	Description
<code>np.sum</code>	<code>np.nansum</code>	Computes sum of elements
<code>np.prod</code>	<code>np.nanprod</code>	Compute product of elements
<code>np.mean</code>	<code>np.nanmean</code>	Compute median of elements
<code>np.std</code>	<code>np.nanstd</code>	Compute standard deviation
<code>np.var</code>	<code>np.nanvar</code>	Compute variance
<code>np.min</code>	<code>np.nanmin</code>	Find minimum value
<code>np.max</code>	<code>np.nanmax</code>	Find maximum value
<code>np.argmin</code>	<code>np.nanargmin</code>	Find index of minimum value
<code>np.argmax</code>	<code>np.nanargmax</code>	Find index of maximum value
<code>np.median</code>	<code>np.nanmedian</code>	Compute median of elements
<code>np.percentile</code>	<code>np.nanpercentile</code>	Compute rank-based statistics of elements
<code>np.any</code>	N/A	Evaluate whether any elements are true
<code>np.all</code>	N/A	Evaluate whether all elements are true

Computation on Arrays: Broadcasting

Broadcasting is simply a set of rules for applying binary functions (addition, subtraction, multiplication, etc.) on arrays of different sizes.

For arrays of the same size, binary operations are performed on an element-by-element

basis. `a=np.array([0, 1, 2])`

`b = np.array([5, 5, 5])`
`a+b`

`array([5,6,7])`

Broadcasting allows these types of binary operations to be performed on arrays of different sizes. `a+5`

`array([5,6,7])`



We can think of this as an operation that stretches or duplicates the value 5 into the array [5,5,5], and adds the results. The advantage of NumPy's broadcasting is that this duplication of values does not actually take place.

We can similarly extend this to arrays of higher dimension. Observe the result when we add a one-dimensional array to a two-dimensional array.

Example

```
M=np.ones((3,3))
```

M

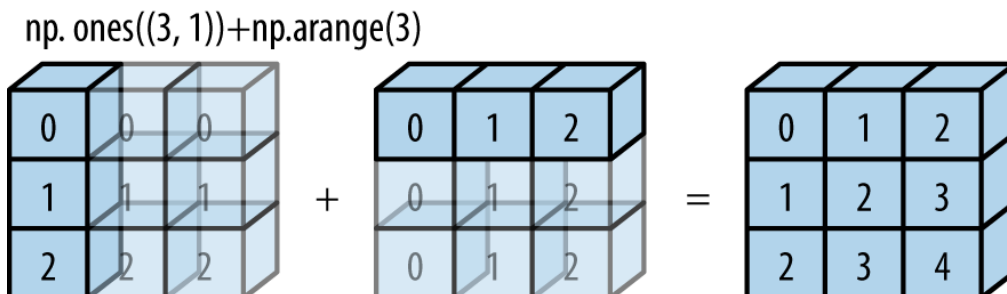
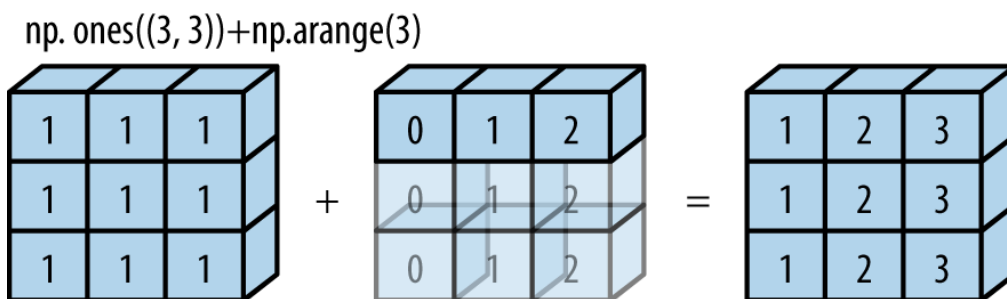
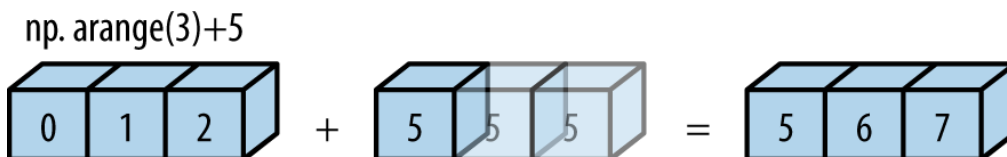
```
array([[ 1.,  1.,  1.],
       [ 1.,  1.,  1.],
       [ 1.,  1.,  1.]])
```

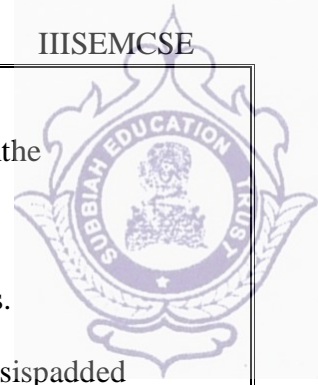
M+a

```
array([[ 1.,  2.,  3.],
       [ 1.,  2.,  3.],
       [ 1.,  2.,  3.]])
```

Here the one-dimensional array is stretched, or broadcast, across the second dimension in order to match the shape of M.

Just as before we stretched or broadcasted one value to match the shape of the other, here we've stretched both a and b to match a common shape, and the result is a two dimensional array.





The light boxes represent the broadcasted values: again, this extra memory is not actually allocated in the course of the operation, but it can be useful conceptually to imagine that it is.

Rules of Broadcasting

Broadcasting in NumPy follows a strict set of rules to determine the interaction between the two arrays.

- Rule 1: If the two arrays differ in their number of dimensions, the shape of the one with fewer dimensions is padded with ones on its leading (left) side.
- Rule 2: If the shape of the two arrays does not match in any dimension, the array with shape equal to 1 in that dimension is stretched to match the other shape.
- Rule 3: If in any dimension the sizes disagree and neither is equal to 1, an error is raised.

Broadcasting example 1

Let's look at adding a two-dimensional array to a one-dimensional array:

```
M = np.ones((2,
3))
a = np.arange(3)
```

Let's consider

```
an operation on these two arrays. The shapes of the arrays are:
M.shape = (2, 3)
a.shape = (3,)
```

We see by rule 1 that the array has fewer dimensions, so we pad it on the left with

```
ones: M.shape -> (2, 3)
a.shape -> (1, 3)
```

By rule 2, we now see that the first dimension disagrees, so we stretch this dimension to

```
match: M.shape -> (2, 3)
a.shape -> (2, 3)
```

The shapes match, and we see that the final shape will be (2, 3):

```
M + a
array([[ 1., 2., 3.],
       [ 1., 2., 3.]])
```

Broadcasting example 2

Let's take a look at an example where both arrays

```
need to be broadcast: a = np.arange(3).reshape((3, 1))
b = np.arange(3)
```

Again, we'll start by writing out the shape of the arrays: a.shape

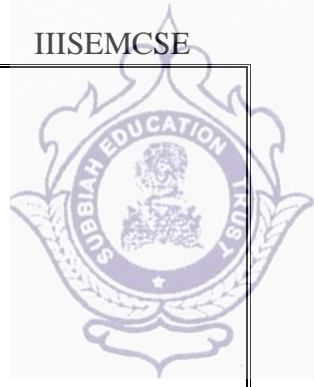
```
pe = (3, 1)
b.shape = (3,)
```

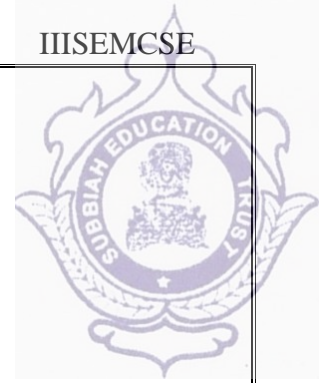
Rule 1 says we must pad the shape of b with ones: a.shape

```
e -> (3, 1)
b.shape -> (1, 3)
```

And rule 2 tells us that we upgrade each of these ones to match the corresponding size of the other array: a.shape -

```
> (3, 3)
b.shape -> (3, 3)
```





Because the result matches, these shapes are compatible. We can see this here: a+b

```
array([[0, 1, 2],
       [1, 2, 3],
       [2, 3, 4]])
```

Comparisons, Masks, and Boolean Logic

Comparison Operators as Functions.

We saw that using +, -, *, /, and others on arrays lead to element-wise operations. NumPy also implements comparison operators such as < (less than) and > (greater than) as element-wise functions.

The result of these comparison operators is always an array with a Boolean data type. All six of the standard comparison operations are available:

```
x = np.array([1, 2, 3, 4, 5])
x < 3 # less than
array([ True,  True, False, False, False],
      dtype=bool)
x > 3 # greater than
array([False, False, False,  True,  True], dtype=bool)

x <= 3 # less than or equal
array([ True,  True,  True, False, False], dtype=bool)

x >= 3 # greater than or equal
array([False, False,  True,  True,  True], dtype=bool)

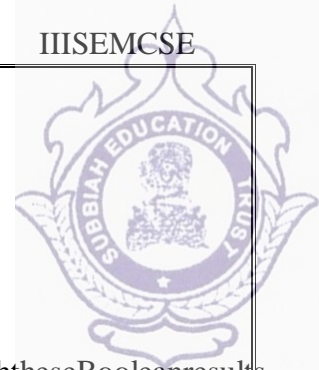
x != 3 # not equal
array([ True,  True, False,  True,  True], dtype=bool)

x == 3 # equal
array([False, False,  True, False, False], dtype=bool)
```

Operator	Equivalent function
==	np.equal
!=	np.not_equal
<	np.less
<=	np.less_equal
>	np.greater
>=	np.greater_equal

Just as in the case of arithmetic functions, these will work on arrays of any size and shape. Here is a two-dimensional example

```
rng =
np.random.RandomState(0)
x = rng.randint(10, size=(3, 4))
x
array([[5, 0, 3, 3],
       [7, 9, 3, 5],
       [2, 4, 7, 6]])
```



x<6

```
array([[ True, True, True,
        True],[False,False,True,T
        rue],
        [True,True, False,False]],dtype=bool)
```

The result is a Boolean array, and NumPy provides a number of straightforward patterns for working with these Boolean results.

Working with Boolean Arrays

- np.count_nonzero()
- np.sum()
- np.sum(x,axis)
- np.any()
- np.all()
- np.all(x ,axis)

Boolean operators

Operator	Equivalent func
&	np.bitwise_and
	np.bitwise_or
^	np.bitwise_xor
~	np.bitwise_not

Example

```
np.sum((inches>0.5)&(inches<1))inc
hes>(0.5&inches)<1
np.sum(~((inches<=0.5)|(inches>=1)))
```

Boolean Arrays as Masks

A more powerful pattern is to use Boolean arrays as masks, to select particular subsets of the data themselves. Returning to our x array from before, suppose we want an array of all values in the array that are less than, say, 5. We can obtain

Boolean array for this condition easily, as we've already seen Example

```
x
array([[5,0,3,3],
        [7, 9, 3,5],
        [2, 4, 7, 6]])
```

x<5

```
array([[False, True, True,
        True],[False,False,True,F
        else],
        [True,True, False,False]],dtype=bool)
```

Masking operation

To select these values from the array, we can simply index on this Boolean array; this is known as a masking operation.

```
x[x<5]
```



```
array([0,3,3, 3,2,4])
```

What is returned is a one-dimensional array filled with all the values that meet this condition; in other words, all the values in positions at which the mask array is True.

Fancy Indexing

Fancy indexing is like the simple indexing we've already seen, but we pass arrays of indices in place of single scalars. This allows us to very quickly access and modify complicated subsets of an array's values.

Exploring Fancy Indexing

Fancy indexing is conceptually simple: it means passing an array of indices to access multiple array elements at once.

Types of fancy indexing.

- Indexing/ accessing more values
- Array of indices
- In multidimensional
- Standard indexing

Example

```
import numpy as np
rand =
np.random.RandomState(42)x =
rand.randint(100, size=10)print(x)
```

```
[51 92 14 71 60 20 82 86 74 74]
```

Indexing/ accessing more values

Suppose we want to access three different elements. We could do it

```
likethis: [x[3], x[7], x[2]]
```

```
[71, 86, 14]
```

Array of indices

We can pass a single list or array of indices to obtain the same

```
result.ind = [3, 7, 4]
```

```
x[ind]
```

```
array([71, 86, 60])
```

In multidimensional

Fancy indexing also works in multiple dimensions. Consider the following array.

```
X = np.arange(12).reshape((3,
4))X
```

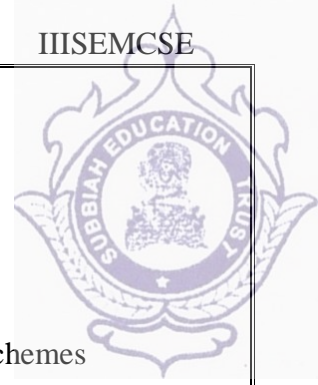
```
array([[ 0, 1, 2, 3],
       [ 4, 5, 6, 7],
       [ 8, 9, 10, 11]])
```

Standard indexing

Like with standard indexing, the first index refers to the row, and the second to the

```
column.row = np.array([0, 1, 2])
```

```
col = np.array([2, 1, 3])
```



```
X[row,col]array(
```

```
[2,5,11])
```

Combined Indexing

For even more powerful operations, fancy indexing can be combined with the other indexing schemes we've seen.

Example array

```
print(X)
```

```
[[ 0 1 2 3]
```

```
 [ 4 5 6 7]
```

```
 [ 8 9 10 11]]
```

- Combine fancy and simple indices

```
X[2,[2,0, 1]]
```

```
array([10,8, 9])
```

- Combine fancy indexing with slicing

```
X[1:,[2,0, 1]]
```

```
array([[ 6,4,5],
```

```
 [10,8,9]])
```

- Combine fancy indexing with

```
masking mask = np.array([1, 0, 1, 0],
```

```
dtype=bool) X[row[:,np.newaxis],mask]
```

```
array([[ 0,2],
```

```
 [ 4,6],
```

```
 [ 8,10]])
```

Modifying Values with Fancy Indexing

Just as fancy indexing can be used to access parts of an array, it can also be used to modify parts of an array. Change some value in an array

Modify particular element by index

For example, imagine we have an array of indices and we'd like to set the corresponding items in an array to some value.

```
x = np.arange(10)
```

```
i = np.array([2,1,8, 4])
```

```
x[i] = 99
```

```
print(x)
```

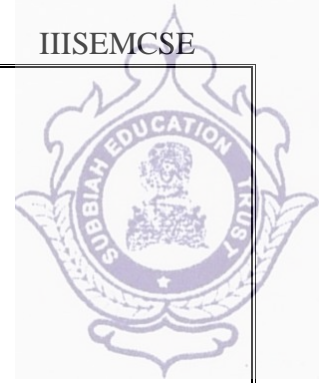
```
[ 0 99 99 99 99 56 7 99 99]
```

Using assignment operator

We can use any assignment-type operator for this. For example

```
x[i] -= 10
```

```
print(x)
```



[08989389 567899]

Using at()

Use the at() method of ufuncs for other behavior of modifications.

```
x =  
np.zeros(10)  
np.add.at(x, i,  
1)print(x)
```

[0.0.1. 2.3.0.0. 0.0.0.]

Sorting Arrays

Sorting in NumPy: np.sort and np.argsort

Python has built-in sort and sorted functions to work with lists, we won't discuss them here because NumPy's np.sort function turns out to be much more efficient and useful for our purposes. By default np.sort uses an $O[N \log N]$, quicksort algorithm, though mergesort and heapsort are also available. For most applications, the default quicksort is more than sufficient.

Sorting without modifying the input.

To return a sorted version of the array without modifying the input, you can use np.sort

```
x =  
np.array([2,1,4,3,5])  
np.sort(x)  
  
array([1, 2, 3, 4, 5])
```

Return sorted indices

A related function is argsort, which instead returns the *indices* of the sorted elements

```
x = np.array([2,1,4,3,5])  
i = np.argsort(x)  
print(i)
```

[1 0 3 2 4]

Sorting along rows or columns

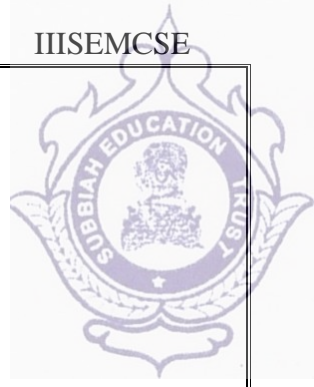
A useful feature of NumPy's sorting algorithms is the ability to sort along specific rows or columns of a multidimensional array using the axis argument. For example

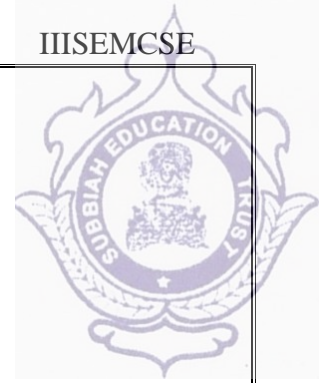
```
rand =  
np.random.RandomState(42)  
X = rand.randint(0, 10, (4, 6))  
print(X)
```

```
[[637469]  
[267437]  
[725417]  
[5 14095]]
```

```
np.sort(X,  
axis=0)array([[2,1,4,0,
```

1,5],





```
[5,2,5,4,3, 7],
[6,3,7,4,6, 7],
[7,6,7,4, 9,9]]
```

```
np.sort(X,
axis=1)array([[3,4,6,6,
7,9],
[2,3,4,6,7,7],
[1,2,4,5,7,7],
[0,1,4,5,5,9]])
```

PartialSorts:Partitioning

Sometimes we're not interested in sorting the entire array, but simply want to find the K smallest values in the array. NumPy provides this in the np.partition function. np.partition takes an array and a number K; the result is a new array with the smallest K values to the left of the partition, and the remaining values to the right, in arbitrary order

```
x= np.array([7,2, 3,1,6,5, 4])
np.partition(x,3)
```

```
array([2, 1,3,4,6,5,7])
```

Note that the first three values in the resulting array are the three smallest in the array, and the remaining array positions contain the remaining values. Within the two partitions, the elements have arbitrary order.

Partitioning in multidimensional array

Similarly to sorting, we can partition along an arbitrary axis of a multidimensional array.

```
np.partition(X,2, axis=1)
```

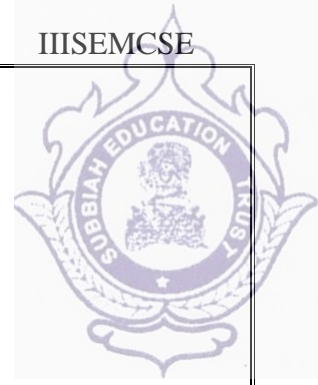
```
array([[3,4,6,7,6,9],
[2,3,4,7,6,7],
[1,2,4,5,7,7],
[0,1,4,5,9,5]])
```

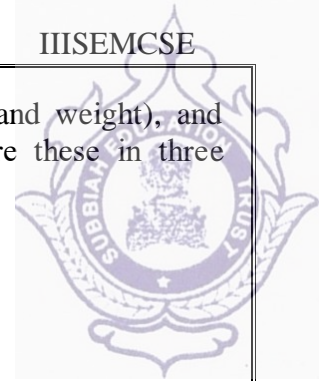
Structured Arrays

This section demonstrates the use of NumPy's structured arrays and record arrays, which provide efficient storage for compound, heterogeneous data.

NumPy data types

Character	Description	Example
'b'	Byte	np.dtype('b')
'i'	Signed integer	np.dtype('i4') == np.int32
'u'	Unsigned integer	np.dtype('u1') == np.uint8
'f'	Floating point	np.dtype('f8') == np.float64
'c'	Complex floating point	np.dtype('c16') == np.complex128
'S', 'a'	string	np.dtype('S5')
'U'	Unicode string	np.dtype('U') == np.str_
'Rawdata (void)'		np.dtype('V') == np.void





Consider if we have several categories of data on a number of people (say, name, age, and weight), and we'd like to store these values for use in a Python program. It would be possible to store these in three separate arrays.

```
name = ['Alice', 'Bob', 'Cathy',
'Doug']
age = [25, 45, 37, 19]
weight = [55.0, 85.5, 68.0, 61.5]
```

Creating structured array

NumPy can handle this through structured arrays, which are arrays with compound data types. Create a structured array using a compound data type specification as follows.

```
data = np.zeros(4, dtype={'names': ('name', 'age', 'weight'),
'formats': ('<U10', '<i4', '<f8')})
```

```
print(data.dtype)
[('name', '<U10'), ('age', '<i4'), ('weight',
'<f8')]
U10-Unicode string
of maximum length 10
i4-4-byte (i.e., 32 bit)
integer
f8-8-byte (i.e., 64 bit)
float
```

Now we can fill the array with our list of values

```
data['name'] =
name
data['age'] =
age
data['weight'] =
weight
print(data)
```

```
[('Alice', 25, 55.0), ('Bob', 45, 85.5), ('Cathy', 37, 68.0), ('Doug', 19, 61.5)]
```

Refer values through index or name

The handy thing with structured arrays is that you can now refer to values either by index or by name.

i. `data['name']` # by name

```
array(['Alice', 'Bob', 'Cathy', 'Doug'], dtype='<U10')
```

ii. `data[0]` # by index

```
('Alice', 25, 55.0)
```

Using Boolean masking

This allows to do some more sophisticated operations such as filtering on any fields.

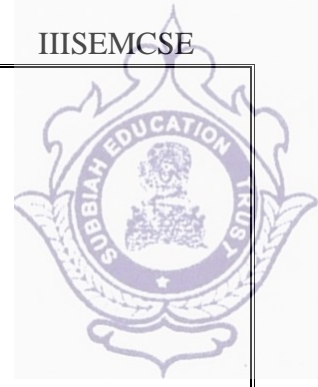
```
data[data['age'] < 30][ 'name']
```

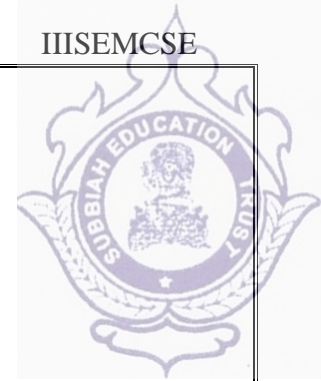
```
array(['Alice', 'Doug'], dtype='<U10')
```

Creating Structured Arrays

Dictionary method

```
np.dtype({'names': ('name', 'age', 'weight'),
'formats': ('<U10', '<i4',
'f8')})
dtype([('name', '<U10'), ('age', '<i4'), ('weight', '<f8')])
```





Numerical types can be specified with Python types

```
np.dtype({'names':('name','age','weight'),
         'formats':((np.str_, 10), int,
                    np.float32)})dtype([('name','<U10'),('age','<i8'),('weigh
t','<f4')])
```

List of tuples

```
np.dtype([('name','S10'),('age','i4'),('weight','f8']])
```

```
dtype([('name','S10'),('age','<i4'),('weight','<f8']])
```

Specify the types alone

```
np.dtype('S10,i4,f8')
```

```
dtype([('f0','S10'),('f1','<i4'),('f2','<f8']])
```

Data Manipulation with Pandas

Pandas is a newer package built on top of NumPy, and provides an efficient implementation of a DataFrame. DataFrames are essentially multidimensional arrays with attached row and column labels, and often with heterogeneous types and/or missing data.

Pandas, and in particular its Series and DataFrame objects, builds on the NumPy array structure and provides efficient access to these sort of “data munging” tasks that occupy much of a data scientist’s time.

Here we will focus on the mechanics of using Series, DataFrame, and related structures effectively.

Introducing Pandas Objects

Pandas objects can be thought of as enhanced versions of NumPy structured arrays in which the rows and columns are identified with labels rather than simple integer indices.

Pandas provides a host of useful tools, methods, and functionality on top of the basic data structures.

Three fundamental Pandas data structures: the Series, DataFrame, and Index

The Pandas Series Object

A Pandas Series is a one-dimensional array of indexed data. It can be created from a list or array as follows:

```
data = pd.Series([0.25, 0.5, 0.75,
                  1.0])data
```

```
00.25
```

```
10.50
```

```
20.75
```

```
31.00
```

```
dtype:float64
```

- **Finding values**

The values are simply a familiar NumPy array

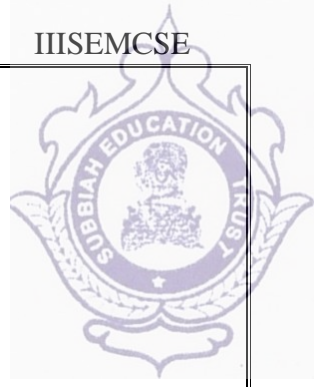
```
data.values
```

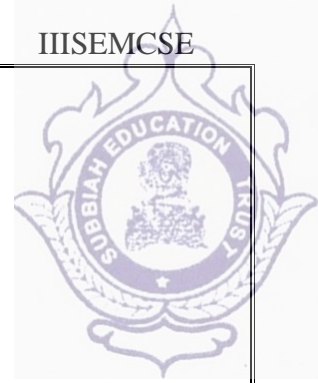
```
array([ 0.25,0.5,0.75,1.])
```

- **Finding index**

The index is an array-like object of type pd.Index

```
data.index
```





RangeIndex(start=0,stop=4,step=1)

- **Access by index**

Likewise with a NumPy array, data can be accessed by the associated index via the familiar Python square-bracket notation

```
data[1]
```

0.5

```
data[1:3]
```

10.50

20.75

dtype:float64

Series as generalized NumPy array

The NumPy array has an implicitly defined integer index used to access the values, the Pandas Series has an explicitly defined index associated with the values.

This explicit index definition gives the Series object additional capabilities. For example, the index need not be an integer, but can consist of values of any desired type.

For example, if we wish, we can use strings as an index.

Strings as an index

```
data=pd.Series([0.25,0.5, 0.75,1.0],
index=['a', 'b', 'c',
'd'])data
```

a 0.25

b 0.50

c 0.75

d 1.00

dtype:float64

Noncontiguous or non sequential indices.

```
data=pd.Series([0.25,0.5, 0.75,1.0],
index=[2, 5, 3,
7])data
```

20.25

50.50

30.75

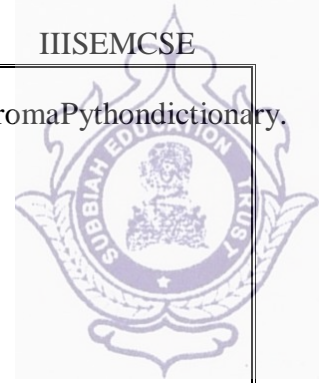
71.00

dtype:float64

Series as specialized dictionary

A dictionary is a structure that maps arbitrary keys to a set of arbitrary values, and a Series is a structure that maps typed keys to a set of typed values.

Just as the type-specific compiled code behind a NumPy array makes it more efficient than a Python list for certain operations, the type information of a Pandas Series makes it much more efficient than Python dictionaries for certain operations.



We can make the Series-as-dictionary analogy even more clear by constructing a Series object directly from a Python dictionary. For example

```
sub1={'sai':90,'ram':85,'kasim':92,'tamil':89}
mark=pd.Series(sub1)
mark

sai      90
ram      85
kasim    92
tamil    89
dtype: int64
```

Dictionary-style item access

```
Mark['ram']
85
```

Array-style slicing

```
Mark['sai':'kasim']
sai      90
ram      85
kasim    92
```

Constructing Series objects

- **List or NumPy array**

```
pd.Series([2, 4, 6])
```

```
0 2
1 4
2 6
dtype: int64
```

- **Repeated to fill the specified index**

```
pd.Series(5, index=[100, 200, 300])
```

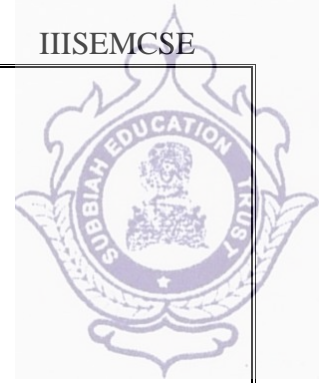
```
100 5
200 5
300 5
dtype: int64
```

- **Data can be a dictionary, in which index defaults to the sorted dictionary keys**

```
pd.Series({'2':'a', '1':'b', '3':'c'})
```

```
1 b
2 a
3 c
dtype: object
```

- **The index can be explicitly set if a different result is preferred**



```
pd.Series({'2':'a',1:'b',3:'c'},index=[3,2])
```

```
3c
```

```
2a
```

```
dtype:object
```

ThePandasDataFrameObject

The fundamental structure in Pandas is the DataFrame. The DataFrame can be thought of either as a generalization of a NumPy array, or as a specialization of a Python dictionary.

DataFrames as a generalized NumPy array

A DataFrame is an analog of a two-dimensional array with both flexible row indices and flexible column names. Just as you might think of a two-dimensional array as an ordered sequence of aligned one-dimensional columns, you can think of a DataFrame as a sequence of aligned Series objects. Here, by “aligned” we mean that they share the same index.

To demonstrate this, let's first construct a new Series listing the marks of subject 2.

```
sub2={'sai':91,'ram':95,'kasim':89,'tamil':90}
```

We can use a dictionary to construct a single two-dimensional object containing this information.

```
result=pd.DataFrame({'DS':sub1,'FDS':sub2})
```

```
result
```

	DS	FDS
sai	90	91
ram	85	95
kasim	92	89
tamil	89	90

DataFrame has an index attribute

Like the Series object, the DataFrame has an index attribute that gives access to the index labels

```
result.index
```

```
Index(['sai', 'ram', 'kasim', 'tamil'], dtype='object')
```

DataFrame has a columns attribute.

The DataFrame has a columns attribute, which is an Index object holding the column labels.

```
result.columns
```

```
Index(['DS', 'FDS'], dtype='object')
```

DataFrame as a specialized dictionary

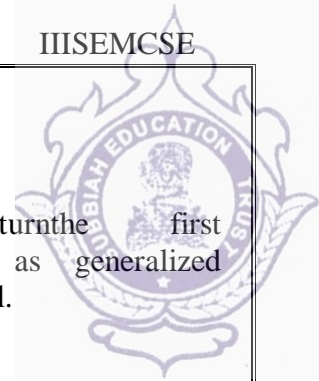
We can also think of a DataFrame as a specialization of a dictionary. Where a dictionary maps a key to a value, a DataFrame maps a column name to a Series of column data.

```
result['DS']
```

```
sai 90
```

```
ram 85
```

```
kasim 92
```



```
tamil89
Name: DS, dtype: int64
```

Note

In a two-dimensional NumPy array, `data[0]` will return the first row. For a DataFrame, `data['col0']` will return the first column. Because of this, it is probably better to think about DataFrames as generalized dictionaries rather than generalized arrays, though both ways of looking at the situation can be useful.

Constructing DataFrame objects

A Pandas DataFrame can be constructed in a variety of ways. Here we'll give several examples.

- **From a single Series object.**
- **From a list of dicts.**
- **From a dictionary of Series objects.**
- **From a two-dimensional NumPy array.**
- **From a NumPy structured array.**

From a single Series object.

A DataFrame is a collection of Series objects, and a single column DataFrame can be constructed from a single Series.

```
sub1 = pd.Series({'sai': 90, 'ram': 85, 'kasim': 92, 'tamil': 89})
pd.DataFrame(sub1, columns=['DS'])
```

	DS
sai	90
ram	85
kasim	92
tamil	89

From a list of dicts.

Any list of dictionaries can be made into a DataFrame. We'll use a simple list comprehension to create some data

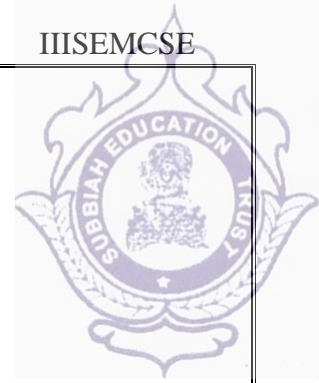
```
data = [{'a': i, 'b': 2 * i} for i in range(3)]
pd.DataFrame(data)
```

a	b
0	0
1	2
2	4

Even if some keys in the dictionary are missing, Pandas will fill them in with NaN (i.e., "not a number") values.

```
pd.DataFrame([{'a': 1, 'b': 2}, {'b': 3, 'c': 4}])
a      b      c
0  1.0  2.0  NaN
1  NaN  3.0  4.0
```

From a dictionary of Series objects.



As we saw before, a DataFrame can be constructed from a dictionary of Series objects as well.

```
pd.DataFrame({'DS':sub1,'FDS':sub2})
```

	DS	FDS
sai	90	91
ram	85	95
kasim	92	89
tamil	89	90

From a two-dimensional NumPy array.

Given a two-dimensional array of data, we can create a DataFrame with any specified column and index names. If omitted, an integer index will be used for each.

```
pd.DataFrame(np.random.rand(3,2), columns=['food', 'water'], index=['a', 'b', 'c'])
```

	food	water
a	0.8652570	0.213169
b	0.4427590	0.108267
c	0.0471100	0.905718

From a NumPy structured array.

A Pandas DataFrame operates much like a structured array, and can be created directly.

```
A = np.zeros(3, dtype=[('A', 'i8'), ('B', 'f8')])A
```

```
array([(0,0.0),(0,0.0),(0,0.0)], dtype=[('A', '<i8'), ('B', '<f8')])
```

```
pd.DataFrame(A)
```

	A	B
0	000.0	100.0
1	100.0	200.0

The Pandas Index Object

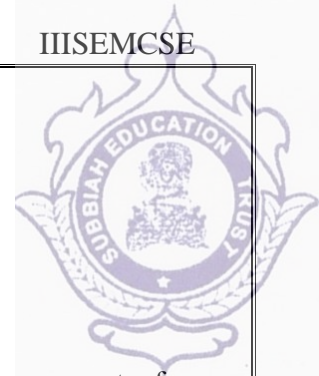
We have seen here that both the Series and DataFrame objects contain an explicit index that lets you reference and modify data. This Index object is an interesting structure in itself, and it can be thought of either as an immutable array or as an ordered set.

```
ind = pd.Index([2, 3, 5, 7, 11])ind
```

```
Int64Index([2,3,5,7,11], dtype='int64')
```

- **Index as an immutable array**

The Index object in many ways operates like an array. For example, we can use standard Python indexing notation to retrieve values or slices.



```
ind[1]
3
ind[:2]
Int64Index([2,5,11],dtype='int64')
```

- **Indexasorderedset**

Pandasobjectsaredesignedtofacilitateoperationssuchasjoinsacrossdatasets,whichdependonmanyaspectsof setarithmetic.

TheIndexobjectfollowsmanyoftheconventionsusedbyPython’sbuilt-insetdatastructure,sothatunions,intersections,differences,and other combinationscan becomputedin afamiliar way.

```
indA=pd.Index([1,3,5,7,9])
indB = pd.Index([2, 3, 5, 7,
11])indA&indB#intersection
```

```
Int64Index([3, 5, 7],
```

```
dtype='int64')indA|indB#union
Int64Index([1,2,3,5,7,9, 11],dtype='int64')
```

```
indA^ indB#symmetricdifference
Int64Index([1,2,9,11],dtype='int64')
```

DataIndexingandSelection

DataSelectioninSeries

ASeriesobjectactsinmanywayslikeaonedimensionalNumPyarray,andinmanywayslikeastandardPythondictionary.It willhelpstounderstandthepatternsofdata indexingandselectioninthese arrays.

- Seriesasdictionary
- Seriesasone-dimensionalarray
- Indexers:loc,iloc, andix

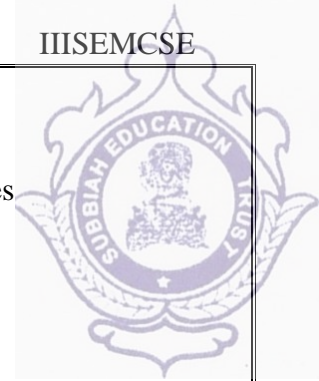
- **Seriesasdictionary**

Likeadictionary,theSeriesobjectprovidesamappingfromacollectionofkeystoacollectionofvalues.

```
data=pd.Series([0.25,0.5, 0.75,1.0],
index=['a', 'b', 'c',
'd'])data
```

```
a 0.25
b0.50
c 0.75
d1.00
dtype:float64
```

```
data['b']
```



0.5

Examine the keys/indices and values

We can also use dictionary-like Python expressions and methods to examine the keys/indices and values

i. `data['a']`

True

ii. `data.keys()`

Index(['a', 'b', 'c', 'd'], dtype='object')

iii. `list(data.items())`

[('a', 0.25), ('b', 0.5), ('c', 0.75), ('d', 1.0)]

Modifying series object

Series objects can even be modified with a dictionary-like syntax. Just as you can extend a dictionary by assigning to a new key, you can extend a Series by assigning to a new index value.

```
data['e'] =
1.25
```

```
a 0.25
b 0.50
c 0.75
d 1.00
e 1.25
dtype: float64
```

- **Series as one-dimensional array**

A Series builds on this dictionary-like interface and provides array-style item selection via the same basic mechanisms as NumPy arrays—that is, slices, masking, and fancy indexing.

Slicing by explicit index

```
data['a':'c']
```

```
a 0.25
b 0.50
c 0.75
dtype: float64
```

Slicing by implicit integer index

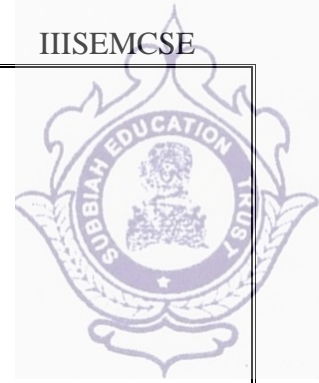
```
data[0:2]
```

```
a 0.25
b 0.50
dtype: float64
```

Masking

```
data[(data > 0.3) & (data < 0.8)]
```

```
b 0.50
c 0.75
```



dtype:float64

Fancy indexing

```
data[['a','e']]
```

a 0.25

e 1.25

dtype:float64

- **Indexers: loc, iloc, and ix**

Pandas provides some special indexer attributes that explicitly expose certain indexing schemes. These are not functional methods, but attributes that expose a particular slicing interface to the data in the Series.

```
data = pd.Series(['a', 'b', 'c'], index=[1, 3, 5])
data
```

1a

3b

5c

dtype:object

loc-the loc attribute allows indexing and slicing that always reference the explicit index.

```
data.loc[1]
```

'a'

```
data.loc[1:3]
```

1a

3b

dtype:object

iloc-The iloc attribute allows indexing and slicing that always reference the implicit Python-style index.

```
data.iloc[1]
```

'b'

```
data.iloc[1:3]
```

3b

5c

dtype:object

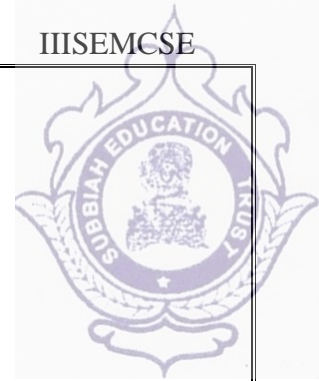
ix-ix is a hybrid of the two, and for Series objects is equivalent to standard []-based indexing.

Data Selection in DataFrame

- DataFrame as a dictionary
- DataFrame as a two-dimensional array
- Additional indexing conventions

DataFrame as a dictionary

The first analogy we will consider is the DataFrame as a dictionary of related Series objects.



The individual Series that make up the columns of the DataFrame can be accessed via dictionary-style indexing of the column name.

Dictionary-style indexing of the column

```
name.result=pd.DataFrame({'DS':sub1,'FDS':sub2})result['DS']
```

	DS
sai	90
ram	85
kasim	92
tamil	89

Attribute-style access with column names that are strings

```
result.DS
```

	DS
sai	90
ram	85
kasim	92
tamil	89

Comparing attribute style and dictionary style accesses

```
result.DS is result['DS']
```

True

Modify the object

Like with the Series objects this dictionary-style syntax can also be used to modify the object, in this case to add a new column:

```
result['TOTAL']=result['DS']+result['FDS']result
```

	DS	FDS	TOTAL
sai	90	91	181
ram	85	95	180
kasim	92	89	181
tamil	89	90	179

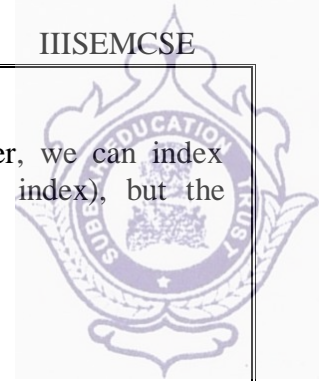
DataFrame as two-dimensional array

- **Transpose**

We can transpose the full DataFrame to swap rows and columns.

```
result.T
```

	sai	ram	kasim	tamil
DS	90	85	92	89
FDS	91	95	89	90
TOTAL	181	180	181	179



Pandas again uses the loc, iloc, and ix indexers mentioned earlier. Using the iloc indexer, we can index the underlying array as if it is a simple NumPy array (using the implicit Python-style index), but the DataFrame index and column labels are maintained in the result

- **loc**

```
result.loc[:'ram',:'FDS']
```

	DS	FDS
sai	90	91
ram	85	95

- **iloc**

```
result.iloc[:2,:2]
```

	DS	FDS
sai	90	91
ram	85	95

- **ix**

```
result.ix[:2,:'FDS']
```

	DS	FDS
sai	90	91
ram	85	95

- **Masking and Fancy indexing**

In the loc indexer we can combine masking and fancy indexing as in the following:

```
result.loc[result.total>180,['DS','FDS']]
```

	DS	FDS
sai	90	91
kasim92	89	

- **Modifying values**

Indexing conventions may also be used to set or modify values; this is done in the standard way that you might be accustomed to from working with NumPy.

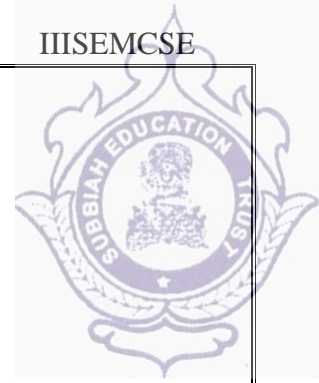
```
result.iloc[1,1]=70
```

	DS	FDS	TOTAL
sai	90	91	181
ram	85	70	180
kasim 92	89	181	
tamil 89	90	179	

Additional indexing

conventions Slicing rowwise

```
result['sai':'kasim']
```



	DS	FDS	TOTAL
sai	90	91	181
ram	85	70	180
kasim 92	89	181	

Such slices can also refer to rows by number rather than by index:

```
result[1:3]
```

	DS	FDS	TOTAL
ram	85	70	180
kasim92	89	181	

Masking row wise

```
result[result.total>180]
```

	DS	FDS	TOTAL
sai	90	91	181
kasim92	89	181	

Operating on Data in Pandas

Pandas inherits much of this functionality from NumPy, and the ufuncs. So Pandas having the ability to perform quick element-wise operations, both with basic arithmetic (addition, subtraction, multiplication, etc.) and with more sophisticated operations (trigonometric functions, exponential and logarithmic functions, etc.).

For unary operations like negation and trigonometric functions, these ufuncs will preserve index and column labels in the output.

For binary operations such as addition and multiplication, Pandas will automatically align indices when passing the objects to the ufunc.

Here we are going to see how the universal functions are working in series and DataFrames by

- **Index preservation**
- **Index alignment**

Index Preservation

Pandas is designed to work with NumPy, any NumPy ufunc will work on Pandas Series and DataFrame objects. We can use all arithmetic and special universal functions as in NumPy on pandas. In outputs the index will be preserved (maintained) as shown below.

For series

```
x=pd.Series([1,2,3,4])
```

```
x
```

```
0 1
```

```
1 2
```

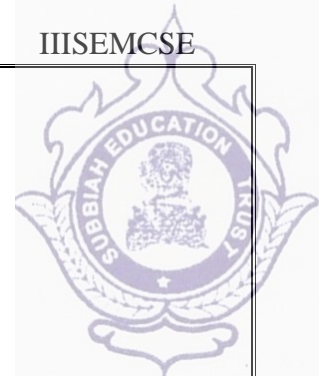
```
2 3
```

```
3 4
```

```
dtype: int64
```

For DataFrame

```
df=pd.DataFrame(np.random.randint(0,10,(3,4)),
                 columns=['a','b','c','d'])
```



df	a	b	c	d
0	1	4	1	4
1	8	4	0	4
2	7	7	7	2

For universal function. (here we use exponent as example)

Ufuncs for series

`np.exp(series)`

```
0 8103.083928
1 154.598150
2 2403.428793
dtype: float64
```

Ufuncs for DataFrame

`np.exp(df)`

	a	b	c	d
0	2.718282	54.598150	2.718282	54.598150
1	2980.957987	54.598150	1.000000	54.598150
2	1096.633158	1096.633158	1096.633158	7.389056

Index Alignment

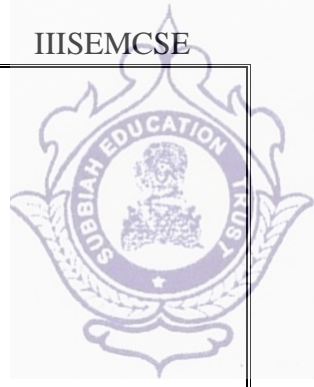
Pandas will align indices in the process of performing the operation. This is very convenient when you are working with incomplete data, as we'll.

Index alignment in Series

Suppose we are combining two different data sources, then the index will be aligned accordingly.

```
x = pd.Series([2,4,6], index=[1,3,5])
y = pd.Series([1,3,5,7], index=[1,2,3,4])
x+y
```

```
13.0
2
NaN 3
.0
4 NaN
5 NaN
dtype: float64
```



The resulting array contains the union of indices of the two input arrays, which we could determine using standard Python set arithmetic on these indices.

Any item for which one or the other does not have an entry is marked with NaN, or “Not a Number,” which is what Pandas marks as missing data.

Fill value in missing data (fill_value)

If using NaN values is not the desired behavior, we can modify the fill value using appropriate object methods in place of the operators.

```
x.add(y, fill_value=0)
```

```
13.0
23.0
39.0
47.0
56.0
dtype: float64
```

Index alignment in DataFrame

A similar type of alignment takes place for both columns and indices when you are performing operations on DataFrames.

```
A = pd.DataFrame(rng.randint(0, 20, (2, 2)), columns=list('AB'))
```

```
A
  AB
0  1  1
1  1  1
```

```
B = pd.DataFrame(rng.randint(0, 10, (3, 3)), columns=list('BAC'))
```

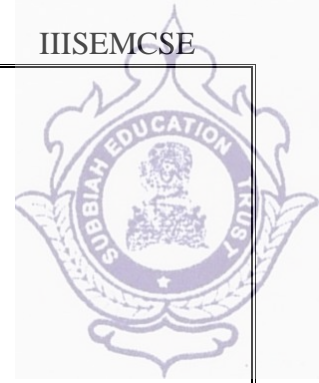
```
B
```

```
  B A
0  4  9
1  5  0
2  6  2
```

```
A+B
```

```
  A B C
0  1  0  5  NaN
1  1  3  6  0
2  NaN  2  NaN  NaN
```

Notice that indices are aligned correctly irrespective of their order in the two objects, and indices in the result are sorted. As was the case with Series, we can use the associated object’s arithmetic method and pass any desired fill_value to be used in place of missing entries. Here we’ll fill with the mean of all values in A.



```
fill =
A.stack().mean()A.add
(B,fill_value=fill)
```

```
  A B C
0 1.015.0 13.5
113.06.04.5
2 6.513.5 10.5
```

Mapping between Python operators and Pandas methods.
Python operator Pandas method(s)

```
+           add()
-           sub(),subtract()
*           mul(),multiply()
/           truediv(),div(),divide()
//          floordiv()
%           mod()
**          pow()
```

Operations between Data Frame and Series

When you are performing operations between a DataFrame and a Series, the index and column alignment is similarly maintained. Operations between a DataFrame and a Series are similar to operations between a two-dimensional and one-dimensional NumPy array.

```
A = rng.randint(10, size=(3,
4))A
array([[3,8, 2, 4],
[2, 6,4, 8],
[6, 1,3,8]])
```

```
A - A[0]
array([[ 0,0,0,0],
[-1,-2,2,4],
[3,-7,1,4]])
```

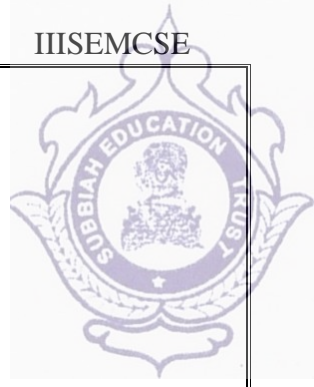
Handling Missing Data

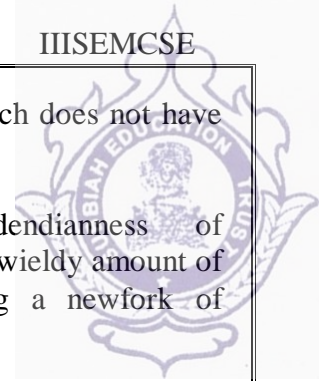
A number of schemes have been developed to indicate the presence of missing data in a table or DataFrame. Generally, they revolve around one of two strategies: using a **mask** that globally indicates missing values, or choosing a **sentinel value** that indicates a missing entry.

In the masking approach, the mask might be an entirely separate Boolean array, or it may involve appropriation of one bit in the data representation to locally indicate the null status of a value.

In the sentinel approach, the sentinel value could be some data-specific convention, such as indicating a missing integer value with -9999 or some rare bit pattern, or it could be a more global convention, such as indicating a missing floating-point value with NaN (Not a Number), a special value which is part of the IEEE floating-point specification.

Missing Data in Pandas





The way in which Pandas handles missing values is constrained by its NumPy package, which does not have a built-in notion of NA values for nonfloating-point datatypes.

NumPy supports fourteen basic integer types once you account for available precisions, signedness, and endianness of the encoding. Reserving a specific bit pattern in all available NumPy types would lead to an unwieldy amount of overhead in special-casing various operations for various types, likely even requiring a new fork of the NumPy package.

Pandas chose to use sentinels for missing data, and further chose to use two already-existing Python null values: the special floating-point NaN value, and the Python None object. This choice has some side effects, as we will see, but in practice ends up being a good compromise in most cases of interest.

None: Pythonic missing data

The first sentinel value used by Pandas is None, a Python singleton object that is often used for missing data in Python code. Because None is a Python object, it cannot be used in any arbitrary NumPy/Pandas array, but only in arrays with datatype 'object' (i.e., arrays of Python objects)

This dtype=object means that the best common type representation NumPy could infer for the contents of the array is that they are Python objects.

NaN: Missing numerical data

NaN is a special floating-point value recognized by all systems that use the standard IEEE floating-point representation.

```
vals2 = np.array([1, np.nan, 3,
4])vals2.dtype
```

```
dtype('float64')
```

You should be aware that NaN is a bit like a data virus—it infects any other object it touches. Regardless of the operation, the result of arithmetic with NaN will be another NaN

```
1 +
```

```
np.nan
```

```
0 * np.nan
```

```
Nan
```

NaN and None in Pandas

NaN and None both have their place, and Pandas is built to handle the two of them nearly interchangeably.

```
pd.Series([1, np.nan, 2,
None])
```

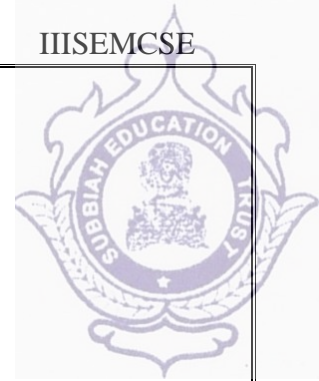
```
1 NaN
```

```
2 2.0
```

```
3 NaN
```

```
dtype: float64
```

For types that don't have an available sentinel value, Pandas automatically type-casts when NA values are present. For example, if we set a value in an integer array to np.nan, it will automatically be upcast to a floating-point type to accommodate the NA



```
x = pd.Series(range(2),
dtype=int)x
00
11
dtype:
int64x[0] =
Nonex
ONaN
11.0
dtype:float64
```

Noticethatinadditionto castingtheinteger arraytofloatingpoint,Pandasautomaticallyconvertsthe None toaNaNvalue.

PandashandlingofNAsbytype

Typeclass	ConversionwhenstoringNAs	NAsentinelvalue
floating	Nochange	np.nan
object	Nochange	Noneornp.nan
integer	Casttofloat64	np.nan
boolean	Casttoobject	Noneornp.nan

Note:InPandas,stringdata isalwaysstored withanobjectdtype.

OperatingonNullValues

thereareseveralusefulmethodsfordetecting,removing, andreplacingnullvalues inPandasdatastructures.Theyare:

- isnull()-Generate aBooleanmask indicatingmissingvalues
- notnull()-Oppositeof isnull()
- dropna()-Returna filteredversion ofthedata
- fillna()-Returnacopyof thedata with missingvalues filled orimputed

Detectingnullvalues

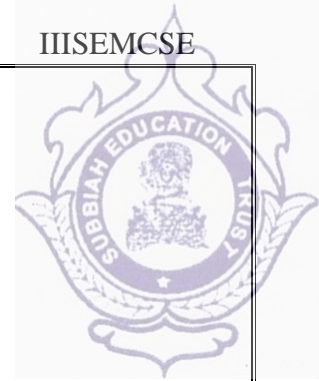
Pandasdatastructureshavetwo usefulmethodsfordetectingnulldata:isnull()andnotnull().isnull()

```
data = pd.Series([1, np.nan, 'hello',
None])data.isnull()
```

```
0 False
1 True
2 False
3 Truedtyp
e:bool
```

```
notnull()
data.notnull()
```

```
0 True
1 False
2 True
```



3 Falsedtyp
e:bool

Dropping null values

dropna()
data.dropna()

01
2hellodtype:
object

Dropping null values in dataframe

```
df = pd.DataFrame([[1, np.nan,
2],[2, 3,5],
[np.nan, 4,
6]])Df
```

012
0 1.0NaN 2
1 2.03.0 5
2 NaN 4.06

df.dropna()

012
1 2.03.0 5

Drop values in column or row

We can drop NA values along a different axis; axis=1 drops all columns containing a null value.

```
df.dropna(axis='columns')
```

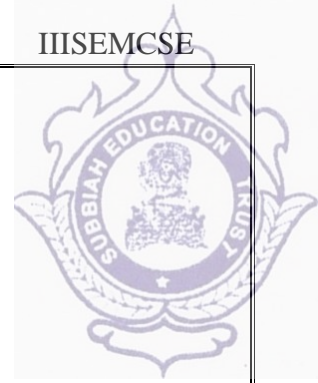
02
15
26

Rows or columns having all null values

You can also specify how='all', which will only drop rows/columns that are all null values.

```
df[3] =  
np.nan*df
```

0123
0 1.0NaN2NaN
1 2.03.05 NaN
2NaN 4.06NaN



```
df.dropna(axis='columns',how='all')
```

```
012
0 1.0NaN 2
1 2.03.0 5
2 NaN 4.06
```

Specificnoofnullvalues(thresh)

thethreshparameter letsyou specify a minimum number of non-null values for the row/column to be kept

```
df.dropna(axis='rows',thresh=3)
```

```
0123
1 2.03.05 NaN
```

Fillingnullvalues

Sometimes rather than dropping NA values, you'd rather replace them with a valid value. This value might be a single number like zero, or it might be some sort of imputation or interpolation from the good values. You could do this in-place using the `isnull()` method as a mask, but because it is such a common operation Pandas provides the `fillna()` method, which returns a copy of the array with the null values replaced.

```
data = pd.Series([1, np.nan, 2, None, 3],
index=list('abcde'))data
```

```
a 1.0
bNaN
c 2.0
dNaN
```

Fillwithsinglevalue

We can fill NA entries with a single value, such as zero

```
data.fillna(0)
```

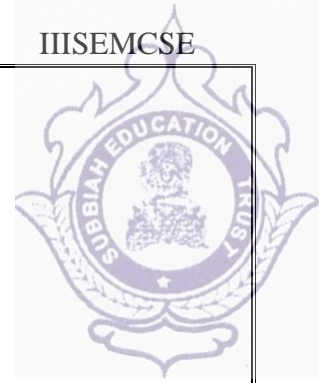
```
a 1.0
b0.0
c 2.0
d0.0
e3.0
dtype:float64
```

Fillwith previous value

We can specify a forward-fill to propagate the previous value forward

```
data.fillna(method='ffill')
```

```
a 1.0
b1.0
c 2.0
d2.0
e3.0
dtype:float64
```



Fill with next value

We can specify a back-fill to propagate the next values backward.

```
data.fillna(method='bfill')
```

```
a 1.0
b 2.0
c 2.0
d 3.0
e 3.0
dtype: float64
```

Hierarchical Indexing

Up to this point we've been focused primarily on one-dimensional and two-dimensional data, stored in Pandas Series and DataFrame objects, respectively. Often it is useful to go beyond this and store higher-dimensional data—that is, data indexed by more than one or two keys.

Pandas does provide Panel and Panel4 objects that natively handle three-dimensional and four-dimensional data, but a more common pattern in practice is to make use of hierarchical indexing (also known as multi-indexing) to incorporate multiple index levels within a single index.

In this way, higher-dimensional data can be compactly represented within the familiar one-dimensional Series and two-dimensional DataFrame objects.

Here we'll explore the direct creation of MultiIndex objects; considerations around indexing, slicing, and computing statistics across multiply indexed data; and useful routines for converting between simple and hierarchically indexed representations of your data.

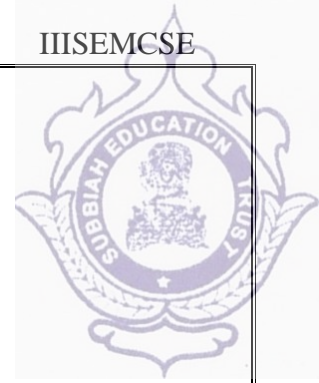
A Multiply Indexed Series

Pandas MultiIndex

Pandas provides a better way. Our tuple-based indexing is essentially a rudimentary multi-index, and the Pandas MultiIndex type gives us the type of operations we wish to have. We can create a multi-index from the tuples as follows

```
index=[('California',2000),('California',2010),
('NewYork', 2000),('NewYork', 2010),
('Texas',2000),('Texas',2010)]
populations=[33871648,37253956,
18976457,19378102,
20851820,25145561]
pop = pd.Series(populations,
index=index)pop
```

```
(California,2000)33871648
(California,2010)37253956
(NewYork,2000)18976457
(NewYork,2010)19378102
(Texas,2000)20851820
```



```
#creatingmultiindex
index =
pd.MultiIndex.from_tuples(index)index
```

```
MultiIndex(levels=[['California','NewYork','Texas'],[2000,2010]],
labels=[[0,0,1,1,2,2],[0, 1,0,1,0,1]])
```

Hierarchicalrepresentationof thedata

```
pop =
pop.reindex(index)pop

California200033871648
                201037253956
NewYork      200018976457
                201019378102
Texas 200020851820
                201025145561

dtype:int64
```

HerethefirsttwocolumnsoftheSeriesrepresentationshowthemultipleindexvalues,whilethethirdcolumnshowsthe data.

Accessalldatawithsecondindex

```
pop[:,2010]

California37253956
NewYork19378102
Texas
25145561dtype
:int64
```

MultiIndexasextradimension

wecouldeasilyhavestoredthesamedatausingasimpleDataFramewithindexandcolumnlabels.The **unstack()**methodwill quicklyconvert amultiplyindexedSeriesintoaconventionallyindexed DataFrame.

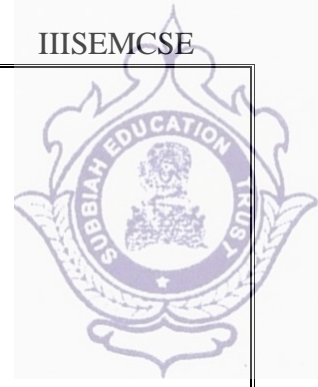
```
pop_df=pop.unstack()
pop_df

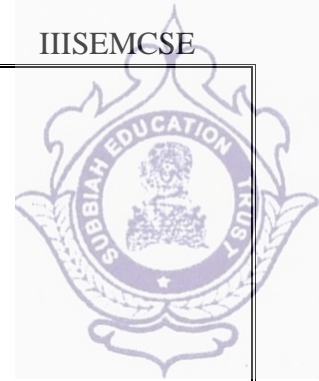
                20002010
California3387164837253956
NewYork      1897645719378102
Texas 2085182025145561
```

The**stack()**method provides theopposite operation.

```
pop_df.stack()

California200033871648
201037253956
NewYork200018976457
201019378102
Texas200020851820
```





```
201025145561
dtype:int64
```

Add a new column in multidimensional dataframe.

```
pop_df=pd.DataFrame({'total':pop,
                    'under18':[9267089,9284094,
                              4687374,4318033,
                              5906301,6879014]})
```

```
pop_df
```

	total	under18
California	2000338716489267089	2010372539569284094
NewYork	2000189764574687374	2010193781024318033
Texas	2000208518205906301	2010251455616879014

Universal functions

All the functions and other functionality work with hierarchical indices.

```
f_u18 = pop_df['under18'] /
pop_df['total']f_u18.unstack()
```

	2000	2010
California	0.273594	0.249211
NewYork	0.247010	0.222831
Texas	0.283251	0.273568

Methods of MultiIndex Creation

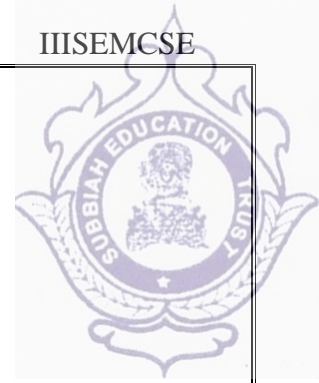
To construct a multiply indexed Series or DataFrame is to simply pass a list of two or more index arrays to the constructor.

```
df = pd.DataFrame(np.random.rand(4,
2),index=[['a', 'a', 'b', 'b'],[1,2,1,2]],
columns=['data1',
'data2'])df
```

	data1	data2
a	10.5542330	3.356072
	20.9252440	2.19474
b	10.4417590	6.10054
	20.1714950	8.86688

If you pass a dictionary with appropriate tuples as keys, Pandas will automatically recognize this and use a MultiIndex by default.

```
data={ ('California',2000):33871648,
       ('California',2010):37253956,
       ('Texas',2000):20851820,
       ('Texas',2010):25145561,
       ('NewYork',2000):18976457,
```



```

                ('NewYork',2010):19378102}
pd.Series(data)

California    200033871648
                201037253956
NewYork       200018976457
                201019378102
Texas         200020851820
                201025145561
dtype:int64
    
```

Explicit MultiIndex constructors

You can construct the MultiIndex from a simple list of arrays, giving the index values within each level.

```
pd.MultiIndex.from_arrays([[ 'a', 'a', 'b', 'b'], [1, 2, 1, 2]])
```

```
MultiIndex(levels=[[ 'a', 'b'], [1, 2]],
            labels=[[0, 0, 1, 1], [0, 1, 0, 1]])
```

Multiindex from a list of tuples,

```
pd.MultiIndex.from_tuples([('a', 1), ('a', 2), ('b', 1), ('b', 2)])
```

```
MultiIndex(levels=[[ 'a', 'b'], [1, 2]],
            labels=[[0, 0, 1, 1], [0, 1, 0, 1]])
```

Multiindex from Cartesian product.

```
pd.MultiIndex.from_product([[ 'a', 'b'], [1, 2]])
```

```
MultiIndex(levels=[[ 'a', 'b'], [1, 2]],
            labels=[[0, 0, 1, 1], [0, 1, 0, 1]])
```

MultiIndex level names

It is convenient to name the level of the MultiIndex. You can accomplish this by passing the names argument to any of the above MultiIndex constructors, or by setting the names attribute of the index after the fact.

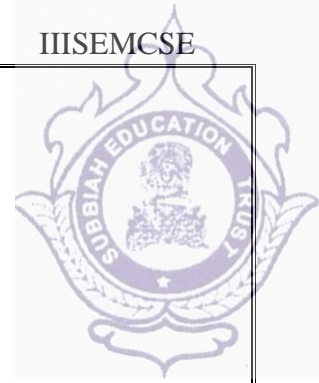
```
pop.index.names = ['state',
                  'year']pop
```

```

state    year
California  200033871648
                201037253956
NewYork    200018976457
                201019378102
Texas      200020851820
                201025145561
dtype:int64
    
```

MultiIndex for columns

In a DataFrame, the rows and columns are completely symmetric, and just as the rows can have multiple levels of indices, the columns can have multiple levels as well.



```
#hierarchicalindicesandcolumns
index = pd.MultiIndex.from_product([[2013, 2014], [1,
2]],names=['year','visit'])
columns = pd.MultiIndex.from_product([[ 'Bob', 'Guido', 'Sue'], ['HR',
'Temp']],names=['subject', 'type'])
```

```
#mocksomedata
data=np.round(np.random.randn(4,6),1)
data[:, ::2]*=10
data+=37
```

```
#createtheDataFrame
health_data = pd.DataFrame(data, index=index,
columns=columns)health_data
```

```
subject      Bob
             GuidoSue      type      HR
             Temp HR Temp HR Tempyear
visit
2013131.038.732.036.735.037.2
           2      44.037.7 50.035.029.036.7
2014130.037.439.037.861.036.9
           2      47.037.8 48.037.351.036.5
```

IndexingandSlicingaMultiIndex

IndexingandslicingonaMultiIndexisdesignedtobeintuitive,andithelpsifyouthinkabouttheindicesasaddeddimensions.We'll firstlook at indexingmultiplyindexed Series,andthen multiplyindexed DataFrames.

Multiplyindexed Series

```
Pop

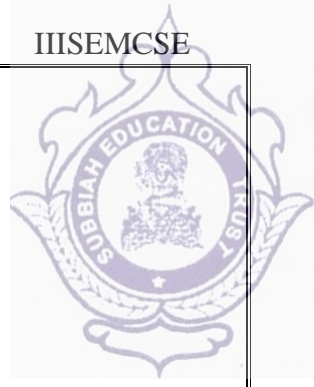
state      year
California  200033871648
           201037253956
NewYork    200018976457
           201019378102
Texas      200020851820
           201025145561

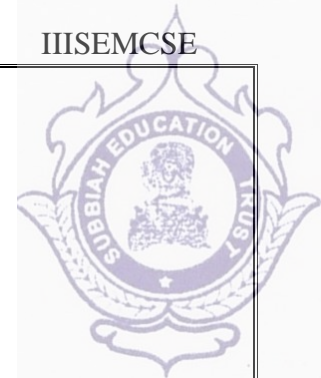
dtype:int64
```

- Accessingleelements
Wecan access singleelements byindexingwithmultiple terms
`pop['California',2000]`

33871648

- Partialindexing
TheMultiIndexalsosupports partialindexing,or indexingjustoneofthelevelsindex
`pop['California']`





```

year
200033871648
201037253956
dtype:int64
    
```

- Partial slicing
 Partial slicing is available as well, as long as the MultiIndex is sorted.
`pop.loc['California':'NewYork']`

```

state      year
California 200033871648
           201037253956
NewYork    200018976457
           201019378102
    
```

```
dtype:int64
```

- Sorted indices
 With sorted indices, we can perform partial indexing on lower levels by passing an empty slice in the first index
`pop[:,2000]`

```

state
California 33871648
NewYork    18976457
Texas      20851820
dtype:int64
    
```

- Other types of indexing and selection
 Selection based on Boolean masks
`pop[pop > 22000000]`

```

state      year
California 200033871648
           201037253956
Texas      201025145561
dtype:int64
    
```

Selection based on fancy indexing

```
pop[['California','Texas']]
```

```

state      year
California 200033871648
           201037253956
Texas      200020851820
           201025145561
    
```

```
dtype:int64
```

Rearranging Multi-Indices



We saw a brief example of this in the `stack()` and `unstack()` methods, but there are many more ways to finely control the rearrangement of data between hierarchical indices and columns, and we'll explore them here.

- **Sorted and unsorted indices**

We'll start by creating some simple multiply-indexed data where the indices are *not lexographically sorted*:

```
index = pd.MultiIndex.from_product(['a', 'c', 'b'], [1, 2])
data = pd.Series(np.random.rand(6), index=index)
data.index.names = ['char', 'int']
```

char	int	
a	1	0.003001
	2	0.164974
c	1	0.741650

Pandas provides a number of convenience routines to perform this type of sorting; examples are the `sort_index()` and `sortlevel()` methods of the `DataFrame`. We'll use the simplest, `sort_index()`, here:

```
data = data.sort_index()
```

char	int	
a	1	0.003001
	2	0.164974
b	1	0.001693
	2	0.526226
c	1	0.741650
	2	0.569264

dtype: float64

With the index sorted in this way, partial slicing will work as expected:

```
data['a':'b']
```

char	int	
a	1	0.003001
	2	0.164974
b	1	0.001693
	2	0.526226

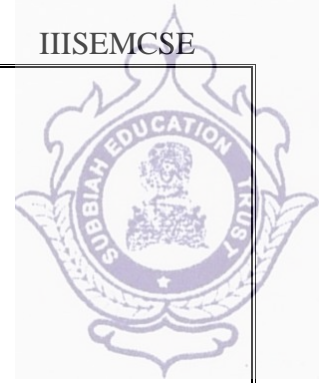
dtype: float64

- **Stacking and unstacking indices**

It is possible to convert a dataset from a stacked multi-index to a simple two-dimensional representation, optionally specifying the level to use.

```
pop.unstack(level=0)
```

state	California	New York
Texas	year	
2000	3387164818976457	20851820
2010	3725395619378102	25145561



```
pop.unstack(level=1)
```

```
year      2000  2010
state
California 3387164837253956
NewYork    1897645719378102
Texas      2085182025145561
```

The opposite of `unstack()` is `stack()`, which here can be used to recover the original series:

```
pop.unstack().stack()
```

```
stateyear
California 200033871648
           201037253956
NewYork    200018976457
           201019378102
Texas      200020851820
           201025145561
```

```
dtype:int64
```

- **Index setting and resetting**

Another way to rearrange hierarchical data is to turn the index labels into columns; this can be accomplished with the `reset_index` method. Calling this on the population dictionary will result in a DataFrame with a state and year column holding the information that was formerly in the index. For clarity, we can optionally specify the name of the data for the column representation.

```
pop_flat =
pop.reset_index(name='population')pop_flat
```

```
state  year  population
0California  200033871648
1California  201037253956
2NewYork    200018976457
3NewYork    201019378102
4 Texas      200020851820
5 Texas      201025145561
```

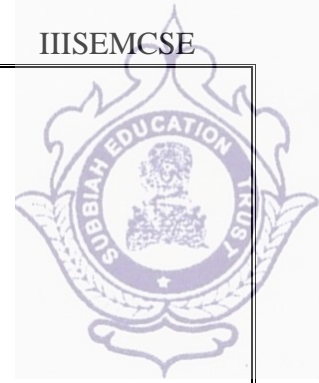
Data Aggregation on Multi-Indices

We've previously seen that Pandas has built-in data aggregation methods, such as `mean()`, `sum()`, and `max()`. For hierarchically indexed data, these can be passed a level parameter that controls which subset of the data the aggregate is computed on.

For example, let's return to our health data: (you can create your own dataframe/series)

```
health_data
```

```
subject      Bob      GuidoSue
type  HR  Temp HR  TempHR  Temp
year visit
2013131.0 38.7    32.036.7 35.037.2
      2    44.037.7    50.035.0 29.036.7
```



```
2014 130.0 37.4      39.0 37.8 61.0 36.9
      2      47.0 37.8      48.0 37.3 51.0 36.5
```

Calculate the average as follows

```
data_mean =
health_data.mean(level='year')
```

```
subject      Bob      Guido Sue
type  HRTemp      HR Temp      HR
Temp year
2013  37.5 38.2 41.0 35.8 53.2 0.36 95
2014  38.5 37.6 43.5 37.5 55.6 0.36 70
```

By further making use of the axis keyword, we can take the mean among levels on the columns as well:

```
data_mean.mean(axis=1,
level='type')
type      HR      Temp
year
2013  36.8 33 33 33 37.0 000000
2014  46.0 000000 37.2 83 33 33
```

Combining Datasets

Concat and Append

Simple Concatenation with pd.concat

Pandas has a function, `pd.concat()`, which has a similar syntax

to `np.concatenate` but contains a number of options that we'll discuss momentarily

`pd.concat()` can be used for a simple concatenation of Series or DataFrame objects, just as `np.concatenate()` can be used for simple concatenations of arrays

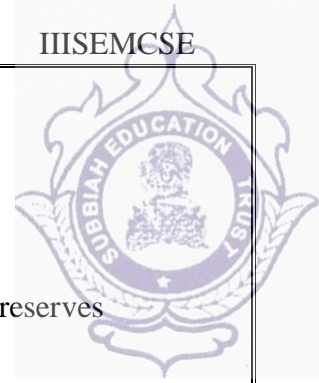
```
ser1 = pd.Series(['A', 'B', 'C'], index=[1, 2, 3])
ser2 = pd.Series(['D', 'E', 'F'], index=[4, 5,
6])
pd.concat([ser1, ser2])
```

```
1 A
2 B
3 C
4 D
5 E
6 F
dtype: object
```

Concatenation in dataframe.

```
df1 = make_df('AB', [1, 2])
df2 = make_df('AB', [3, 4])
print(df1); print(df2); print(pd.concat([df1, df2]))
```

```
df3      df4      pd.concat([df3, df4], axis='col')
```



```
AB CD ABCD
0 A0B00C0D0 0A0B0C0D0
1 A1B11C1D1 1A1B1C1D1
```

Duplicate indices

One important difference between `np.concatenate` and `pd.concat` is that Pandas concatenation preserves indices, even if the result will have duplicate indices! Consider this simple example.

```
x=make_df('AB',[0,1])
y= make_df('AB',[2,3])

y.index=x.index#makeduplicateindices!
print(x);print(y);print(pd.concat([x,y]))

x          y          pd.concat([x,y])
AB  AB  AB
0 A0B00A2 B20      A0 B0
1 A1B11A3 B31      A1 B1
0 A2B2
1 A3B3
```

The `append()` method

Series and DataFrame objects have an `append` method that can accomplish the same thing in fewer keystrokes. For example, rather than calling `pd.concat([df1, df2])`, you can simply call `df1.append(df2)`:

```
print(df1); print(df2);
print(df1.append(df2))df1    df2
df1.append(df2)
AB  AB  AB
1 A1B1 3A3B31A1B1
2 A2B2 4A4B42A2B2
3 A3B3
4 A4B4
```

Merge and Join

One essential feature offered by Pandas is its high-performance, in-memory join and merge operations.

Categories of Joins

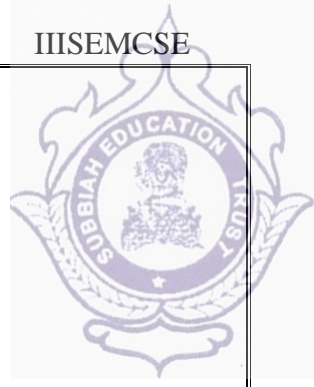
- One-to-one joins
- Many-to-one joins
- Many-to-many joins

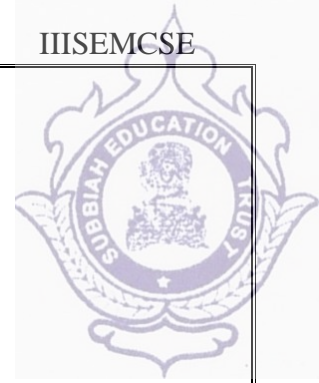
One-to-one joins

The simplest type of merge expression is the one-to-one join, which is in many ways very similar to the column-wise concatenation.

```
df1=pd.DataFrame({'employee':['Bob','Jake','Lisa','Sue'],
'group':['Accounting','Engineering','Engineering','HR']})

df2 = pd.DataFrame({'employee': ['Lisa', 'Bob', 'Jake',
'Sue'],'hire_date':[2004,2008,2012,2014]})
```





```
print(df1);print(df2)
```

df1	employee	group	df2	employee	hire_date
0	Bob	Accounting	0	Lisa	2004
1	Jake	Engineering	1	Bob	2008
2	Lisa	Engineering	2	Jake	2012
3	Sue	HR	3	Sue	2014

To combine this information into a single DataFrame, we can use the `pd.merge()` function

```
df3 = pd.merge(df1, df2)
```

	employee	group	hire_date
0	Bob	Accounting	2008
1	Jake	Engineering	2012
2	Lisa	Engineering	2004
3	Sue	HR	2014

Many-to-one joins

Many-to-one joins are joins in which one of the two key columns contains duplicate entries. For the many-to-one case, the resulting DataFrame will preserve those duplicate entries as appropriate.

```
df4 = pd.DataFrame({'group': ['Accounting', 'Engineering', 'HR'],
                    'supervisor': ['Carly', 'Guido', 'Steve']})
pd.merge(df3, df4)
```

	employee	group	hire_date	supervisor
0	Bob	Accounting	2008	Carly
1	Jake	Engineering	2012	Guido
2	Lisa	Engineering	2004	Guido
3	Sue	HR	2014	Steve

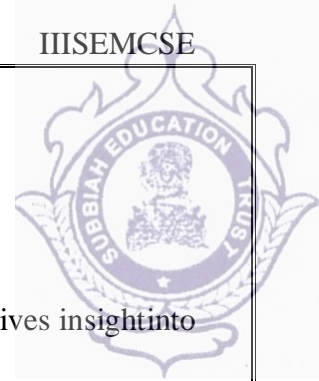
The resulting DataFrame has an additional column with the “supervisor” information, where the information is repeated in one or more locations as required by the inputs.

Many-to-many joins

Many-to-many joins are a bit confusing conceptually, but are nevertheless well defined. If the key column in both the left and right array contains duplicates, then the result is a many-to-many merge. This will be perhaps most clear with a concrete example.

```
df5 = pd.DataFrame({'group': ['Accounting', 'Accounting', 'Engineering', 'Engineering', 'HR', 'HR'],
                    'skills': ['math', 'spreadsheets', 'coding', 'linux', 'spreadsheets', 'organization']})
pd.merge(df1, df5)
```

	employee	group	skills
0	Bob	Accounting	math
1	Bob	Accounting	spreadsheets
2	Jake	Engineering	coding
3	Jake	Engineering	linux
4	Lisa	Engineering	coding



5	Lisa	Engineering	linux	
6	Sue	HR		spreadsheets
7	Sue	HR		organization

Aggregation and Grouping

Computing aggregations like `sum()`, `mean()`, `median()`, `min()`, and `max()`, in which a single number gives insight into the nature of a potentially large dataset.

Simple Aggregation in Pandas

As with a one-dimensional NumPy array, for a Pandas Series the aggregates return a single value.

```
rng =
np.random.RandomState(42)ser
= pd.Series(rng.rand(5))
ser
```

```
00.374540
10.950714
20.731994
30.598658
40.156019
dtype: float64
```

Sum

```
ser.sum()2.81192549
17081569
```

Mean

```
ser.mean()0.56238509
834163142
```

These same operations also performed in DataFrame

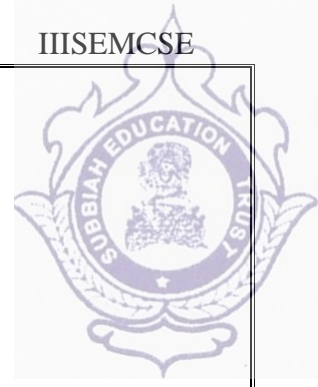
Listing of Pandas aggregation methods

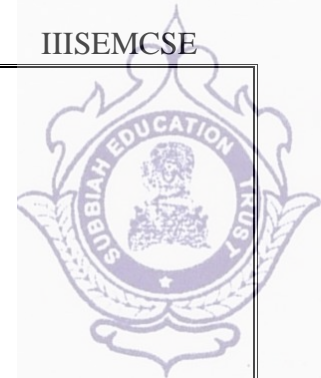
Aggregation	Description
<code>count()</code>	Total number of items
<code>first()</code> , <code>last()</code>	First and last item
<code>mean()</code> , <code>median()</code>	Mean and median
<code>min()</code> , <code>max()</code>	Minimum and maximum
<code>std()</code> , <code>var()</code>	Standard deviation and variance
<code>mad()</code>	Mean absolute deviation
<code>prod()</code>	Product of all items
<code>sum()</code>	Sum of all items

GroupBy: Split, Apply, Combine

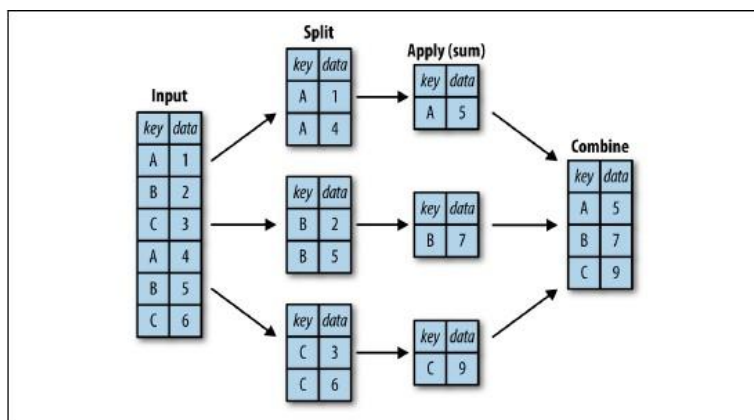
Simple aggregations can give you a flavor of your dataset, but often we would prefer to aggregate conditionally on some label or index: this is implemented in the so-called groupby operation. The name “group by” comes from a command in the SQL database language, but it is perhaps more illuminative to think of it in the terms first coined by Hadley Wickham of Rstats fame: split, apply, combine.

- The split step involves breaking up and grouping a DataFrame depending on the value of the specified key.
- The apply step involves computing some function, usually an aggregate, transformation, or filtering, within the individual groups.





- The combine step merges the results of these operations into an output array.



Example

```
df=pd.DataFrame({'key':['A','B','C','A','B','C'],
                 'data':range(6)},columns=['key','data'])
```

Df

	key	data
0	A	0
1	B	1
2	C	2
3	A	3
4	B	4
5	C	5

The GroupBy object

The GroupBy object is a very flexible abstraction. The most important operations made available by a GroupBy are aggregate, filter, transform, and apply.

GroupBy supports the basic operations like.

- Column indexing.
- Iteration over groups.
- Dispatch methods.
- Aggregate, filter, transform, apply

Column indexing.

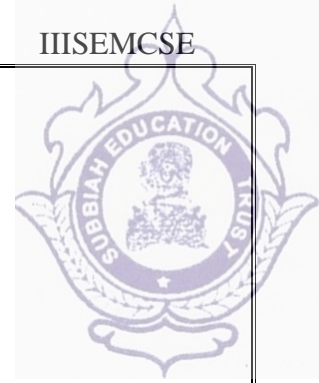
The GroupBy object supports column indexing in the same way as the DataFrame, and returns a modified GroupBy object. For example

```
df=pd.read_csv('D:\iris.csv')df.groupby('variety')
```

```
<pandas.core.groupby.generic.DataFrameGroupBy object at 0x0000023BAADE84C0>
```

```
df.groupby('variety')['petal.length']
```

```
<pandas.core.groupby.generic.SeriesGroupBy object at 0x0000023BAADE8490>
```



```
df.groupby('variety')['petal.length'].sum()
```

```
varietySetosa73.1
Versicolor    213.0
Virginica     277.6
Name:petal.length,dtype:float64
```

Iteration over groups.

The GroupBy object supports direct iteration over the groups, returning each group as a Series or DataFrame.

This can be useful for doing certain things manually, though it is often much faster to use the built-in apply functionality, which we will discuss momentarily.

Dispatch methods.

Through some Python class magic, any method not explicitly implemented by the GroupBy object will be passed through and called on the groups, whether they are DataFrame or Series objects. For example, you can use the describe() method of DataFrames to perform a set of aggregations that describe each group in the data.

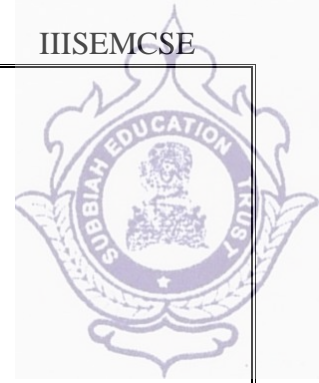
Example

```
df.groupby('variety')['petal.length'].describe().unstack()
```

```
variety
count   Setosa    50.000000
        Versicolor 50.000000
        Virginica  50.000000
mean    Setosa    1.462000
        Versicolor 4.260000
        Virginica  5.552000
std     Setosa    0.173664
        Versicolor 0.469911
        Virginica  0.551895
min     Setosa    1.000000
        Versicolor 3.000000
        Virginica  4.500000
25%     Setosa    1.400000
        Versicolor 4.000000
        Virginica  5.100000
50%     Setosa    1.500000
        Versicolor 4.350000
        Virginica  5.550000
75%     Setosa    1.575000
        Versicolor 4.600000
        Virginica  5.875000
max     Setosa    1.900000
        Versicolor 5.100000
        Virginica  6.900000
dtype: float64
```

Aggregate, filter, transform, and apply

```
rng=np.random.RandomState(0)
df=pd.DataFrame({'key':['A','B','C','A','B','C'],
```



```
'data1':range(6),
'data2':rng.randint(0,10,6)},
columns = ['key', 'data1',
'data2'])df
```

	key	data1	data2
0	A	0	5
1	B	1	0
2	C	2	3
3	A	3	3
4	B	4	7
5	C	5	9

Aggregation.

We're now familiar with GroupBy aggregations with sum(), median(), and the like, but the aggregate() method allows for even more flexibility. It can take a string, a function, or a list thereof, and compute all the aggregates at once. Here is a quick example combining all these:

```
df.groupby('key').aggregate(['min', np.median,
max])
```

	min	median	max	min	median	max
key						
A	0	1.5	3	3	4.0	5
B	1	2.5	4	0	3.5	7
C	2	3.5	5	3	6.0	9

Filtering.

A filtering operation allows you to drop data based on the group properties. For example, we might want to keep all groups in which the standard deviation is larger than some critical value.

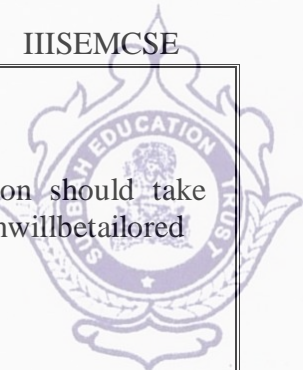
The filter() function should return a Boolean value specifying whether the group passes the filtering.

Transformation.

While aggregation must return a reduced version of the data, transformation can return some transformed version of the full data to recombine. For such a transformation, the output is the same shape as the input. A common example is to center the data by subtracting the group-wise mean:

```
df.groupby('key').transform(lambda x: x-x.mean())
```

	data1	data2
0	-1.5	1.0
1	-1.5	-3.5
2	-1.5	-3.0
3	1.5	-1.0
4	1.5	3.5
5	1.5	3.0



The apply() method.

The apply() method lets you apply an arbitrary function to the group results. The function should take a DataFrame, and return either a Pandas object (e.g., DataFrame, Series) or a scalar; the combine operation will be tailored to the type of output returned.

Pivot Tables

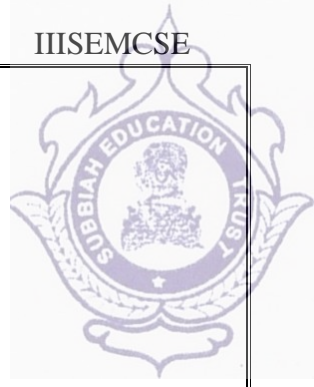
A pivot table is a similar operation that is commonly seen in spreadsheets and other programs that operate on tabular data. The pivot table takes simple column wise data as input, and groups the entries into a two-dimensional table that provides a multidimensional summarization of the data. The difference between pivot tables and GroupBy can sometimes cause confusion; it helps me to think of pivot tables as essentially a multidimensional version of GroupBy aggregation. That is, you split apply- combine, but both the split and the combine happen across not a one-dimensional index, but across a two-dimensional grid.

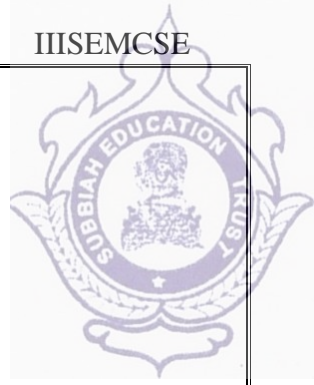
Pivot Table Creation

```
import numpy as np
import pandas as pd
df = pd.read_csv('D:\diabetes.csv')
df.pivot_table('preg', index='age', columns='Class').sample(10)
```

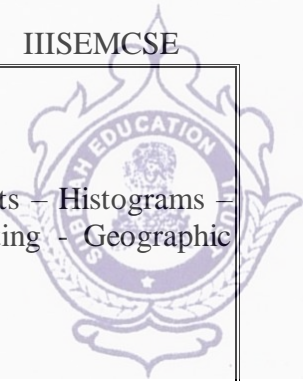
here diabetes data set has large no of rows so we use sample()

Class	tested_negative	tested_positive
age		
63	5.500000	NaN
28	3.440000	2.000000
61	7.000000	4.000000
69	5.000000	NaN
45	7.285714	7.375000
62	6.500000	1.000000
53	2.000000	6.250000
68	8.000000	NaN
23	1.516129	1.857143





Class	tested_negative	tested_positive
age		
52	13.000000	3.428571



UNIT V DATA VISUALIZATION

Importing Matplotlib – Line plots – Scatter plots – visualizing errors – density and contour plots – Histograms – legends – colors – subplots – text and annotation – customization – three dimensional plotting – Geographic Data with Basemap - Visualization with Seaborn.

Simple Line Plots

The simplest of all plots is the visualization of a single function $y = fx$. Here we will take a first look at creating a simple plot of this type.

The *figure* (an instance of the class `plt.Figure`) can be thought of as a single container that contains all the objects representing axes, graphics, text, and labels.

The *axes* (an instance of the class `plt.Axes`) is what we see above: a bounding box with ticks and labels, which will eventually contain the plot elements that make up our visualization.

Line Colors and Styles

- The first adjustment you might wish to make to a plot is to control the line colors and styles.
- To adjust the color, you can use the `color` keyword, which accepts a string argument representing virtually any imaginable color. The color can be specified in a variety of ways
- If no color is specified, Matplotlib will automatically cycle through a set of default colors for multiple lines

Different forms of color representation.

```
specify color by name           -color='blue'
short color code (rgbcmk)      -color='g'
Grayscale between 0 and 1      -color='0.75'
Hex code (RRGGBB from 00 to FF)-
color='#FFDD44' RGB tuple, values 0 and 1 -
color=(1.0,0.2,0.3) all HTML color names supported -
color='chartreuse'
```

- We can adjust the line style using the `linestyle` keyword.

Different line styles

```
linestyle='solid' line
style='dashed' lines
tyle='dashdot' lines
tyle='dotted'
```

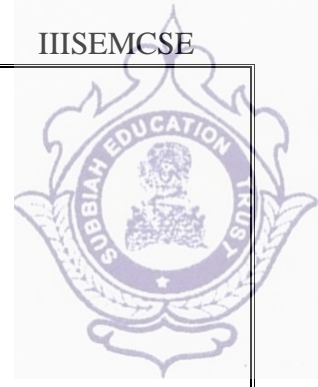
Short assignment

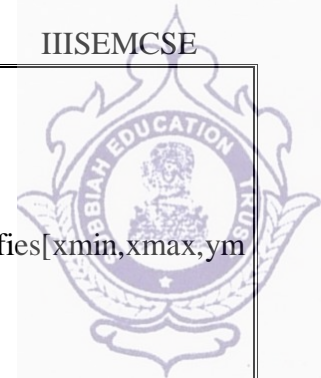
```
linestyle='-' #
solid linestyle='--' #
dashed linestyle='-'
.'#dashdot linestyle=':'
# dotted
```

- `linestyle` and `color` codes can be combined into a single non-keyword argument to the `plt.plot()` function

```
plt.plot(x, x + 0, '-g') # solid
green plt.plot(x, x + 1, '--c') # dashed
cyan plt.plot(x, x + 2, '-.k') # dashdot
black plt.plot(x, x + 3, ':r'); # dottedred
```

Axes Limits





- The most basic way to adjust axis limits is to use the `plt.xlim()` and `plt.ylim()` methods
 Example

```
plt.xlim(10,0)
plt.ylim(1.2,-1.2);
```
- The `plt.axis()` method allows you to set the x and y limits with a single call, by passing a list that specifies `[xmin, xmax, ymin, ymax]`

```
plt.axis([-1,11,-1.5,1.5]);
```
- A `square` ratio is used to represent one unit in x is equal to one unit in y. `plt.axis('equal')`

Labeling Plots

The labeling of plots includes titles, axis labels, and simple legends. Title - `plt.title()`

Label - `plt.xlabel()`

`plt.ylabel()`

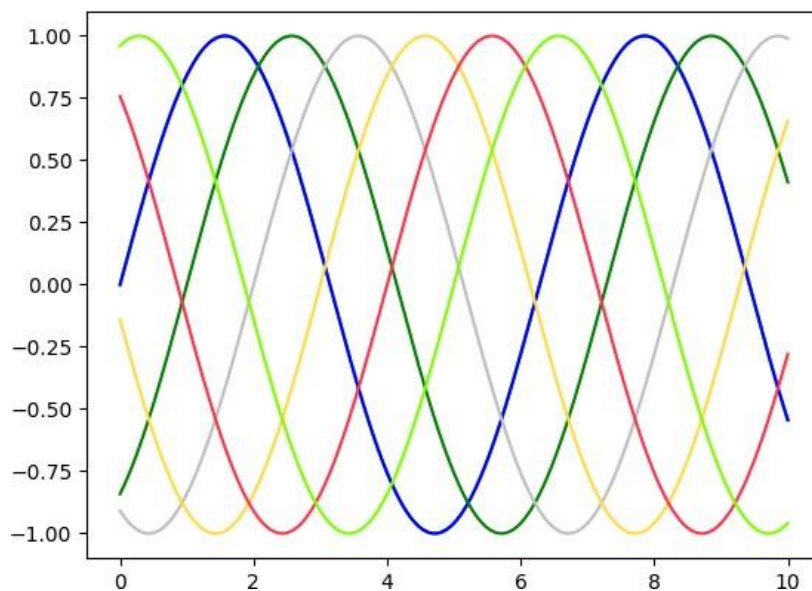
Legend - `plt.legend()`

Example

programs Linecolor

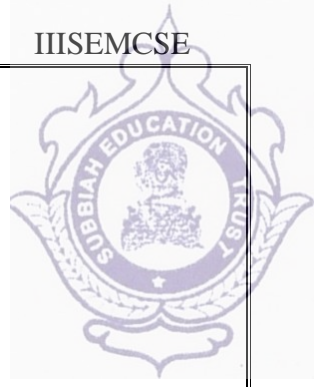
r

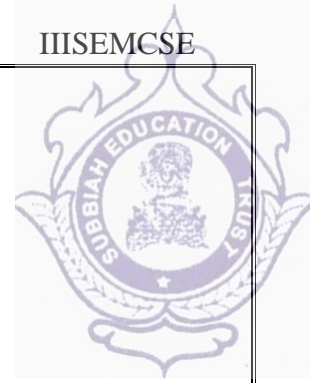
```
import matplotlib.pyplot as plt
import numpy as np
fig=plt.figure()
ax=plt.axes()
x=np.linspace(0,10,1000)
ax.plot(x,np.sin(x));
plt.plot(x, np.sin(x - 0), color='blue') # specify color by name
plt.plot(x, np.sin(x - 1), color='g') # short color code
plt.plot(x,np.sin(x-2),color='0.75')#Grayscale between 0 and 1
plt.plot(x,np.sin(x-3),color='#FFDD44')#Hex code(RRGGBB from 00 to FF)
plt.plot(x, np.sin(x - 4), color=(1.0,0.2,0.3)) # RGB tuple, values 0 and 1
plt.plot(x,np.sin(x-5),color='chartreuse');#all HTML color names supported
```



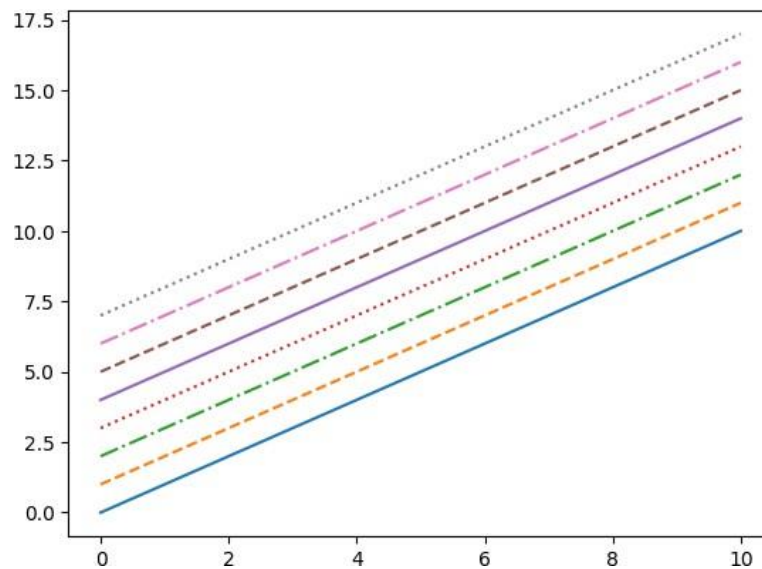
Linestyle

```
import matplotlib.pyplot as plt
```



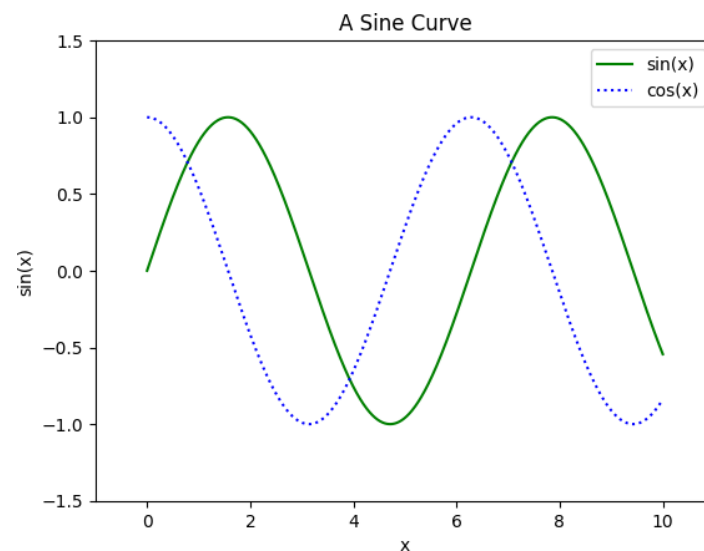


```
import numpy as np
fig=plt.figure()
ax=plt.axes()
x=np.linspace(0, 10, 1000)
plt.plot(x, x + 0, linestyle='solid')
plt.plot(x, x + 1, linestyle='dashed')
plt.plot(x, x + 2, linestyle='dashdot')
plt.plot(x, x + 3, linestyle='dotted');
#For short, you can use the following codes:
plt.plot(x, x + 4, linestyle='-') # solid
plt.plot(x, x + 5, linestyle='--') # dashed
plt.plot(x, x + 6, linestyle='-.' ) # dashdot
plt.plot(x, x + 7, linestyle=':') # dotted
```

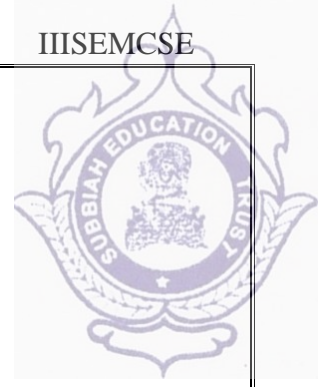


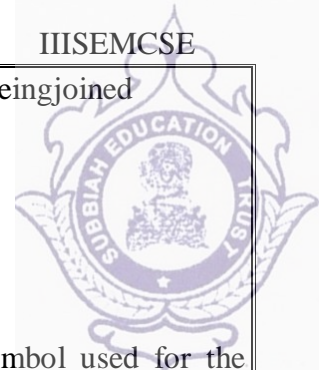
Axis limit with label and legend

```
import matplotlib.pyplot as plt
import numpy as np
fig=plt.figure()
ax=plt.axes()
x=np.linspace(0,10, 1000)
plt.xlim(-1,11)
plt.ylim(-1.5,1.5);
plt.plot(x,np.sin(x),'-g',label='sin(x)')
plt.plot(x,np.cos(x),':b',label='cos(x)')
plt.title("A Sine Curve")
plt.xlabel("x")
plt.ylabel("sin(x)");
plt.legend();
```



Simple Scatter Plots





Another commonly used plot type is the simple scatter plot, a close cousin of the line plot. Instead of points being joined by line segments, here the points are represented individually with a dot, circle, or other shape.

Syntax

```
plt.plot(x,y,'typeofsymbol',color);
```

Example

```
plt.plot(x,y,'o',color='black');
```

- The third argument in the function call is a character that represents the type of symbol used for the plotting. Just as you can specify options such as '-' and '--' to control the line style, the marker style has its own set of short string codes.

Example

- Various symbols used to specify ['o', '.', ',', 'x', '+', 'v', '^', '<', '>', 's', 'd']
- Shorthand assignment of line, symbol and color also allowed.

```
plt.plot(x,y,'-ok');
```

- Additional arguments in plt.plot()
We can specify some other parameters related with scatter plot which makes it more attractive. They are color, marker size, linewidth, marker face color, marker edge color, marker edge width, etc

Example

```
plt.plot(x, y, '-p',
color='gray', markersize=15,
linewidth=4, markerfacecolor
='white', markeredgecolor='g
ray', markeredgewidth=2)plt.
ylim(-1.2,1.2);
```

Scatter Plots with plt.scatter

- A second, more powerful method of creating scatter plots is the plt.scatter function, which can be used very similarly to the plt.plot function
- ```
plt.scatter(x,y,marker='o');
```
- The primary difference of plt.scatter from plt.plot is that it can be used to create scatter plots where the properties of each individual point (size, face color, edge color, etc.) can be individually controlled or mapped to data.
  - Notice that the color argument is automatically mapped to a color scale (shown here by the colorbar() command), and the size argument is given in pixels.
  - Cmap—color map used in scatter plot gives different color combinations.

### Perceptually Uniform Sequential

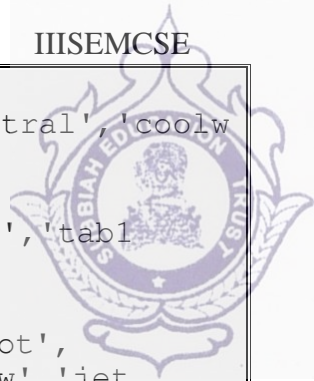
```
['viridis', 'plasma', 'inferno', 'magma']
```

### Sequential

```
['Greys', 'Purples', 'Blues', 'Greens', 'Oranges', 'Reds', 'YlOrBr', 'YlOrRd',
'OrRd', 'PuRd', 'RdPu', 'BuPu', 'GnBu', 'PuBu', 'YlGnBu', 'PuBuGn', 'BuGn', 'YlGn']
```

### Sequential (2)

```
['binary', 'gist_yarg', 'gist_gray', 'gray', 'bone', 'pink', 'spring', 'summer',
'autumn', 'winter', 'cool', 'Wistia', 'hot', 'afmhot', 'gist_heat', 'copper']
```



**Diverging**

```
['PiYG', 'PRGn', 'BrBG', 'PuOr', 'RdGy', 'RdBu', 'RdYlBu', 'RdYlGn', 'Spectral', 'coolw
arm', 'bwr', 'seismic']
```

**Qualitative**

```
['Pastel1', 'Pastel2', 'Paired', 'Accent', 'Dark2', 'Set1', 'Set2', 'Set3', 'tab1
0', 'tab20', 'tab20b', 'tab20c']
```

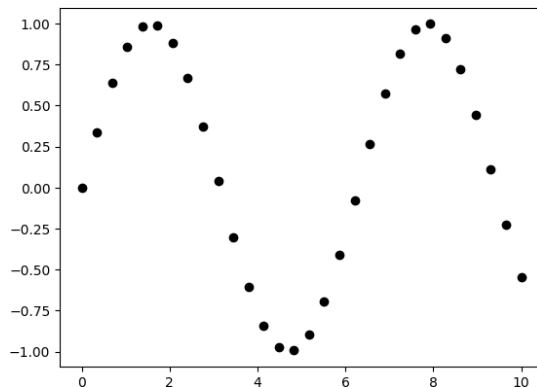
**Miscellaneous**

```
['flag', 'prism', 'ocean', 'gist_earth', 'terrain', 'gist_stern', 'gnuplot',
'gnuplot2', 'CMRmap', 'cubehelix', 'brg', 'hsv', 'gist_rainbow', 'rainbow', 'jet
', 'nipy_spectral', 'gist_ncar']
```

**Example programs.**

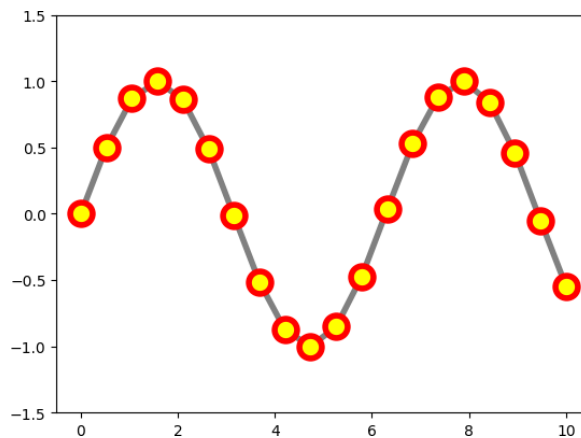
**Simple scatterplot.**

```
import numpy as np
import matplotlib.pyplot as plt
x=np.linspace(0,10, 30)
y=np.sin(x)
plt.plot(x,y,'o',color='black');
```



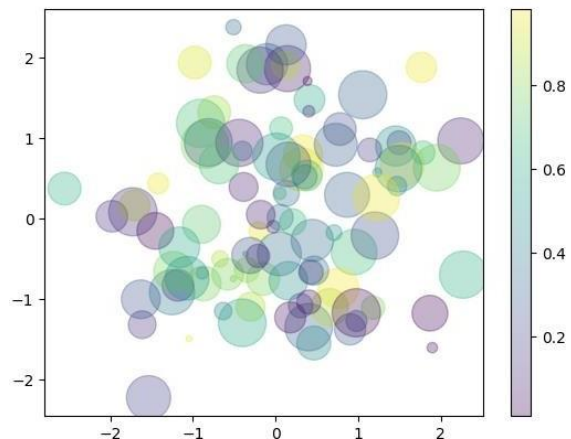
**Scatter plot with edge color, face color, size, and width of marker. (Scatter plot with line)**

```
import numpy as np
import matplotlib.pyplot as plt
x=np.linspace(0,10, 20)
y=np.sin(x)
plt.plot(x,y,'-o',color='gray',markersize=15
,
linewidth=4,markerfacecolor
='yellow',markeredgecolor='r
ed',markeredgecolorwidth=4)plt.yl
im(-1.5,1.5);
```

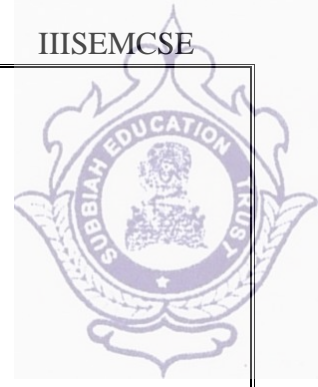


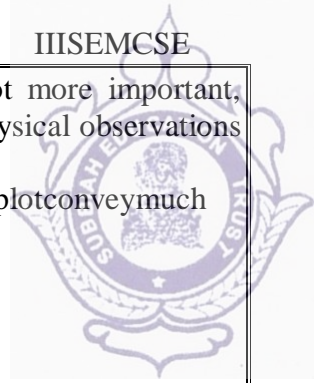
**Scatter plot with random colors, size, and transparency**

```
import numpy as np
import matplotlib.pyplot as plt
rng=np.random.RandomState(0)
x=rng.randn(100)
y =
rng.randn(100)
colors=
rng.rand(100)
sizes=1000 *rng.rand(100)
plt.scatter(x,y,c=colors,s=sizes,alpha=0.3,
map='viridis')plt.colorbar()
```



**Visualizing Errors**





For any scientific measurement, accurate accounting for errors is nearly as important, if not more important, than accurate reporting of the number itself. For example, imagine that I am using some astrophysical observations to estimate the Hubble Constant, the local measurement of the expansion rate of the Universe. In visualization of data and results, showing these errors effectively can make a plot convey much more complete information.

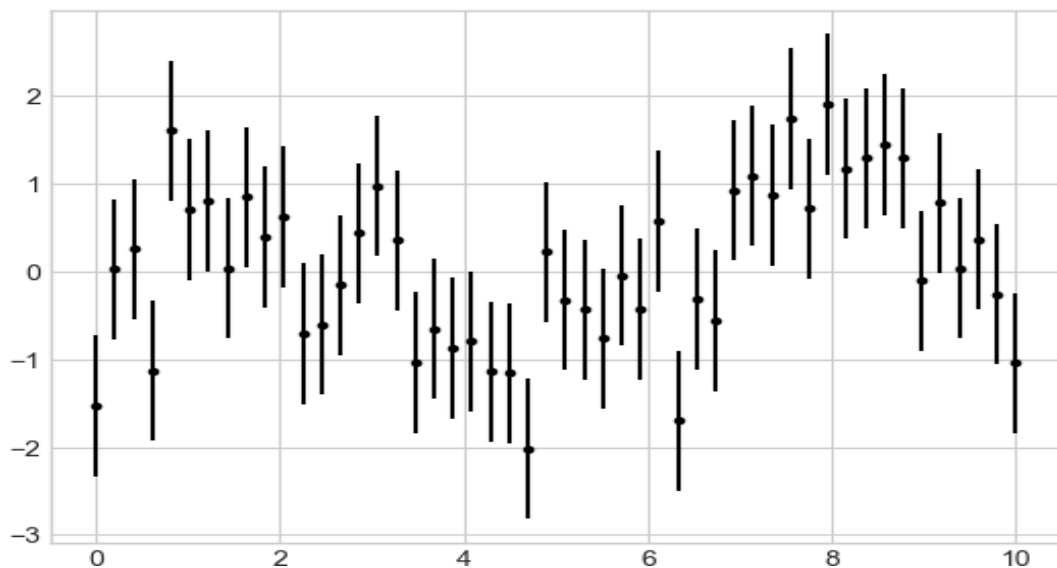
Types of errors

- Basic Error bars
- Continuous Errors

**Basic Error bars**

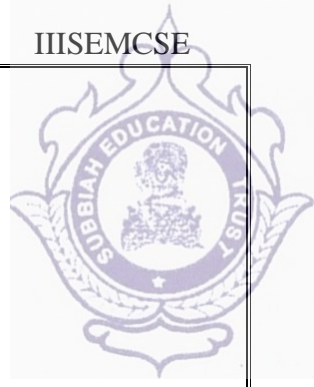
A basic error bar can be created with a single Matplotlib function call.

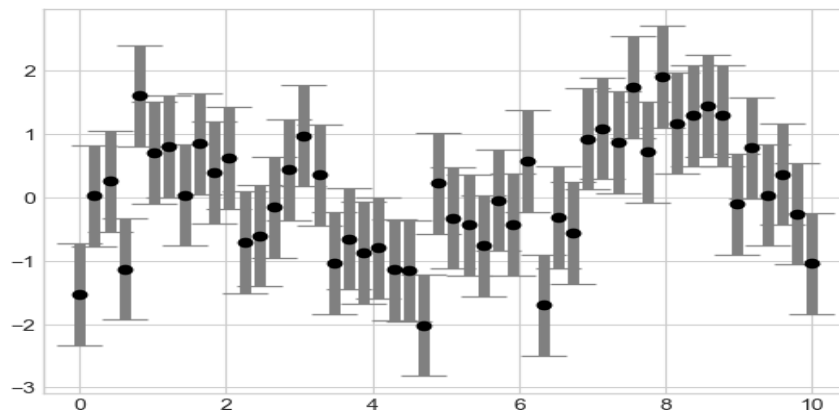
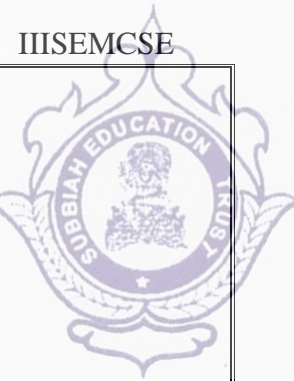
```
import matplotlib.pyplot as plt
plt.style.use('seaborn-whitegrid')
import numpy as np
x = np.linspace(0,10,50)
dy = 0.8
y = np.sin(x) + dy * np.random.randn(50)
plt.errorbar(x,y,yerr=dy,fmt='.k');
```



- Here the `fmt` is a format code controlling the appearance of lines and points, and has the same syntax as the shorthand used in `plt.plot()`
- In addition to these basic options, the errorbar function has many options to fine tune the outputs. Using these additional options you can easily customize the aesthetics of your errorbar plot.

```
plt.errorbar(x,y,yerr=dy,fmt='o',color='black',ecolor='lightgray',elinewidth=3,capsize=0);
```





### Continuous Errors

- In some situations it is desirable to show errorbars on continuous quantities. Though Matplotlib does not have a built-in convenience routine for this type of application, it's relatively easy to combine primitives like `plt.plot` and `plt.fill_between` for a useful result.
- Here we'll perform a simple Gaussian process regression (GPR), using the Scikit-Learn API. This is a method of fitting a very flexible nonparametric function to data with a continuous measure of the uncertainty.

### Density and Contour Plots

To display three-dimensional data in two dimensions using contours or color-coded regions. There are three Matplotlib functions that can be helpful for this task:

- `plt.contour` for contour plots,
- `plt.contourf` for filled contour plots, and
- `plt.imshow` for showing images.

### Visualizing a Three-Dimensional Function

A contour plot can be created with the `plt.contour` function.

It takes three arguments:

- a grid of x values,
- a grid of y values, and
- a grid of z values.

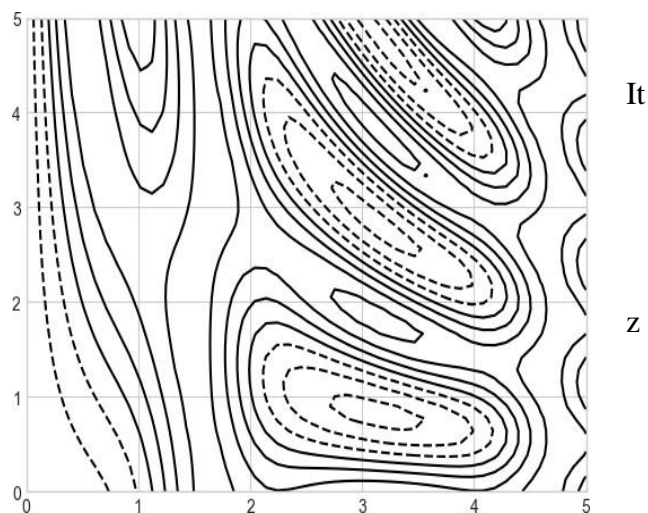
The x and y values represent positions on the plot, and the

z values will be represented by the contour levels.

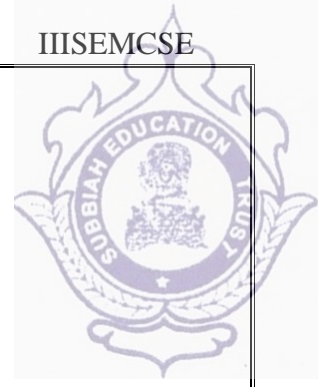
The way to prepare such data is to use the `np.meshgrid` function, which builds two-dimensional grids from one-dimensional arrays:

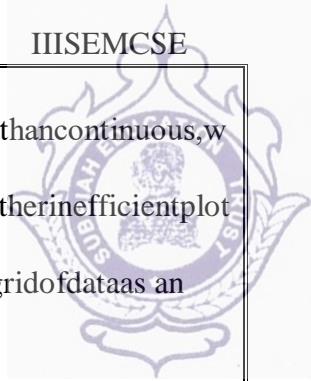
Example

```
def f(x,y):
 return np.sin(x) ** 10 + np.cos(10 + y * x) *
np.cos(x)
x=np.linspace(0,5,50)
y=np.linspace(0,5,40)
X,Y = np.meshgrid(x,
y)
Z=f(X,Y)
plt.contour(X,Y,Z,colors='black');
```



- Notice that by default when a single color is used, negative values are represented by dashed lines, and positive values by solid lines.
- Alternatively, you can color-code the lines by specifying a colormap with the `cm` argument.
- We'll also specify that we want more lines to be drawn—20 equally spaced intervals within the data range.





```
plt.contour(X,Y,Z,20,cmap='RdGy');
```

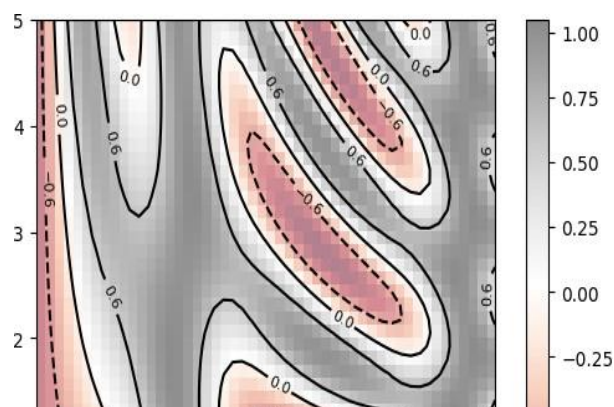
- One potential issue with this plot is that it is a bit “splotchy.” That is, the color steps are discrete rather than continuous, which is not always what is desired.
- You could remedy this by setting the number of contours to a very high number, but this results in a rather inefficient plot: Matplotlib must render a new polygon for each step in the level.
- A better way to handle this is to use the `plt.imshow()` function, which interprets a two-dimensional grid of data as an image.

**There are a few potential gotchas with `imshow()`.**

- `plt.imshow()` doesn't accept an x and y grid, so you must manually specify the extent `[xmin, xmax, ymin, ymax]` of the image on the plot.
- `plt.imshow()` by default follows the standard image array definition where the origin is in the upper left, not in the lower left as in most contour plots. This must be changed when showing gridded data.
- `plt.imshow()` will automatically adjust the axis aspect ratio to match the input data; you can change this by setting, for example, `plt.axis(aspect='image')` to make x and y units match.

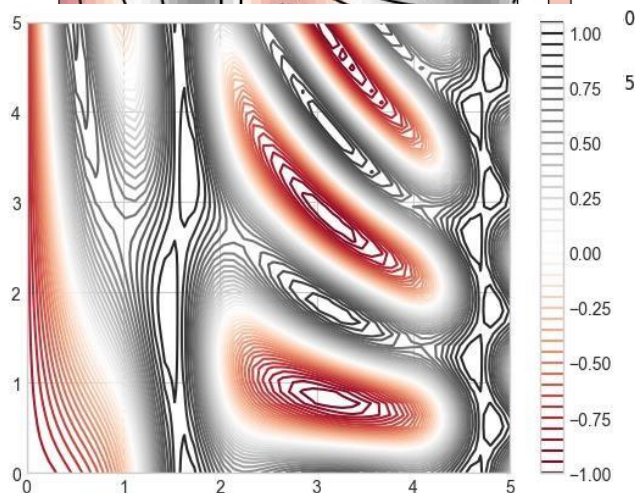
Finally, it can sometimes be useful to combine contour plots and image plots. We'll use a partially transparent background image (with transparency set via the `alpha` parameter) and overplot contours with labels on the contours themselves (using the `plt.clabel()` function):

```
contours = plt.contour(X, Y, Z, 3,
 colors='black')
plt.clabel(contours, inline=True,
 fontsize=8)
plt.imshow(Z, extent=[0, 5, 0, 5],
 origin='lower', cmap='RdGy', alpha=0.5)
plt.colorbar();
```



**Example Program**

```
import numpy as np
import matplotlib.pyplot as plt
def eff(x, y):
 return np.sin(x)**10 + np.cos(10 + y*x)*np.cos(x)
x = np.linspace(0, 5, 50)
y = np.linspace(0, 5, 40)
X, Y = np.meshgrid(x, y)
Z = eff(X, Y)
plt.imshow(Z, extent=[0, 10, 0, 10], origin='lower',
 cmap='RdGy')
plt.colorbar();
```

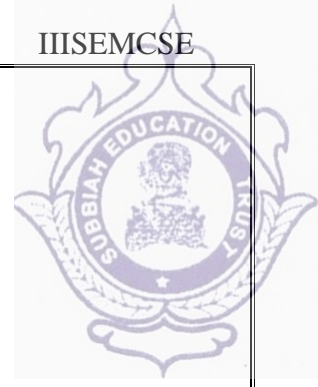


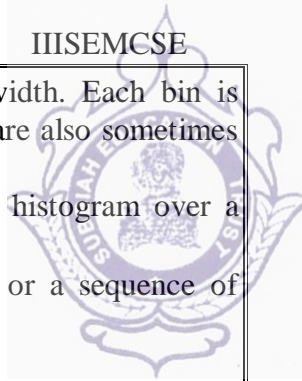
**Histograms**

- A histogram is a simple plot to represent a large dataset. A histogram is a graph showing frequency distributions. It is a graph showing the number of observations within each given interval.

**Parameters**

- `plt.hist()` is used to plot a histogram. The `hist()` function will use an array of numbers to create a histogram, the array is sent into the function as an argument.





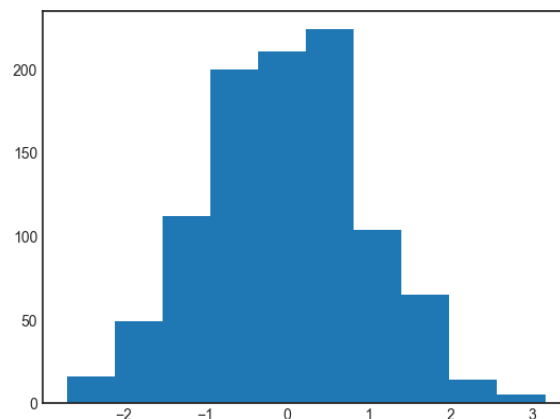
- **bins** - A histogram displays numerical data by grouping data into "bins" of equal width. Each bin is plotted as a bar whose height corresponds to how many data points are in that bin. Bins are also sometimes called "intervals", "classes", or "buckets".
- **normed** - Histogram normalization is a technique to distribute the frequencies of the histogram over a wider range than the current range.
- **x** -(n,) array or sequence of (n,) arrays Input values, this takes either a single array or a sequence of arrays which are not required to be of the same length.
- **histtype** - {'bar', 'barstacked', 'step', 'stepfilled'}, optional The type of histogram to draw.
  - 'bar' is a traditional bar-type histogram. If multiple data are given the bars are arranged side by side.
  - 'barstacked' is a bar-type histogram where multiple data are stacked on top of each other.
  - 'step' generates a line plot that is by default unfilled.
  - 'stepfilled' generates a line plot that is by default filled. Default is 'bar'
- **align**-{'left', 'mid', 'right'}, optional Control how the histogram is plotted.
  - 'left': bars are centered on the left bin edges.
  - 'mid': bars are centered between the bin edges.
  - 'right': bars are centered on the right bin edges. Default is 'mid'
- **orientation**-{'horizontal', 'vertical'}, optional If 'horizontal', barh will be used for bar-type histograms and the bottom kwarg will be the left edges.
- **color**-color or array\_like of colors or None, optional Color spec or sequence of color specs, one per dataset. Default (None) uses the standard line color sequence. Default is None
- **label**-str or None, optional. Default is None

**Other parameter**

- **\*\*kwargs** - Patch properties, it allows us to pass a variable number of keyword arguments to a python function. \*\*denotes the type of function.

**Example**

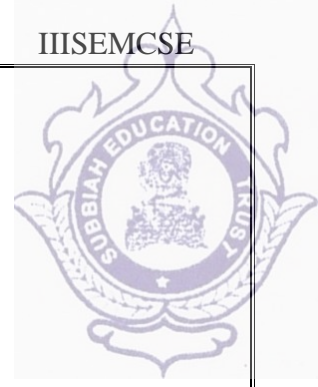
```
import numpy as np
import matplotlib.pyplot as plt
plt.style.use('seaborn-white')
data = np.random.randn(1000)
plt.hist(data);
```

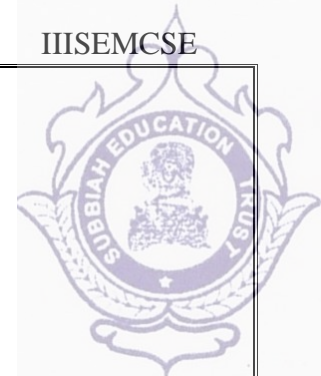


The hist() function has many options to tune both the calculation and the display; here's an example of a more customized histogram.

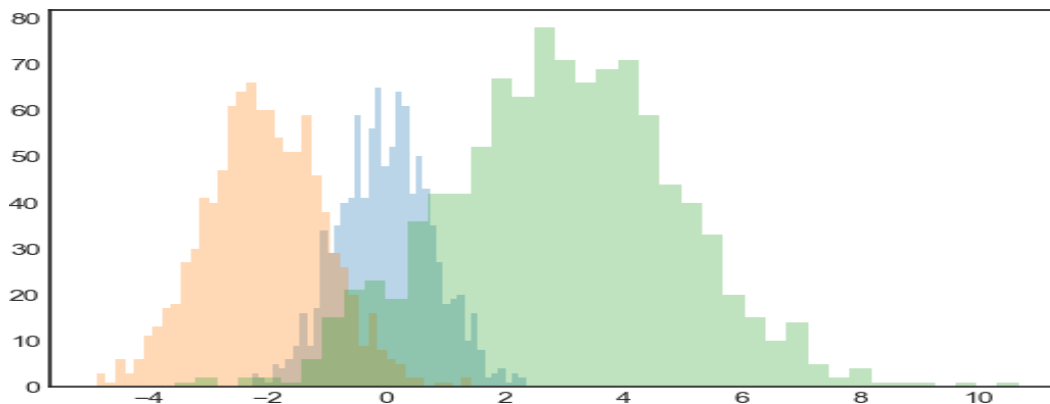
```
plt.hist(data, bins=30, alpha=0.5, histtype='stepfilled', color='steelblue', edgecolor='none');
```

The plt.hist docstring has more information on other customization options available. I find this combination of histtype='stepfilled' along with some transparency alpha to be very useful when comparing histograms of several distributions.





```
x1=np.random.normal(0,0.8,1000)
x2=np.random.normal(-2,1,1000)
x3=np.random.normal(3,2,1000)
kwargs = dict(histtype='stepfilled', alpha=0.3,
bins=40)plt.hist(x1, **kwargs)
plt.hist(x2,
**kwargs)plt.hist(x3,*
```



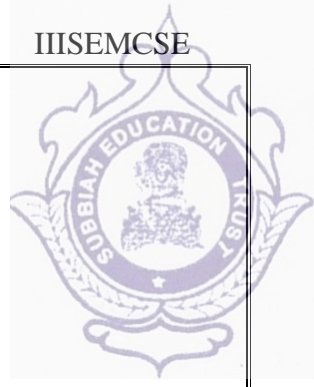
```
*kwargs);
```

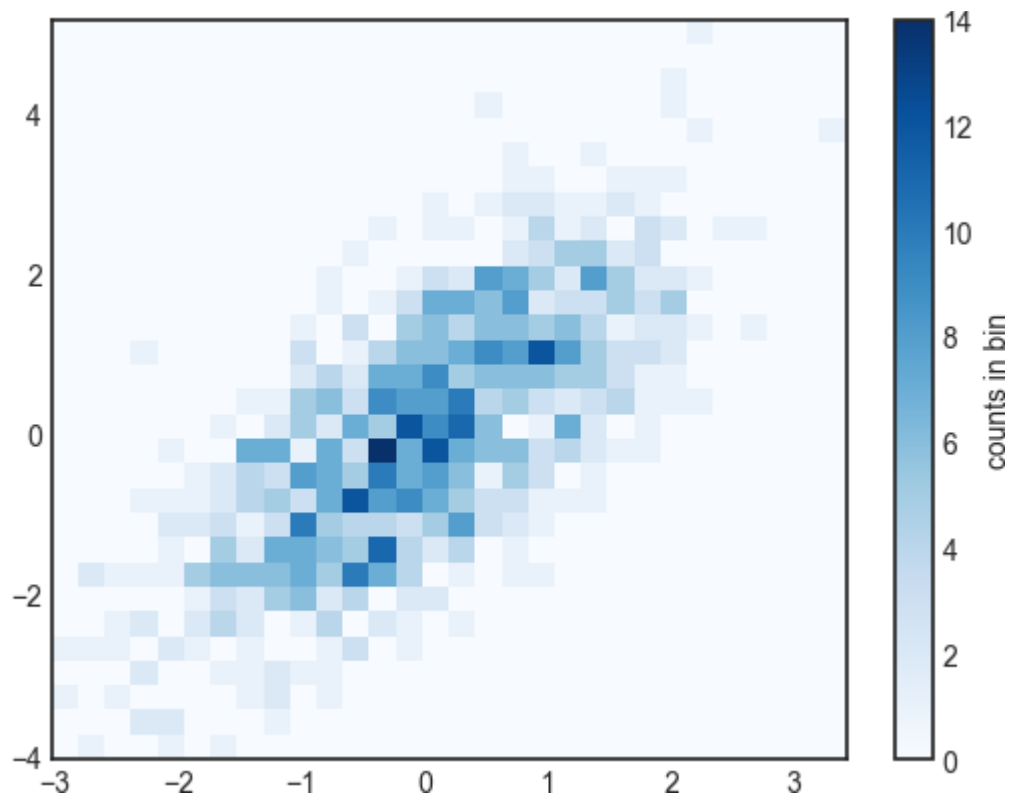
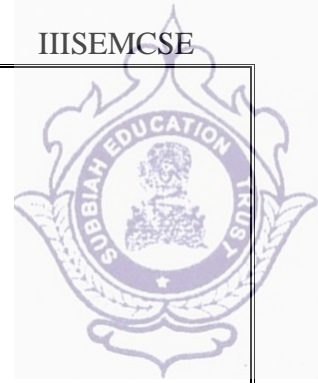
### Two-Dimensional Histograms and Binnings

- We can create histograms in two dimensions by dividing points among two-dimensional bins.
- We would define x and y values. Here for example we'll start by defining some data—an x and y array drawn from a multivariate Gaussian distribution:
- Simple way to plot a two-dimensional histogram is to use Matplotlib's `plt.hist2d()` function

### Example

```
mean =[0, 0]
cov =[[1,1],[1,2]]
x,y=np.random.multivariate_normal(mean,cov,1000).T
plt.hist2d(x,
y,bins=30, cmap='Blues')
cb =
plt.colorbar()cb.set_label('
counts in bin')
```





## Legends

Plot legends give meaning to a visualization, assigning labels to the various plot elements. We previously saw how to create a simple legend; here we'll take a look at customizing the placement and aesthetics of the legend in Matplotlib.

Plot legends give meaning to a visualization, assigning labels to the various plot elements. We previously saw how to create a simple legend; here we'll take a look at customizing the placement and aesthetics of the legend in Matplotlib.

```
plt.plot(x,np.sin(x),'-b',label='Sine')
plt.plot(x, np.cos(x), '--r',
label='Cosine')plt.legend();
```

### Customizing Plot Legends

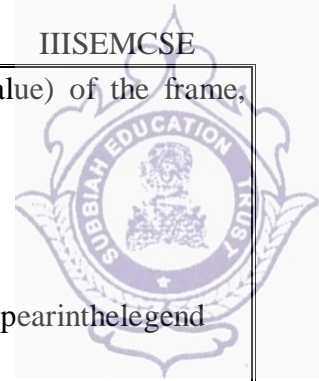
**Location and turn off the frame** - We can specify the location and turn off the frame. By the parameter `loc` and `frameon`.

```
ax.legend(loc='upper left',
frameon=False)fig
```

**Number of columns** - We can use the `ncol` command to specify the number of columns in the legend.

```
ax.legend(frameon=False, loc='lower center',
ncol=2)fig
```

### Rounded box, shadow and frame transparency



We can use a rounded box (fancybox) or add a shadow, change the transparency (alpha value) of the frame, or change the padding around the text.

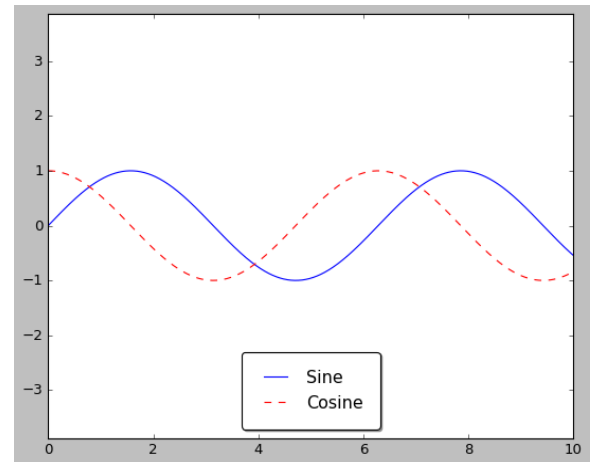
```
ax.legend(fancybox=True, framealpha=1, shadow=True,
borderpad=1)fig
```

### Choosing Elements for the Legend

- The legend includes all labeled elements by default. We can change which elements and labels appear in the legend by using the objects returned by plot commands.
- The plt.plot() command is able to create multiple lines at once, and returns a list of created line instances. Passing any of these to plt.legend() will tell it which to identify, along with the labels we'd like to specify

```
y = np.sin(x[:, np.newaxis] + np.pi * np.arange(0, 2,
0.5))lines =plt.plot(x,y)
plt.legend(lines[:2],['first','second']);
```

```
Applying label
individually.plt.plot(x,y[:,0],l
abel='first')
plt.plot(x,y[:,1],label='second')
plt.plot(x, y[:,
2:])plt.legend(framealpha=1,frameon=Tr
ue);
```



### Multiple legends

It is only possible to create a single legend for the entire plot. If you try to create a second legend using plt.legend() or ax.legend(), it will simply override the first one. We can work around this by creating a new legend artist from scratch, and then using the lower-level ax.add\_artist() method to manually add the second artist to the plot

### Example

```
import matplotlib.pyplot as plt
plt.style.use('classic')
import numpy as np
x= np.linspace(0,10,1000)
ax.legend(loc='lowercenter',frameon=True,shadow=True,borderpad=1,fancybox=True)fig
```

## Color Bars

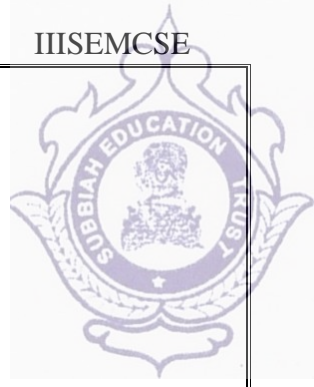
In Matplotlib, a color bar is a separate axis that can provide a key for the meaning of colors in a plot. For continuous labels based on the color of points, lines, or regions, a labeled color bar can be a great tool. The simplest color bar can be created with the plt.colorbar() function.

### Customizing Colorbars

#### Choosing colormap.

We can specify the colormap using the cmap argument to the plotting function that is creating the visualization. Broadly, we can know three different categories of colormaps:

- **Sequential colormaps**- These consist of one continuous sequence of colors (e.g., binary or viridis).
- **Divergent colormaps**- These usually contain two distinct colors, which show positive and negative deviations from a mean (e.g., RdBu or PuOr).
- **Qualitative colormaps** - These mix colors with no particular sequence (e.g., rainbow or jet).

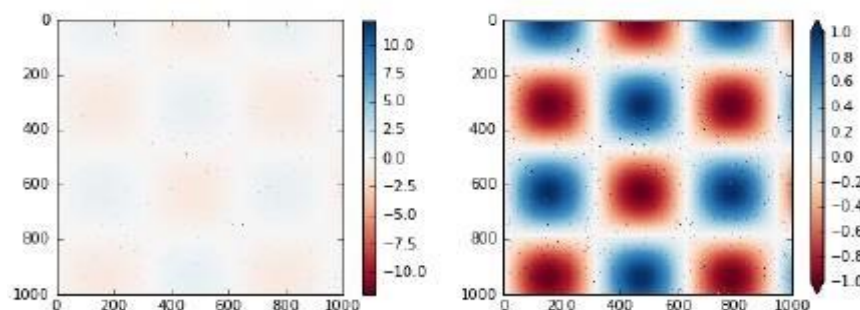




### Color limits and extensions

- Matplotlib allows for a larger range of color bar customization. The color bar itself is simply an instance of `plt.Axes`, so all of the axes and tick formatting tricks we've learned are applicable.
- We can narrow the color limits and indicate the out-of-bounds values with a triangular arrow at the top and bottom by setting the `extend` property.

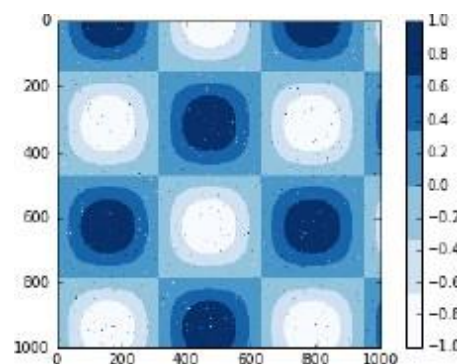
```
plt.subplot(1, 2,
2)plt.imshow(I,
cmap='RdBu')plt.colorbar(e
xtend='both')plt.clim(-1,1);
```



### Discrete colorbars

Color maps are by default continuous, but sometimes you'd like to represent discrete values. The easiest way to do this is to use the `plt.cm.get_cmap()` function, and pass the name of a suitable colormap along with the number of desired bins.

```
plt.imshow(I, cmap=plt.cm.get_cmap('Blues',
6))plt.colorbar()
plt.clim(-1,1);
```



### Subplots

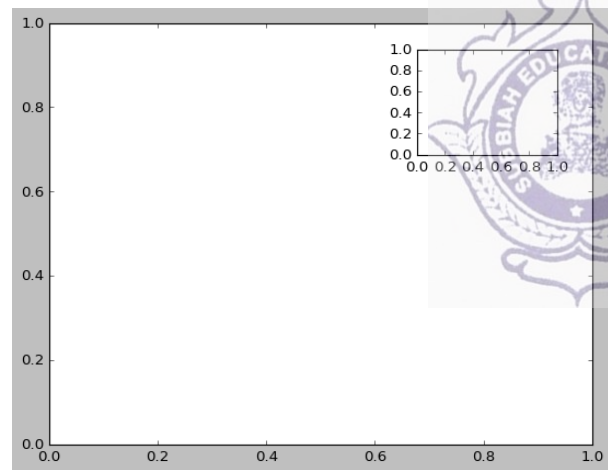
- Matplotlib has the concept of subplots: groups of smaller axes that can exist together within a single figure.
- These subplots might be insets, grids of plots, or other more complicated layouts.
- We'll explore four routines for creating subplots in Matplotlib.
  - `plt.axes`: Subplots by Hand
  - `plt.subplot`: Simple Grid of Subplots
  - `plt.subplots`: The Whole Grid in One Go
  - `plt.GridSpec`: More Complicated Arrangements

### `plt.axes`: Subplots by Hand

- The most basic method of creating an axis is to use the `plt.axes` function. As we've seen previously, by default this creates a standard axes object that fills the entire figure.
- `plt.axes` also takes an optional argument that is a list of four numbers in the figure coordinate system.
- These numbers represent [bottom, left, width, height] in the figure coordinate system, which ranges from 0 at the bottom left of the figure to 1 at the top right of the figure.

Forexample,  
we might create an inset axes at the top-right corner of another axes by setting the x and y position to 0.65 (that is, starting at 65% of the width and 65% of the height of the figure) and the x and y extents to 0.2 (that is, the size of the axes is 20% of the width and 20% of the height of the figure).

```
import matplotlib.pyplot as plt
import numpy as np
ax1=plt.axes()#standard axes ax2=p
lt.axes([0.65,0.65,0.2,0.2])
```



### Vertical subplot

The equivalent of `plt.axes()` command within the object-oriented interface is `fig.add_axes()`. Let's use this to create two vertically stacked axes.

```
fig=plt.figure()
ax1 =fig.add_axes([0.1,0.5, 0.8,0.4],
xticklabels=[],ylim=(-1.2,1.2))
ax2 =fig.add_axes([0.1,0.1, 0.8,0.4],
ylim=(-1.2,1.2))
x = np.linspace(0,
10)ax1.plot(np.sin(x)
)
ax2.plot(np.cos(x));
```

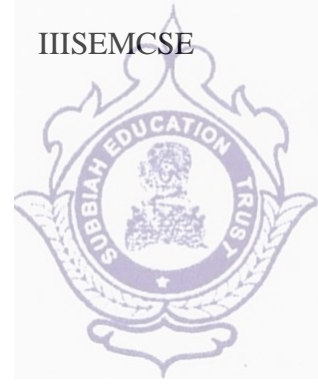
- We now have two axes (the top with no tick labels) that are just touching: the bottom of the upper panel (at position 0.5) matches the top of the lower panel (at position 0.1+0.4).
- If the axis value is changed in second plot both the plots are separated with each other, example `ax2 =fig.add_axes([0.1,0.01,0.8, 0.4`

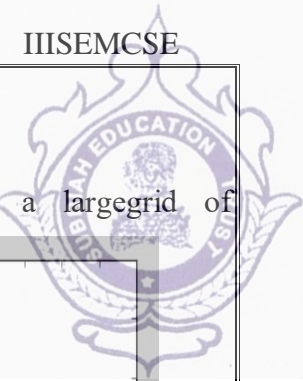
### plt.subplot: Simple Grids of Subplots

- Matplotlib has several convenience routines to align columns or rows of subplots.
- The lowest level of these is `plt.subplot()`, which creates a single subplot within a grid.

- This command takes three integer arguments—the number of rows, the number of columns, and the index of the plot to be created in this scheme, which runs from the upper left to the bottom right

```
for i in range(1,
7):plt.subplot(2,3,i
)
plt.text(0.5,0.5,str((2,3,i)),fo
ntsize=18,ha='center')
```



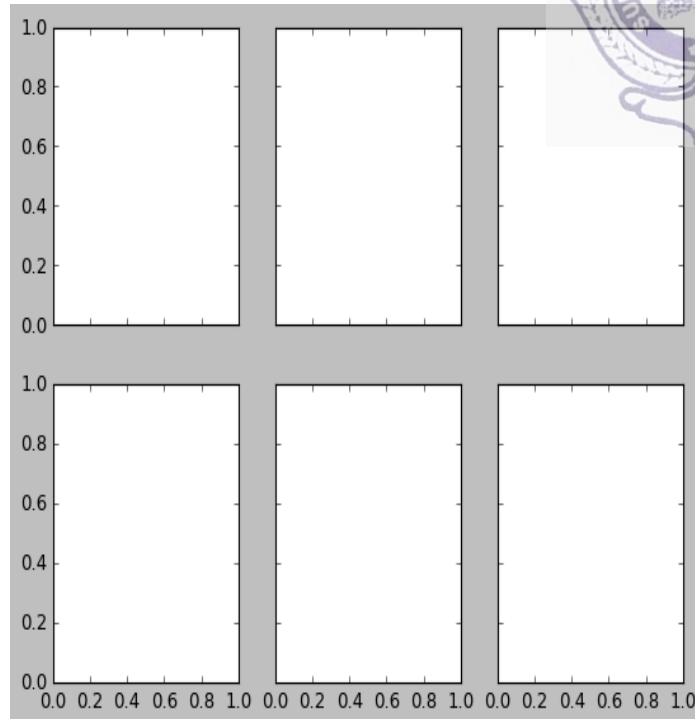


### plt.subplots:TheWholeGrid in OneGo

- The approach just described can become quite tedious when you're creating a large grid of subplots, especially if you'd like to hide the x- and y-axis labels on the inner plots.
- For this purpose, plt.subplots() is the easier tool to use (not the case at the end of subplots).
- Rather than creating a single subplot, this function creates a full grid of subplots in a single line, returning them in a NumPy array.
- The arguments are the number of rows and number of columns, along with optional keywords sharex and sharey, which allow you to specify the relationships between different axes.
- Here we'll create a 2x3 grid of subplots, where all axes in the same row share their y-axis scale, and all axes in the same column share their x-axis scale.

```
fig, ax = plt.subplots(2, 3,
 sharex='col', sharey='row')
```

Note that by specifying sharex and sharey, we've automatically removed inner labels on the grid to make the plot cleaner.

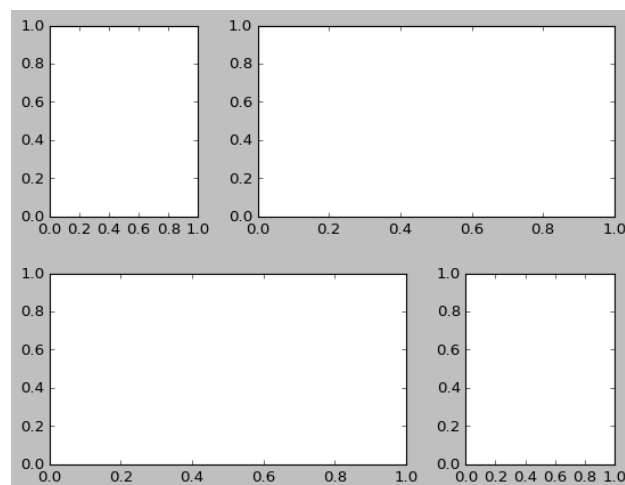


### plt.GridSpec:MoreComplicatedArrangements

To go beyond a regular grid to subplots that span multiple rows and columns, plt.GridSpec() is the best tool. The plt.GridSpec() object does not create a plot by itself; it is simply a convenient interface that is recognized by the plt.subplot() command.

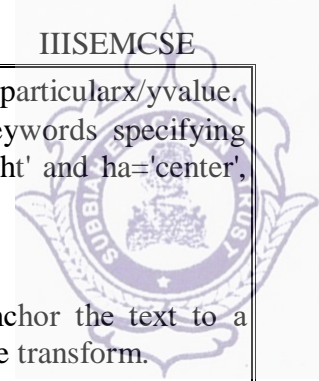
For example, a gridspec for a grid of two rows and three columns with some specified width and height space looks like this:

```
grid = plt.GridSpec(2, 3, wspace=0.4,
 hspace=0.3)
plt.subplot(grid[0, 0])
plt.subplot(grid[0, 1:])
plt.subplot(grid[1, :2])
plt.subplot(grid[1, 2]);
```



### Text and Annotation

- The most basic types of annotations we will use are axes labels and titles, here we will see some more visualization and annotation information's.



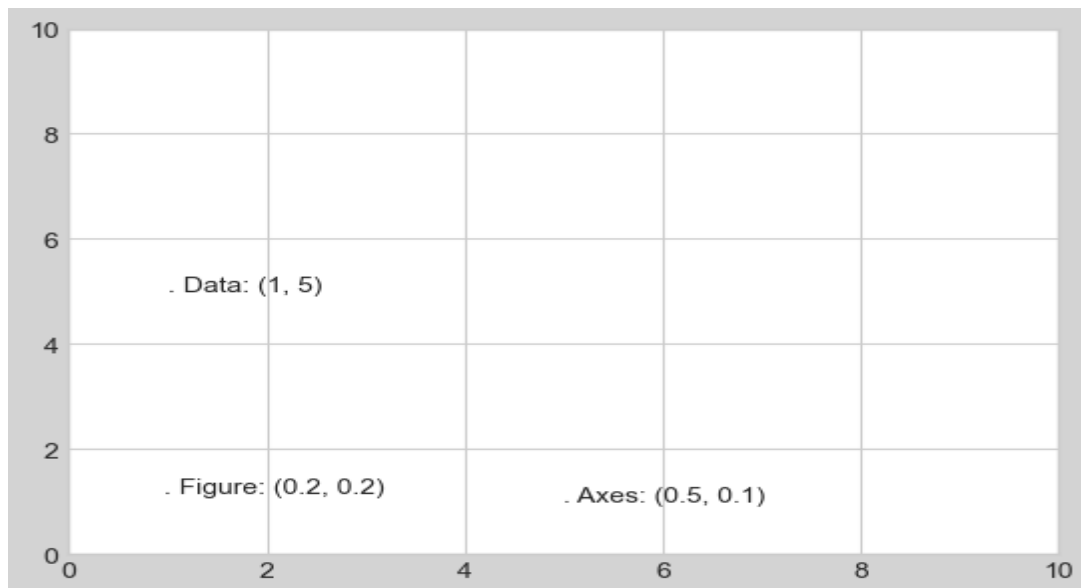
- Text annotation can be done manually with the `plt.text/ax.text` command, which will place text at a particular `x/y` value.
- The `ax.text` method takes an `x` position, a `y` position, a string, and then optional keywords specifying the color, size, style, alignment, and other properties of the text. Here we used `ha='right'` and `ha='center'`, where `ha` is short for horizontal alignment.

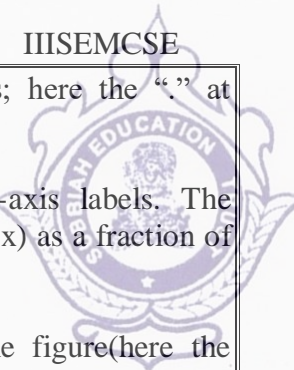
### Transforms and Text Position

- We anchored our text annotations to data locations. Sometimes it's preferable to anchor the text to a position on the axes or figure, independent of the data. In Matplotlib, we do this by modifying the transform.
- Any graphics display framework needs some scheme for translating between coordinate systems.
- Mathematically, such coordinate transformations are relatively straightforward, and Matplotlib has a well-developed set of tools that it uses internally to perform them (the tools can be explored in the `matplotlib.transforms` sub module).
- There are three predefined transforms that can be useful in this situation.
  - `ax.transData` - Transform associated with data coordinates
  - `ax.transAxes` - Transform associated with the axes (in units of axes dimensions)
  - `fig.transFigure` - Transform associated with the figure (in units of figure dimensions)

### Example

```
import matplotlib.pyplot as plt
import matplotlib as mpl
plt.style.use('seaborn-whitegrid')
import numpy as np
import pandas as pd
fig, ax = plt.subplots(facecolor='lightgray')
ax.axis([0, 10, 0, 10])
transform=ax.transData is the default, but we'll specify it anyway
ax.text(1, 5, ". Data: (1, 5)", transform=ax.transData)
ax.text(0.5, 0.1, ". Axes: (0.5, 0.1)", transform=ax.transAxes)
ax.text(0.2, 0.2, ". Figure: (0.2, 0.2)", transform=fig.transFigure);
```





Note that by default, the text is aligned above and to the left of the specified coordinates; here the “.” at the beginning of each string will approximately mark the given coordinate location.

The transData coordinates give the usual data coordinates associated with the x- and y-axis labels. The transAxes coordinates give the location from the bottom-left corner of the axes (here the white box) as a fraction of the axes size.

The transfigure coordinates are similar, but specify the position from the bottom left of the figure (here the gray box) as a fraction of the figure size.

Notice now that if we change the axes limits, it is only the transData coordinates that will be affected, while the others remain stationary.

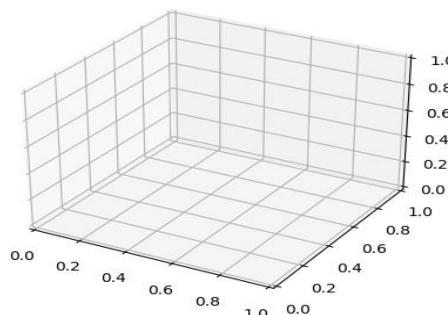
### Arrows and Annotation

- Along with tick marks and text, another useful annotation mark is the simple arrow.
- Drawing arrows in Matplotlib is not much harder because there is a `plt.arrow()` function available.
- The arrows it creates are SVG (scalable vector graphics) objects that will be subject to the varying aspect ratio of your plots, and the result is rarely what the user intended.
- The arrow style is controlled through the `arrowprops` dictionary, which has numerous options available.

### Three-Dimensional Plotting in Matplotlib

We enable three-dimensional plots by importing the `plot3d` toolkit, included with the main Matplotlib installation.

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
dfg = plt.figure()
ax = plt.axes(projection='3d')
```



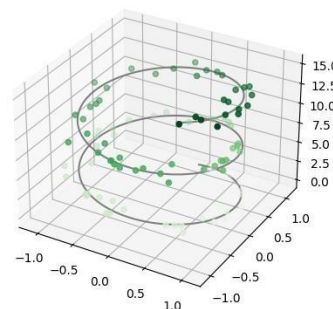
With this 3D axes enabled, we can now plot a variety of three-dimensional plot types.

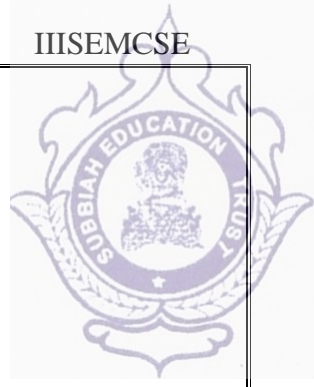
### Three-Dimensional Points and Lines

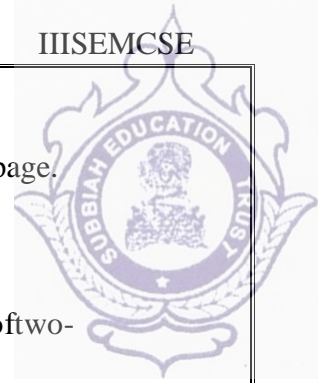
The most basic three-dimensional plot is a line or scatter plot created from sets of (x, y, z) triples.

In analogy with the more common two-dimensional plots discussed earlier, we can create these using the `ax.plot3D` and `ax.scatter3D` functions

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
dax = plt.axes(projection='3d')
Data for a three-dimensional line
zline = np.linspace(0, 15, 1000)
xline = np.sin(zline)
yline = np.cos(zline)
ax.plot3D(xline, yline, zline, 'gray')
Data for three-dimensional scattered points
zdata = 15 * np.random.random(100)
xdata = np.sin(zdata) + 0.1 * np.random.randn(100)
ydata = np.cos(zdata) + 0.1 * np.random.randn(100)
```







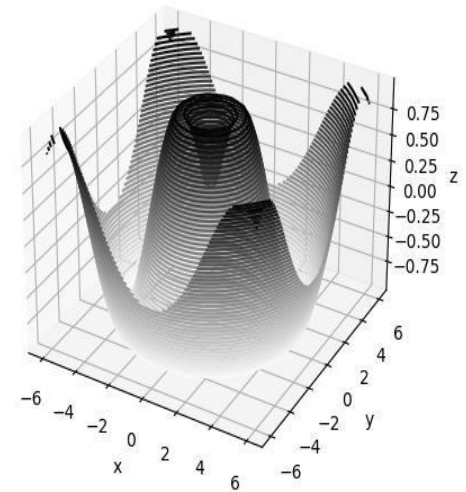
```
ax.scatter3D(xdata,ydata,zdata,c=zdata,cmap='Greens');plt.show()
```

Notice that by default, the scatter points have their transparency adjusted to give a sense of depth on the page.

### Three-Dimensional Contour Plots

- `mpl_toolkits.mplot3d` contains tools to create three-dimensional relief plots using the same inputs.
- Like two-dimensional `ax.contour` plots, `ax.contour3D` requires all the input data to be in the form of two-dimensional regular grids, with the Z data evaluated at each point.
- Here we'll show a three-dimensional contour diagram of a three-dimensional sinusoidal function

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
def d(x, y):
 return np.sin(np.sqrt(x**2 + y**2))
x = np.linspace(-6, 6, 30)
y = np.linspace(-6, 6, 30)
X, Y = np.meshgrid(x, y)
Z = d(X, Y)
fig = plt.figure()
ax = fig.axes[0]
ax.contour3D(X, Y, Z, 50, cmap='binary')
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
plt.show()
```



Sometimes the default viewing angle is not optimal, in which case we can use the `view_init` method to set the elevation and azimuthal angles.

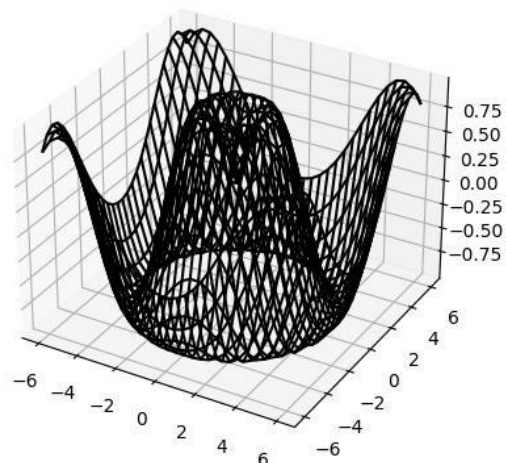
```
ax.view_init(60, 35)
fig
```

### Wireframes and Surface Plots

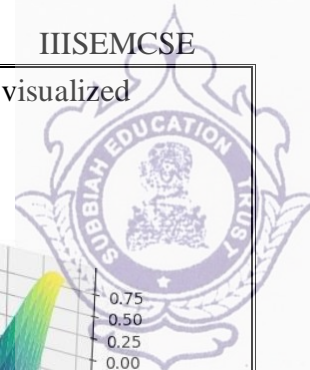
- Two other types of three-dimensional plots that work on gridded data are wireframes and surface plots.
- These take a grid of values and project it onto the specified three-dimensional surface, and can make the resulting three-dimensional forms quite easy to visualize.

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
fig = plt.figure()
ax = fig.axes[0]
ax.plot_wireframe(X, Y, Z, color='black')
ax.set_title('wireframe')
plt.show()
```

wireframe

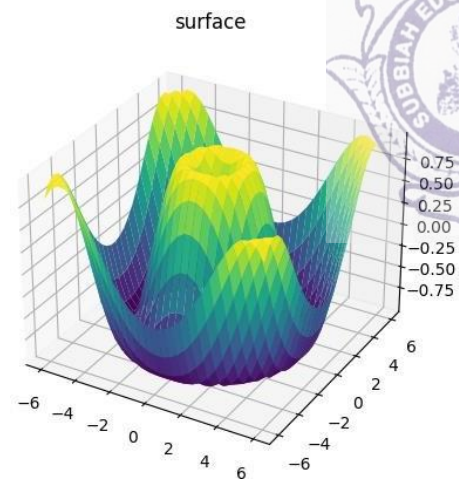


- A surface plot is like a wireframe plot, but each face of the wireframe is a filled polygon.



- Adding a colormap to the filled polygons can aid perception of the topology of the surface being visualized

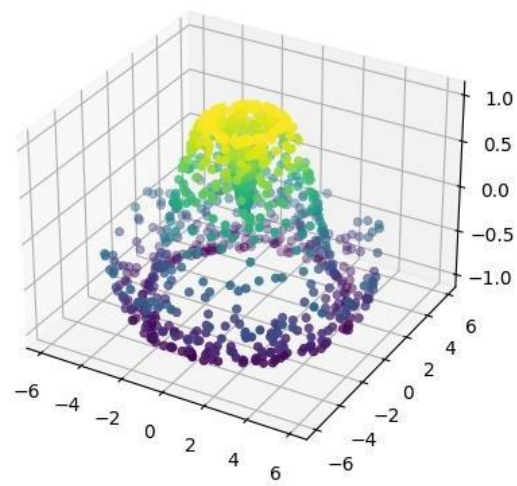
```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
ax = plt.axes(projection='3d')
ax.plot_surface(X, Y, Z, rstride=1,
 cstride=1, cmap='viridis',
 edgecolor='none')
ax.set_title('surface')
plt.show()
```



### Surface Triangulations

- For some applications, the evenly sampled grids required by the preceding routines are overly restrictive and inconvenient.
- In these situations, the triangulation-based plots can be very useful.

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
d
theta = 2 * np.pi * np.random.random(1000)
r = 6 * np.random.random(1000)
x = np.ravel(r * np.sin(theta))
y = np.ravel(r * np.cos(theta))
z = f(x, y)
ax = plt.axes(projection='3d')
ax.scatter(x, y, z, c=z, cmap='viridis', linewidth=0.5)
```



### Geographic Data with Basemap

- One common type of visualization in data science is that of geographic data.
- Matplotlib's main tool for this type of visualization is the Basemap toolkit, which is one of several Matplotlib toolkits that live under the `mpl_toolkits` namespace.
- Basemap is a useful tool for Python users to have in their virtual toolbelts
- Installation of Basemap. Once you have the Basemap toolkit installed and imported, geographic plots also require the PIL package in Python 2, or the pillow package in Python 3.

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.basemap import Basemap
plt.figure(figsize=(8,8))
m = Basemap(projection='ortho',
 resolution=None, lat_0=50, lon_0=-100)
m.bluemarble(scale=0.5);
```

- Matplotlib axes that understand spherical coordinates and allow us to easily over-plot data on the map

- We'll use an etopo image (which shows topographical features both on land and under the ocean) as the map background

Program to display particular area of the map with latitude and longitude lines

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.basemap import Basemap
from itertools import chain
fig=plt.figure(figsize=(8,8))
m = Basemap(projection='lcc',
resolution=None,width=8E6,height=8E6,
lat_0=45,lon_0=-
100,)m.etopo(scale=0.5,
alpha=0.5)def draw_map(m,scale=0.2):
draw a shaded-relief
img=m.shadedrelief(scale=scale)
lats and longs are returned as a
dictionary lats=m.drawparallels(np.linspace(-
90,90,13))
lons = m.drawmeridians(np.linspace(-180, 180,
13))# keys contain the plt.Line2D instances
lat_lines = chain(*(tup[1][0] for tup in
lats.items()))lon_lines=chain(*(tup[1][0]for
tup in lons.items()))all_lines=chain(lat_lines,lon_lines)
cycle through these lines and set the desired style for
line in all_lines:
line.set(linestyle='-',alpha=0.3,color='r')
```



## Map Projections

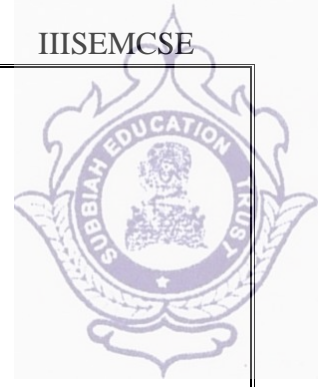
The Basemap package implements several dozen such projections, all referenced by a short format code. Here we'll briefly demonstrate some of the more common ones.

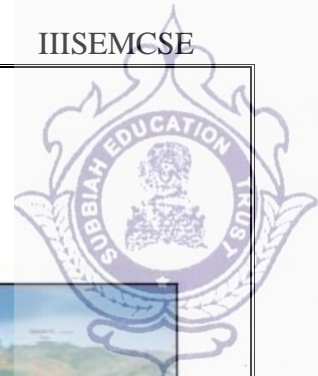
- Cylindrical projections
- Pseudo-cylindrical projections
- Perspective projections
- Conic projections

### Cylindrical projection

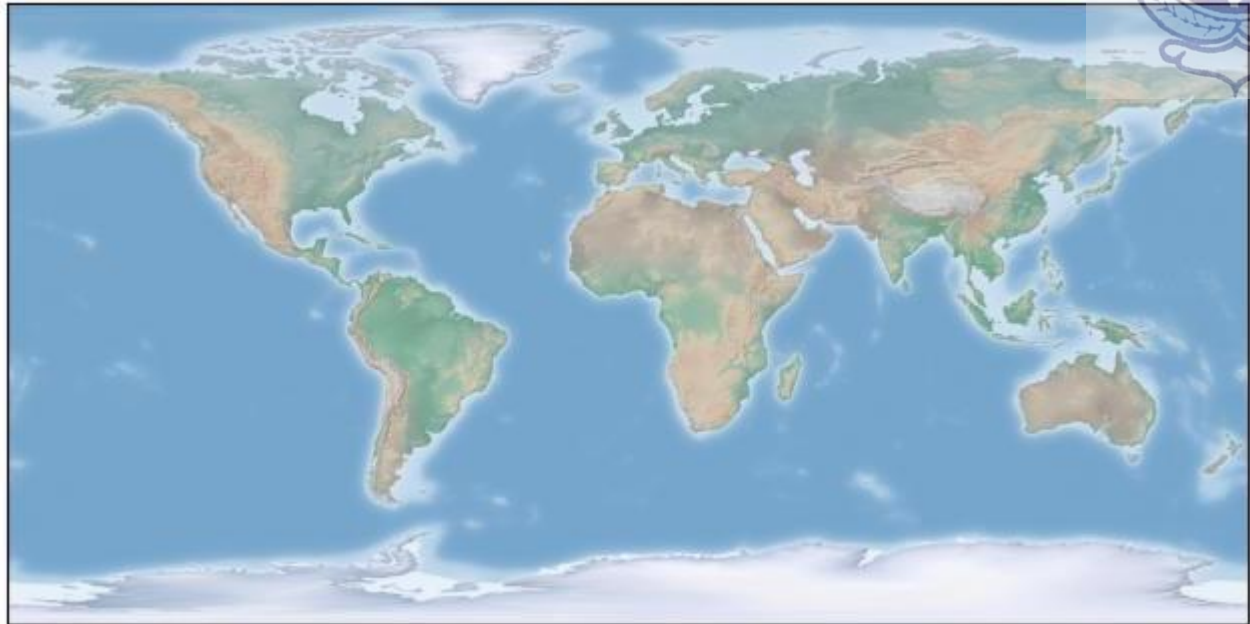
- The simplest of map projections are cylindrical projections, in which lines of constant latitude and longitude are mapped to horizontal and vertical lines, respectively.
- This type of mapping represents equatorial regions quite well, but results in extreme distortions near the poles.
- The spacing of latitude lines varies between different cylindrical projections, leading to different conservation properties, and different distortion near the poles.
- Other cylindrical projections are the Mercator (projection='merc') and the cylindrical equal-area (projection='cea') projections.
- The additional arguments to Basemap for this view specify the latitude (lat) and longitude (lon) of the lower-left corner (llcrnr) and upper-right corner (urcrnr) for the desired map, in units of degrees.

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.basemap import Basemap
```





```
fig=plt.figure(figsize=(8,6),edgecolor='w')
m = Basemap(projection='cyl',
resolution=None,llcrnrlat=-90,urcnrlat=90,
llcrnrlon=-180,urcnrlon=180,
)draw_map(m)
```



**Pseudo-cylindrical projections**

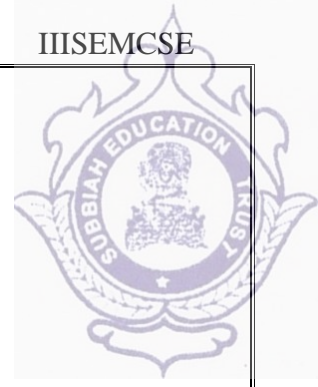
- Pseudo-cylindrical projections relax the requirement that meridians (lines of constant longitude) remain vertical; this can give better properties near the poles of the projection.
- The Mollweide projection (projection='moll') is one common example of this, in which all meridians are elliptical arcs
- It is constructed so as to
- preserve area across the map: though there are distortions near the poles, the area of small patches reflects the true area.
- Other pseudo-cylindrical projections are the sinusoidal (projection='sinu') and Robinson (projection='robin') projections.
- The extra arguments to Basemap here refer to the central latitude (lat\_0) and longitude (lon\_0) for the desired map.

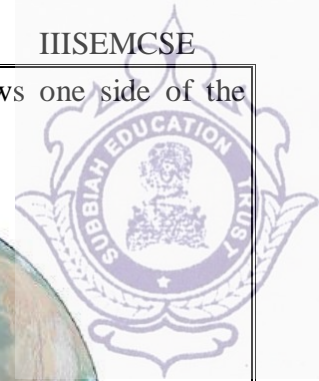


```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.basemap import
Basemap fig=plt.figure(figsize=(8,6),edgecolor
='w')
m = Basemap(projection='moll',
resolution=None,lat_0=0,lon_0=0)
draw_map(m)
```

**Perspective projections**

- Perspective projections are constructed using a particular choice of perspective point, similar to if you photographed the Earth from a particular point in space (a point which, for some projections, technically lies within the Earth!).





- One common example is the orthographic projection (projection='ortho'), which shows one side of the globe as seen from a viewer at a very long distance.
- Thus, it can show only half the globe at a time.
- Other perspective-based projections include the gnomonic projection (projection='gnom') and stereographic projection (projection='stere').
- These are often the most useful for showing small portions of the map.



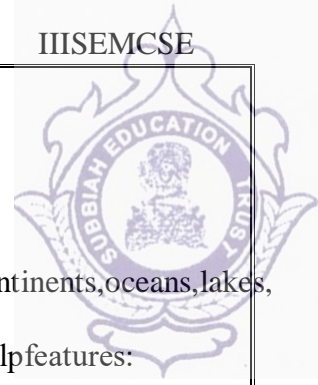
```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.basemap import
Basemap
fig = plt.figure(figsize=(8,8))
m = Basemap(projection='ortho',
resolution=None, lat_0=50, lon_0=0)
draw_map(m);
```

### Conic projections

- A conic projection projects the map onto a single cone, which is then unrolled.
- This can lead to very good local properties, but regions far from the focus point of the cone may become very distorted.
- One example of this is the Lambert conformal conic projection (projection='lcc').
- It projects the map onto a cone arranged in such a way that two standard parallels (specified in Basemap by lat\_1 and lat\_2) have well-represented distances, with scale decreasing between them and increasing outside of them.
- Other useful conic projections are the equidistant conic (projection='eqdc') and the Albers equal-area (projection='aea') projection

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.basemap import
Basemap
fig = plt.figure(figsize=(8,8))
m = Basemap(projection='lcc', resolution=None,
lon_0=0, lat_0=50, lat_1=45, lat_2=55, width=1.6E7,
height=1.2E7)
draw_map(m)
```





## Drawing a Map Background

The Basemap package contains a range of useful functions for drawing borders of physical features like continents, oceans, lakes, and rivers, as well as political boundaries such as countries and US states and counties.

The following are some of the available drawing functions that you may wish to explore using IPython's help features:

- Physical boundaries and bodies of

water drawcoastlines()-

Draw continental coastlines

drawlsmask() - Draw a mask between the land and sea, for use with projecting images on one or the

other drawmapboundary() - Draw the map boundary, including the fill color for oceans

drawrivers() - Draw rivers on the map

fillcontinents()- Fill the continents with a given color; optionally fill lakes with another color

- Political boundaries

drawcountries() - Draw country

boundaries drawstates() - Draw US state

boundaries drawcounties()-

Draw US county boundaries

- Map features

drawgreatcircle() - Draw a great

circle between two points drawparallels() - Draw lines of

constant latitude drawmeridians() - Draw lines of constant

longitude drawmapscale()- Draw a linear scale on the map

- Whole-globe images

bluemarble() -

Project NASA's bluemarble image onto the map shadedrelief() -

Project a shaded relief image onto the map etopo()- Draw an

etopo relief image onto the map

warpimage()- Project a user-provided image onto the map

## Plotting Data on Maps

- The Basemap toolkit is the ability to over-plot a variety of data onto a map background.

- There are many map-specific functions available as methods of the Basemap

instance. Some of these map-specific methods are:

contour()/contourf()-

Draw contour lines or filled contours imshow()- Draw an

image

pcolor()/pcolormesh()- Draw

a pseudocolor plot for irregular/regular meshes plot()- Draw lines and/or markers

scatter()-

Draw points with markers quiver()-

Draw vectors

barbs() - Draw wind

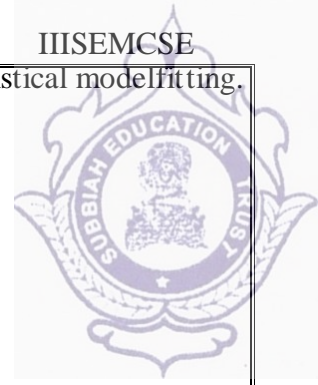
barbs drawgreatcircle()-

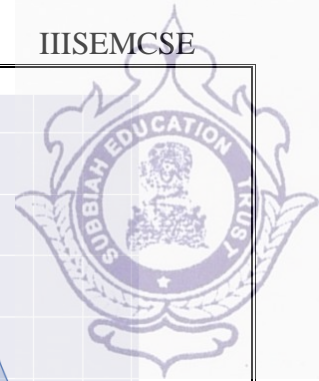
Draw a great circle

## Visualization with Seaborn

The main idea of Seaborn is that it provides high-

level command to create a variety of plot types useful for statistical data exploration, and even some statistical model fitting.





### Histograms, KDE, and densities

- In statistical data visualization, all you want is to plot histograms and joint distributions of variables. We have seen that this is relatively straightforward in Matplotlib
- Rather than a histogram, we can get a smooth estimate of the distribution using a kernel density estimation, which Seaborn does with `sns.kdeplot`

```
import pandas as pd
import seaborn as sns
```

```
data = np.random.multivariate_normal([0,0],[[5,2],[2,2]],size=2000)
```

```
data = pd.DataFrame(data,columns=['x','y'])
```

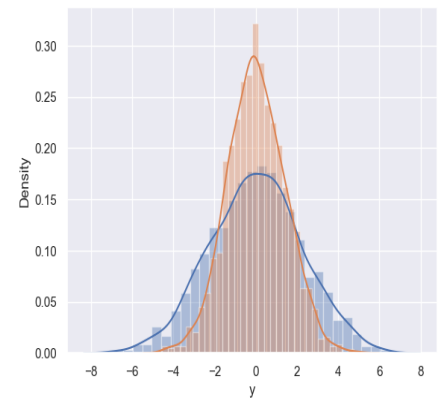
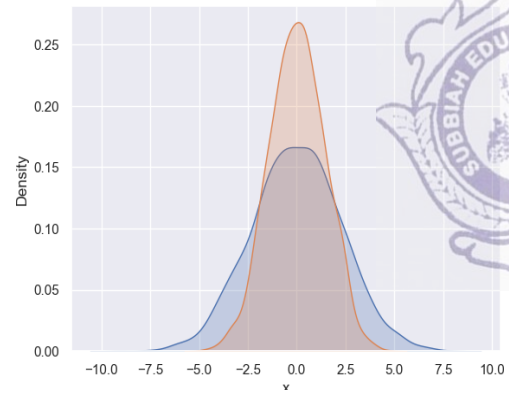
```
for col in 'xy':
 sns.kdeplot(data[col],shade=True)
```

- Histograms and KDE can be combined using `distplot`

```
sns.distplot(data['x'])
sns.distplot(data['y']);
```

- If we pass the full two-dimensional dataset to `kdeplot`, we will get a two-dimensional visualization of the data.

- We can see the joint distribution and the marginal distributions together using `sns.jointplot`.

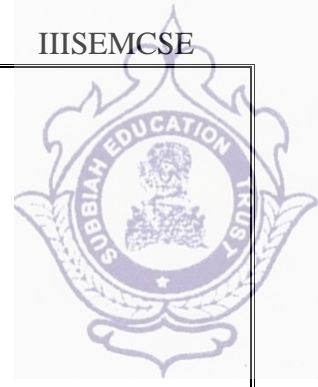


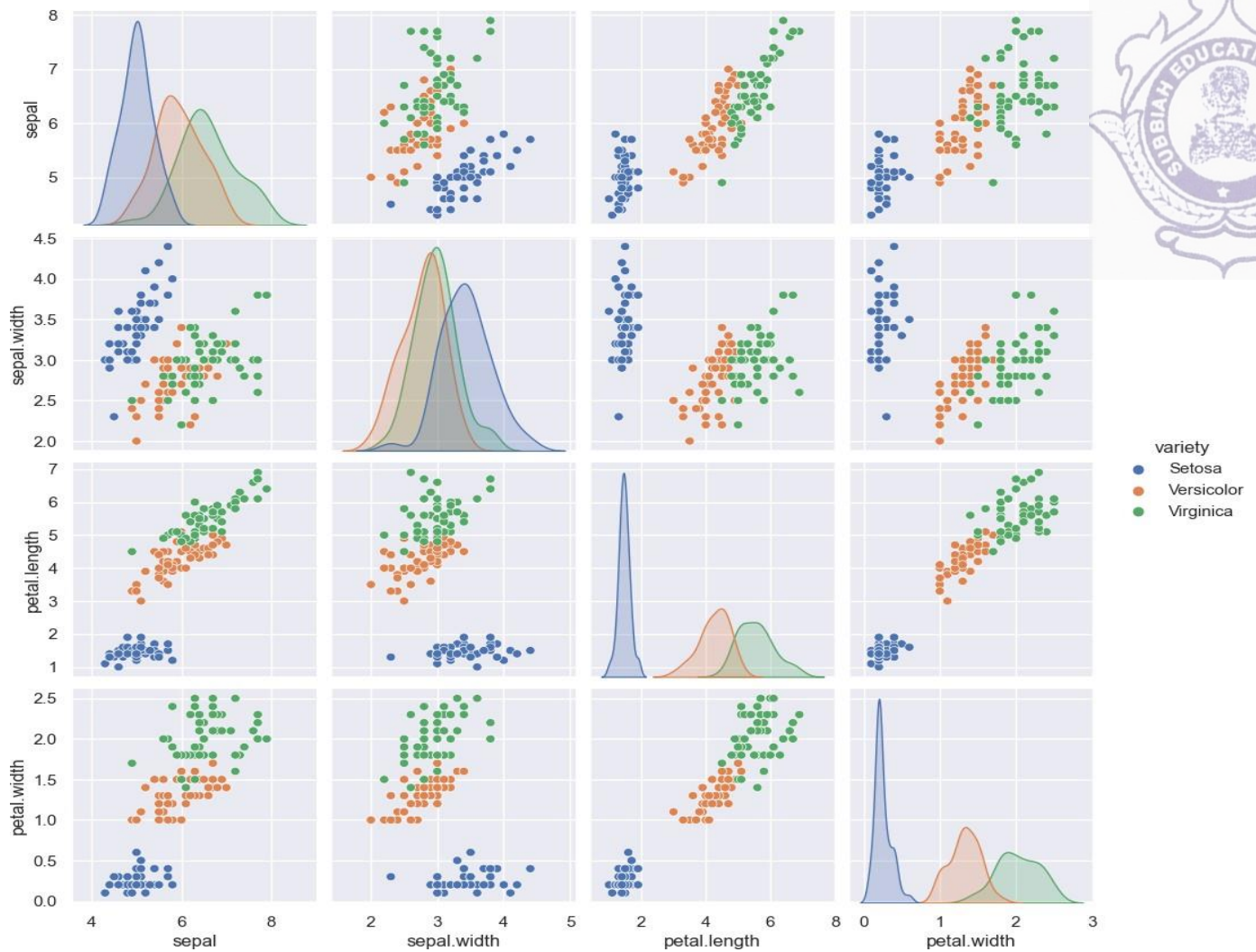
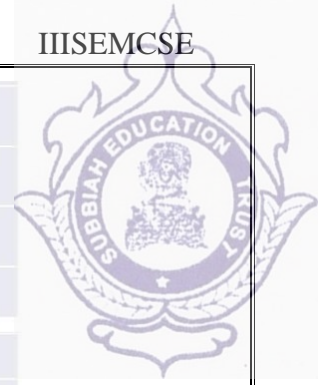
### Pairplots

When you generalize `jointplot` to a dataset of larger dimensions, you end up with pairplots. This is very useful for exploring correlations between multidimensional data, when you'd like to plot all pairs of values against each other.

We'll demo this with the Iris dataset, which lists measurements of petals and sepals of three iris species:

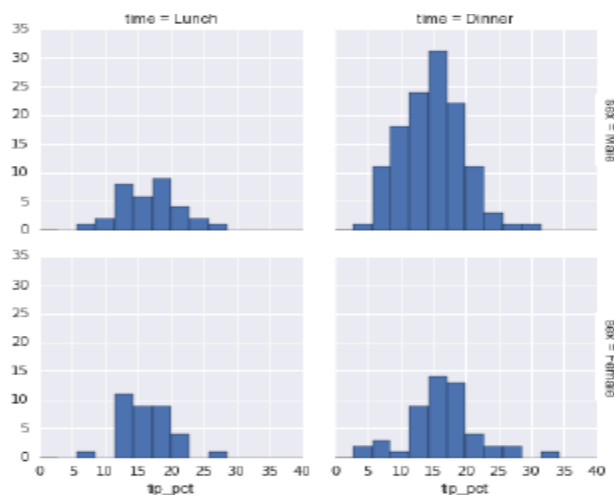
```
import seaborn as sns
iris = sns.load_dataset("iris")
sns.pairplot(iris, hue='species', size=2.5);
```





**Faceted histograms**

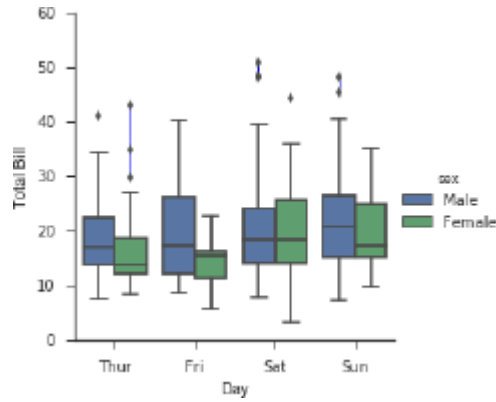
- Sometimes the best way to view data is via histograms of subsets. Seaborn's FacetGrid makes this extremely simple.
- We'll take a look at some data that shows the amount that restaurant staff receive in tips based on various indicator data





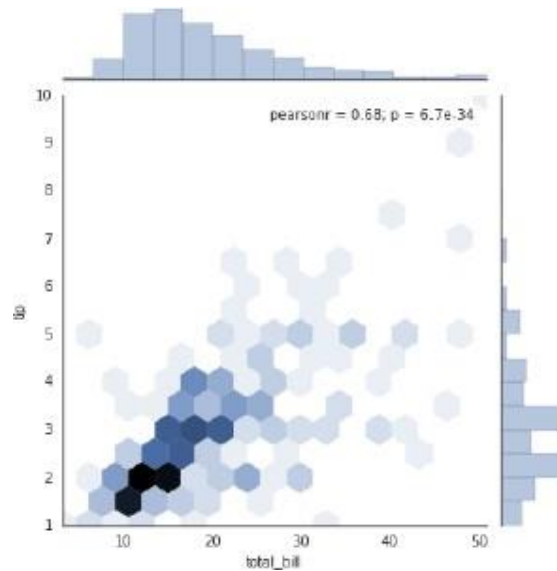
**Factorplots**

Factorplots can be useful for this kind of visualization as well. This allows you to view the distribution of a parameter within bins defined by any other parameter.



**Jointdistributions**

Similar to the pairplot we saw earlier, we can use `sns.jointplot` to show the joint distribution between different datasets, along with the associated marginal distributions.



**Barplots**

Time series can be plotted with `sns.factorplot`.

